Viscosity of Metallic Glass Forming Liquids: Analysis Based on Bond Strength-Coordination Number Fluctuations

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Abstract. A model that describes the viscous behavior in terms of the mean values of the bond strength, the coordination number, and their fluctuations of the structural units that form the melt has been proposed by one of the authors. In the present study, the viscous behavior of several metallic glass forming systems are analyzed by using the model. From the analysis, microscopic information such as the number of bonds that must be broken to observe the viscous flow is obtained. It is also shown that when the magnitudes of energy and coordination number fluctuations are equal, the behavior of the viscosity described by our model corresponds perfectly to the behavior described by the Vogel-Fulcher-Tammann (VFT) equation.

Introduction

In recent years, multicomponent bulk metallic glasses have attracted considerable interest [1-6]. In contrast to traditional amorphous metals, these new alloys have low critical cooling rates and fully amorphous samples with one side dimension as large as 1 cm can be produced by conventional cooling processes. The bulk metallic glasses are characterized by the high thermal stability of their supercooled liquids, which permit the study of thermophysical properties in the supercooled liquid state in addition to the amorphous solids [7-9]. In order to use efficiently the unique properties of bulk metallic glasses such as extraordinary high strength, low ductility, high hardness, excellent corrosion resistance, etc., a good understanding of fundamental materials properties is indispensable. In the present study, the viscous behavior of several metallic glass forming systems are analyzed by using a model for the viscosity proposed by one of the authors [10]. From the analysis, microscopic information such as the number of bonds that must be broken to observe the viscous flow is obtained. It will be also shown that under certain condition, the behavior of the viscosity described by our model corresponds perfectly to the behavior described by the well known Vogel-Fulcher-Tammann (VFT) equation. Furthermore, the bulk metallic glass forming materials will be characterized by studying the trend in the temperature dependence of the viscosity among oxides, chalcogenides and polymeric glass forming liquids.

Model and Results

The temperature dependence of the viscosity for various glass forming materials is conventionally characterized by the so-called Angell's plot [11]. By plotting the logarithm of the viscosity η as a function of the reduced inverse temperature T_g/T , where T_g is the glass transition temperature, curves with different degrees of non-Arrhenius behavior may be systematized. The degree of deviation from the Arrhenius behavior is called fragility. For highly polymerized network glass formers such as SiO₂, nearly straight lines in $\ln \eta$ vs T_g/T plot are observed. These types of materials exhibit small values of fragility and are called strong systems. On the other hand, for systems with non-directional interatomic or intermolecular bonds such as ionic or organic liquids, strong deviations from the Arrhenius behavior are observed. These types of materials exhibit large values of fragility and are called fragiles.

The concept of fragility has been used widely and has played a fundamental role in understanding the relaxation behavior of supercooled liquids. However, the microscopic mechanism responsible for the degree of fragility is still not well understood. Some years ago, one of the authors has derived an expression for the fragility based on a simple model of the melt [10]. According to the model, the fragility is determined by the relaxation of structural units that form the melt and is described in terms of the bond strength, the coordination number and their fluctuations of the structural units.

The glass forming melt is formed by an agglomeration of structural units. As the temperature of the system is lowered, the viscosity of the melt increases and at the glass transition temperature T_{g} , the spatial distribution of the structural units is frozen. In our model, each structural unit is bound to other structural units by a certain bond strength which is denoted as

$$E = E_0 + \Delta E , \qquad (1)$$

where E_0 is the average value and ΔE is its fluctuation. Each structural unit is surrounded by a certain number of other structural units. The coordination number of the structural units is denoted as

$$Z = Z_0 + \Delta Z \,, \tag{2}$$

where Z_0 is the average value and ΔZ is its fluctuation. According to the model, the viscous flow occurs when the structural units move from one position to another by breaking the bonds connecting the structural units. Based on this picture, the temperature dependence of the viscosity has been described as

$$\ln\left(\frac{\eta}{\eta_0}\right) = \frac{Cx + Cx^2 \left\{ \left[\ln\left(\frac{\eta_{Tg}}{\eta_0}\right) + \frac{1}{2}\ln(1-B)\right] \frac{(1-B)}{C} - 1 \right\} - \frac{1}{2}\ln(1-Bx^2), \quad (3)$$

where

$$B = \frac{(\Delta E)^2 (\Delta Z)^2}{R^2 T_g^2}, \qquad C = \frac{E_0 Z_0}{R T_g}, \quad \text{and} \quad x = \frac{T_g}{T}.$$
 (4)

