

**A Theoretical Study of some Elementary Steps Involved in  
Catalytic Cycles by Enzymes and Transition Metal  
Complexes**

酵素及び遷移金属錯体の触媒サイクルに含まれる  
素反応過程に関する理論的研究

学位論文

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**A THEORETICAL STUDY OF SOME  
ELEMENTARY STEPS INVOLVED IN  
CATALYTIC CYCLES BY ENZYMES AND  
TRANSITION METAL COMPLEXES**

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**1994**

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## General Introduction

### 1.1 Background

The catalyst is of importance in many fields, such as synthetic and organic chemistry, biochemistry, and industrial chemistry. In general, the catalyst promotes the chemical reactions by activating chemically inactive or less active molecules, and stabilizing reactive intermediates and/or transition states. There are recent increasing interests on catalyses of the transition-metal complexes and enzymes. This is because transition-metal complexes and enzymes perform various catalytic reactions under mild reaction conditions, and several times, those reactions are highly selective. However, enzyme is generally expensive and much sensitive to reaction conditions; for instance, they are active at only moderate temperature and in the neutral pH region. Therefore, intensive efforts have been made to develop artificial enzymic catalysts that can be used under reaction conditions of wide range. Also, in transition metal catalysts, there remain several points to be solved; for instance, separation of products from substrates and catalysts, use of less expensive metals unlike rhodium and platinum, use of simple ligand, etc. In order to develop such useful catalyst, we need detailed information on the geometry, electronic state, and bonding nature of the intermediate involved in catalytic reactions. However, isolation, identification, and characterization of the intermediates are very difficult because the amount of intermediate is very small and its reactivity is high in general.

Under these circumstances, theoretical study is expected

to offer valid information not only on the geometry, electronic structure, and bonding nature of the intermediate but also on the transition state of the catalytic reaction. In this thesis, we present theoretical studies on several elementary processes involved in catalytic reactions by enzymes and transition metal complexes. The ab initio MO method is mainly employed here, in which the electron correlation effects are considered with the second ~ fourth order Møller-Plesset perturbation (MP2 ~ MP4) and single and double excitation-configuration interaction (SD-CI) methods. Detailed knowledge obtained in this thesis is expected to be useful for designing a good catalyst for CO<sub>2</sub> fixation.

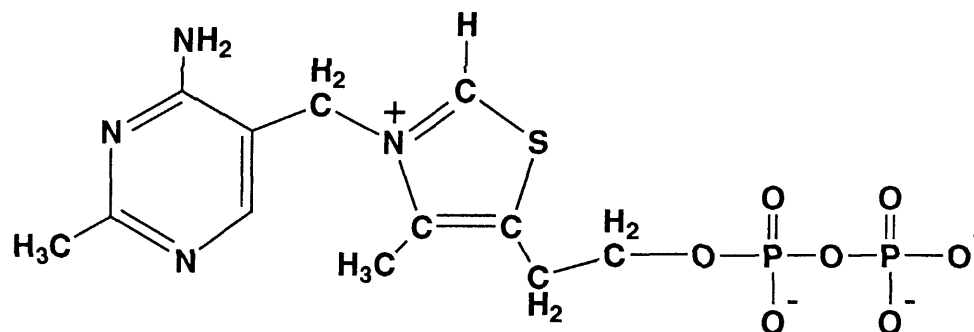
In this chapter, reactions examined here are reviewed, the first is coenzyme-catalyzed carboxylation and decarboxylation reactions, the second is the CO<sub>2</sub> insertion reaction into transition metal-hydride and alkyl bonds, and the third is the oxidative addition of the Si-X  $\sigma$ -bond to transition metal complexes. Also, the aims of the present study are described.