Here, *R* is the gas constant. η_{T_g} and η_0 are the viscosities at the glass transition temperature and at the high temperature limit, respectively. For their values, the usual values $\eta_{T_g} = 10^{12}$ Pa·s and $\eta_0 = 10^{-5}$ Pa·s were adopted [11]. Note that the expression of the viscosity given above is written in terms of physically intuitive quantities *B*, *C*, and *x*. *C* gives the total bond strength of the structural unit and *B* gives its fluctuation. By using Eq. 3, the fragility index is calculated as

$$m = \lim_{T \to T_g} \frac{d \log \eta}{d(T_g/T)} = \frac{B - C + 2\left[\ln\left(\frac{\eta_{T_g}}{\eta_0}\right) + \frac{1}{2}\ln(1-B)\right]}{2.3(1-B)}.$$
(5)

In previous reports [9,10,12,13], there were shown that by choosing appropriately the values of B and C, the model reproduces quite well the temperature dependence of the viscosity of many kind of materials that includes oxides, chalcogenides, polymeric and metallic systems. The model provides also a clear picture to understand the viscous flow. For instance, by using the fitted values of B and C,



Fig. 1. The behavior of m and N_B in the B and C plane. The values of B and C determined for several compounds are also shown. The painted zone indicates the empirical relation found between B and C. The thick line represents the behavior of Eq. (7).

information on the number of bonds that must be broken to observe the viscous flow has been extracted [9]. It is written as

$$N_{B} = \frac{B - C + 2\left[\ln\left(\frac{\eta_{T_{g}}}{\eta_{0}}\right) + \frac{1}{2}\ln(1 - B)\right]}{(1 - B)C}.$$
(6)

The behavior of N_B is shown in Fig. 1 together with the behavior of the fragility index *m*. The painted zone indicates the empirical correlation found between *B* and *C* [9]. The values of *B* and *C* obtained for some materials are also shown. We can recognize that bulk metallic glass forming liquids considered here have intermediate values of fragility index that extend from about 30 to 55 and that the values of N_B extend from about 3 to 20 structural units. It should be noted that N_B increases with the increase of *m*. This behavior indicates that large numbers of structural units are involved in the viscous flow of a fragile system. This observation is in harmony with the concept of Cooperatively Rearranging Region in the theory of Adam and Gibbs [14]. Concerning the relationship between *B* and *C*, a theoretical expression has been derived from the model [12,13]. It is written as

$$C = \frac{2\gamma(1-B)}{2\gamma + \sqrt{B}(1+\gamma^2)} \left[\ln\left(\frac{\eta_{T_g}}{\eta_0}\right) + \frac{1}{2}\ln(1-B) \right], \quad \gamma = \frac{|\Delta E|/E_0}{|\Delta Z|/Z_0}.$$
(7)

The behavior of this expression for the case of $\gamma = 1$ is shown in Fig. 1 by a thick line. Eq. (7) is of particular interest because, it reproduces exactly the behavior of the viscosity described by the well known Vogel-Fulcher-Tammann (VFT) equation [12,15]. Examples of such correspondences are illustrated in Fig. 2, where the temperature dependences of the viscosity and relaxation time calculated by the two models are compared. The numbers in the figure indicate the systems that are given in Table 1. The symbols in the table are the usual quantities used in the VFT equation,

$$\ln \eta = \ln \eta_0 + \frac{B_{VFT}}{T - T_0},\tag{8}$$

where B_{VFT} and T_0 are the two VFT parameters which are usually used as fitting parameters and η_0 is the viscosity at the high temperature limit. The perfect correspondence between our model and the VFT equation has been also confirmed for the case of oxide glass forming liquids [12].



Fig. 2. Normalized temperature dependence of the viscosity and relaxation time in some bulk metallic glass forming systems calculated by the Bond Strength-Coordination Number Fluctuation Model (full lines) and by the VFT equation (symbols). The relaxation time is calculated by $\tau = \eta / G_{\infty}$, where G_{∞} is the shear modulus at high frequency. The numbers indicate the systems given in Table 1.