## **1.2 Coenzyme Catalyses of Carboxylation and Decarboxylation**

The coenzyme is, in general, necessary as a cofactor in the enzymic reaction and plays an important catalytic function. In enzymic reactions, there are two typical reactions related to CO<sub>2</sub> fixation; one is decarboxylation of pyruvate anion and the other is transcarboxylation reactions. These decarboxylation and transcarboxylation are considered to be important not only as metabolic functions but also as useful function for CO<sub>2</sub> fixation.<sup>1-11</sup>

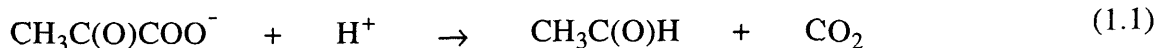
In decarboxylation reactions, thiamin diphosphate (TDP, vitamin B<sub>1</sub>) shown in Figure 1.1 is a coenzyme of pyruvate





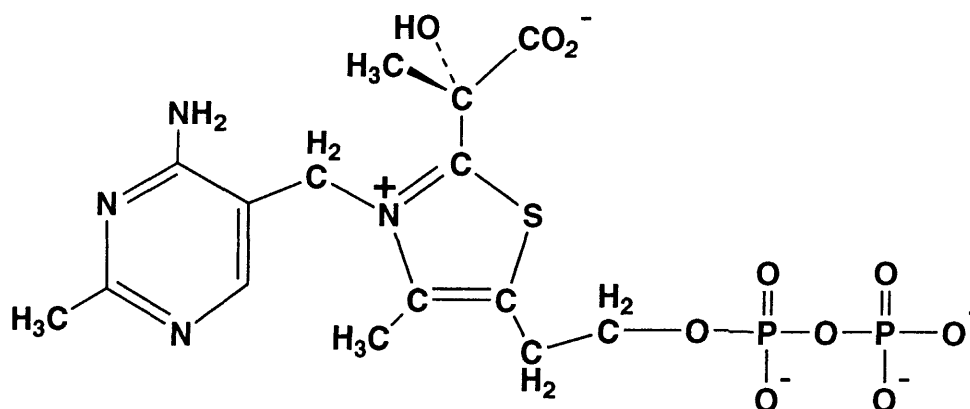
**Figure 1.1** Thiamin Diphosphate (TDP)

decarboxylase which catalyzes the conversion of pyruvate to acetaldehyde and carbon dioxide (eq 1.1).<sup>12</sup> This reaction can be seen as electrophilic substitution of carbon dioxide for proton at an acyl carbon.<sup>12</sup>

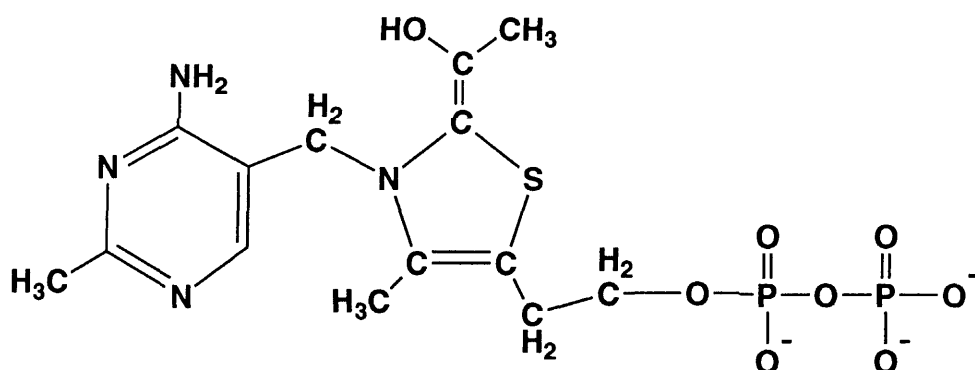


In general, the carbon atom of carbonyl is favorable for nucleophilic substitution rather than electrophilic substitution, because of its electropositive character. In fact, this type of reaction is chemically unprecedented. In spite of such unfavorable situation, the enzymic system of TDP reacts with pyruvate to form a lactyl-TDP (LTDP, Figure 1.2), in which electron density increases at the carbon atom of the carbonyl group, to accelerate the proton attack to the carbonyl carbon atom. It has been experimentally reported that the coenzyme of TDP is important in decarboxylation of pyruvate and TDP itself can catalyzes its decarboxylation.<sup>13</sup>

Although many experimental works have been carried out on TDP, there still remain several issues to be examined as follows;



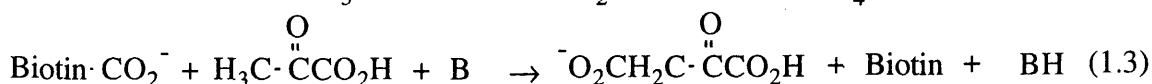
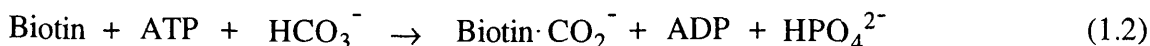
**Figure 1.2** Lactyl-Thiamin Diphosphate (LTDP)



**Figure 1.3** Enamine intermediate

- (1) Geometry of LTDP (Figure 1.2) has not been known because LTDP is high by reactive species and its life time is only a few minutes.<sup>14</sup>
- (2) It has not been fully investigated whether an enamine intermediate (Figure 1.3) is involved in the reaction or not.
- (3) Geometry of transition state, activation energy, and reaction energy of decarboxylation of LTDP have not been fully investigated.

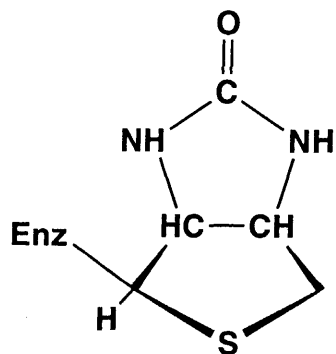
Transcarboxylation is catalyzed by biotin (vitamin H, see Figure 1.4). This is a coenzyme which catalyzes the bond formation between the carboxylate group derived from bicarbonate ( $\text{HCO}_3^-$ ) and a carbon atom adjacent to a carbonyl group. The reaction mechanism is summarized as follows;<sup>15-17</sup>



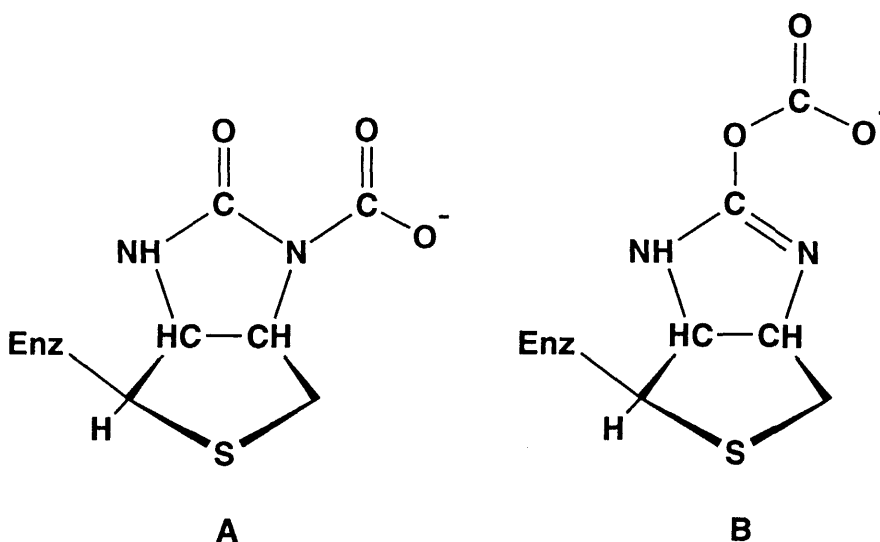
First, carboxybiotin is formed from biotin,  $\text{HCO}_3^-$ , adenosine triphosphate (ATP) (eq 1.2), accompanied with conversion of ATP to adenosine diphosphate (ADP), and inorganic phosphate.<sup>18,19</sup> Then, the carboxyl group transfers from carboxybiotin to an  $\alpha$ -carbon of the carbonyl compound (eq 1.3).<sup>20-22</sup>