No.	Material	$B_{\rm VFT}$ [K]	<i>T</i> ₀ [K]	$T_{g}[K]$	т	$\ln(\eta_{T_g}/\eta_{T_0})$	(B, C)
1.	Zr _{46.75} Ti _{8.25} Cu _{7.5} Ni ₁₀ Be _{27.5}	7848	381	596	44.0	36.51	(0.409, 13.1)
2.	$Mg_{65}Cu_{25}Y_{10}$	5827	259	411	45.0	38.34	(0.372, 14.1)
3.	$Pd_{48}Ni_{32}P_{20}$	5333	401	566	48.2	32.32	(0.503, 9.3)
4.	Zr _{41,2} Ti _{13,8} Cu _{12,5} Ni ₁₀ Be _{22,5}	7705	412	615	49.9	37.96	(0.449, 12.4)
5.	$Pt_{60}Ni_{15}P_{25}$	4828	340	463	64.2	39.25	(0.540, 10.3)
6.	Pd _{77.5} Cu ₆ Si _{16.5}	3137	506	613	73.0	29.32	(0.683, 5.0)
7.	Pd ₇₇ Cu _{6.5} Si _{16.5}	6852	463	620	74.9	43.64	(0.559, 10.9)
8.	Au _{76.9} Ge _{13.65} Si _{9.45}	1523	238	285	85.4	32.41	(0.699, 5.2)
9.	Al ₈₅ Ni ₈ Ce ₇	1345	498	535	228.2	36.34	(0.868 2.4)
10.	Ni ₆₅ Nb ₃₅	4861	784	908	124.1	39.10	(0.748, 5.2)
11.	$Ni_{60}Nb_{35}Sn_5$	7370	670	858	77.3	39.10	(0.611, 8.4)
12.	Ni ₅₇ Fe ₃ Nb ₃₅ Sn ₅	9692	591	839	57.5	39.10	(0.496, 11.5)
13.	Ni ₆₀ (Nb ₄₀ Ta ₆₀) ₃₄ Sn ₆	11039	581	863	51.9	39.10	(0.454, 12.7)
14.	$Pd_{40}Ni_{40}P_{20}$	7059	390	578	50.1	37.55	(0.456, 12.1)
15.	$Cu_{47}Ti_{34}Zr_{11}Ni_8$	6000	500	673	58.6	34.68	(0.553, 8.8)
16.	La ₅₅ Al ₂₅ Ni ₅ Cu ₁₀ Co ₅	6657	241	466	26.7	29.65	(0.268, 14.2)
17.	La ₅₅ Al ₂₅ Ni ₅ Cu ₁₅	5027	286	459	33.3	28.97	(0.387, 10.9)
18.	La ₅₅ Al ₂₅ Ni ₂₀	5517	307	491	34.7	29.98	(0.391, 11.2)

Table 1. VFT parameters B_{VFT} , T_0 , glass transition temperature T_g , fragility index *m* and the parameters of our model *B* and *C*, for some metallic glass forming systems. Materials data are taken from [16-18].

From Table 1, we note that the values of $\ln(\eta_{T_g}/\eta_0)$ are not constant. This is in contrast with the usual representation of the temperature dependence of the viscosity in the Angell's plot, where it is fixed at $\ln(\eta_{T_g}/\eta_0) = 39.1[11]$. Due to this difference, not all the systems tabulated in Table 1

collapse on a single curve. This situation is illustrated in Fig. 3. Note that all the data are located between the two boundary curves determined by $\ln(\eta_{Tg}/\eta_0) = 39.1$ and 29.7.

According to our model, the observation that most systems have values of *B* and *C* around the thick line in Fig. 1, indicates that the degree of energy fluctuation and the coordination number fluctuation are almost the same. Deviations from the $\gamma = 1$ line indicate that the magnitudes of such fluctuations are different. It is known that a single VFT equation can not reproduce the viscosity data when the temperature range is wide enough [19]. Our Bond Strength-Coordination Number Fluctuation Model fits the experimental data better than the VFT relation. Physically, this is possible by relaxing the condition $\gamma = 1$.



Fig. 3. The values of the parameters *B* and *C* determined for the metallic glass forming systems tabulated in Table 1. The two curves are drawn by using different values of $\ln(\eta_{T_{\sigma}}/\eta_0)$.

Summary

The viscosity of the liquids increases drastically when the temperature is lowered and approaches the glass transition temperature. At the microscopic scale, the constituent elements of a glass are considered to form certain types of clusters or structural units. Such structural units are bound to other structural units by certain bond strength by retaining its spatial random connectivity. Within the glass, the thermally activated viscous flow occurs by bond-breaking and bond-switching. Based on this picture, a model for the temperature dependence of the viscosity has been proposed by one of the authors. The model describes the viscosity behavior in terms of the mean values of the bond strength, the coordination number, and their fluctuations of the structural units that form the melt.

In the present study, the viscous behavior of several metallic glass forming systems are analyzed by using the above mentioned model. From the analysis, microscopic information such as the number of bonds that must be broken to observe the viscous flow has been obtained. It has been shown that this quantity increases with the increase in the fragility and is intimately related with the magnitude of the cooperatively rearranging region in the theory of Adam and Gibbs. It has been also shown that when the magnitude of bond strength energy and coordination number fluctuations between the structural units are the same, the behavior of the viscosity described by our model corresponds perfectly to the behavior described by the phenomenological VFT equation. This finding is expected to provide a microscopic physical interpretation to the parameters used in the VFT equation. By studying the materials trend in the temperature dependence of the viscosity that includes oxides, chalcogenides, polymers and metallic glass forming liquids, it was shown that metallic systems have intermediate values of fragility.

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