Interestingly, two kinds of intermediate were proposed in biotin carboxylation; one is N-carboxybiotin (Figure 1.5A) and the other is O-carboxybiotin (Figure 1.5B). Imoto et al. reported that imidazolidone ring is less reactive for carbon dioxide<sup>23</sup> and Caplow found that carbonyl group of carboxybiotin is less electrophilic.<sup>24</sup> These experimental results suggested that biotin-dependent carboxylation proceeds via the O-carboxybiotin.<sup>25</sup> On the other hand, Lane et al. obtained the experimental result that supports the existence of N-carboxylated species in biotin-dependent enzymic reaction by confirming the enzyme activity of N-carboxybiotin derivative isolated.<sup>26</sup> Thus, N-carboxylation mechanism has been undoubtedly accepted now.

Considering the above-mentioned discussion presented in experimental field, following issues should be examined to understand well the mechanism of biotin-dependent catalytic reaction;



**Figure 1.4** d-(+)-Biotin



**Figure 1.5** N-carboxybiotin **A** and O-carboxybiotin **B**

- (1) Geometry, reactivity, and electronic structure of N-carboxybiotin.
- (2) Comparison of N-carboxylation with O-carboxylation.

### 1.3 Catalyses of Transition-metal Complexes Related to CO<sub>2</sub> Fixation

Recently, chemical fixation of CO<sub>2</sub><sup>27</sup> becomes of great importance because of increase in the concentration of CO<sub>2</sub> in the atmosphere.

In electrochemical<sup>28-41</sup> and photochemical<sup>42-46</sup> reduction of CO<sub>2</sub> catalyzed by transition-metal complexes or enzyme, CO<sub>2</sub> is converted into useful substances such as carbon monoxide, methanol, formic acid, oxalic acid, organic acids, and methane.

In spite of many experimental works, only a few processes using CO<sub>2</sub> as raw material for carbon source have been developed. Considering this unsuccessful situation in the CO<sub>2</sub> fixation, detailed theoretical information on the reactions of CO<sub>2</sub> is necessary to find an excellent catalyst for the CO<sub>2</sub> fixation; for instance, geometry, bonding nature, and electronic structure of intermediate and transition state, the activation energy, and the reaction energy, are useful and indispensable for further development of the chemistry of CO<sub>2</sub> fixation.

In the many reactions of CO<sub>2</sub>, insertion of CO<sub>2</sub> into a M-R (R = hydride, alkyl, or alkoxide)<sup>47-53</sup> bond (eq 1.4) is

$$\begin{array}{l}
 (\text{L})_n\text{M-R} + \text{CO}_2 \quad \rightarrow \quad (\text{L})_n\text{M}(\eta^1\text{-OC(O)R}) \\
 \quad \quad \quad \quad \quad \quad \quad \quad \rightarrow \quad (\text{L})_n\text{M}(\eta^2\text{-O}_2\text{CR}) \quad (1.4)
 \end{array}$$

expected to be utilized for constructing the good catalytic system since many transition metal catalytic cycles involve the insertion reactions of alkene, alkyne, and carbonyl into a M-R bond. In fact, formyl or carboxyl group is formed through the insertion reaction of CO<sub>2</sub>, and they would play an important role as a precursor or an intermediate of catalytic CO<sub>2</sub> fixation. From those reasons, many experimental works have been actively carried out on the CO<sub>2</sub> insertion into the M-R bond.<sup>54-63</sup>

In contrast to these experimental works, only a few theoretical works on the insertion of CO<sub>2</sub> have been reported, to our knowledge. From theoretical works, we can

expect to obtain several informations on the CO<sub>2</sub> insertion into the M-R bond, as follows;

- (1) Changes in geometry, electron distribution, and bonding nature,
- (2) The activation energy and the reaction energy,
- (3) Reactivity of transition-metal-hydride and alkyl complexes in the CO<sub>2</sub> insertion, and
- (4) Differences in reactivity between CO<sub>2</sub> and C<sub>2</sub>H<sub>4</sub> in the insertion reaction.

#### **1.4 Oxidative Addition of the Si-X $\sigma$ -Bond to Transition-metal Complex**

Oxidative addition of the saturated  $\sigma$ -bond (eq 1.5) to transition-metal complexes is of importance in activation of saturated compound.<sup>64,65</sup> For instance, the oxidation addition of the C-H bond to transition metal complex is considered to be involved in activation of alkane.<sup>66</sup> In fact, the C-H bond activation of hydrocarbon was



experimentally found by Graham,<sup>67</sup> Bergman,<sup>68</sup> and Jones<sup>69</sup> and their co-workers. Mechanistic studies on this C-H bond activation have elucidated that the C-H bond activation is achieved by oxidative addition of the C-H bond to the coordinatively unsaturated transition-metal complex.<sup>66</sup>

Under these circumstances, several interesting theoretical works on the oxidative addition of H<sub>2</sub>, CH<sub>4</sub>, C<sub>2</sub>H<sub>6</sub>, have been carried out with the molecular orbital (MO) method.<sup>70-76</sup> In these studies, the detailed knowledge including the geometry of transition state, activation energy, the reaction energy has been presented.

Similar to the oxidative addition of the C-H  $\sigma$ -bond, the oxidative addition of Si-X  $\sigma$ -bond (X = H, CH<sub>3</sub>, or SiH<sub>3</sub>) (eq 1.6) is of importance in catalytic syntheses of various



organosilicon compounds; for instance, the Si-H oxidative addition is involved as a key process in transition-metal catalyzed hydrosilylation of alkene.<sup>77-80</sup> Also, the Si-Si oxidative addition is involved in bis-silylation of alkene and alkyne.<sup>81-90</sup>

Sakaki and his collaborator have investigated the oxidative addition of CH<sub>4</sub> and SiH<sub>4</sub> with Pt(PH<sub>3</sub>)<sub>2</sub>, by using ab initio MO method.<sup>91</sup> They showed that Si-H oxidative addition occurs much more easily with the lower activation energy and the larger exothermicity than the C-H oxidative addition.<sup>91</sup> Although palladium (0) complexes have often been used as catalysts in the bis-silylation,<sup>64a,76,82-87,88c,89</sup> previous theoretical work revealed that the Pd(0) complex was unfavorable for the oxidative addition of H-H and C-X (X = H, CH<sub>3</sub>) bonds.<sup>92</sup>

In this regard, it is necessary to investigate theoretically the oxidative addition of the Si-X  $\sigma$ -bond to the palladium (0) complex, in particular, to clarify the reason that the Si-H and Si-Si oxidative addition to palladium (0) complexes can proceed unlike the C-H and H-H oxidative addition. The detailed knowledge on these issues is expected to be useful to construct a efficient catalytic system for synthetic reaction of organosilicon compounds.

### 1.5 Aims of the present study

As described above, there remain many issues to be theoretically solved in catalytic reactions of enzymes and transition metal complexes. Aims of this thesis are summarized as follows.

In chapter 2, decarboxylation function of thiamin diphosphate was theoretically investigated. Aims of this chapter are;

- 1) to obtain detailed knowledge on geometry changes and energy changes in decarboxylation of 2-lactylthiazolium cation,
- 2) to offer theoretical evidence of the enamine intermediate, and
- 3) to make clear the differences in reactivity between 2-lactylthiazolium cation and the other two lactylazolium, 2-lactyloxazolium and 2-lactylimidazolium.

In chapter 3, carboxyimidazolidone was theoretically investigated as a model of carboxybiotin. The main purposes are;

- 1) to present information necessary for systematic theoretical investigation of biotin,
- 2) to present such detailed information as CO<sub>2</sub> binding energy, geometry, bonding nature, electron distribution, and reactivity of carboxyimidazolidone,
- 3) to compare N-carboxyimidazolidone with O-carboxyimidazolidone, and
- 4) to examine the stability of the  $\eta^2$ -side-on carboxyimidazolidone.

In chapter 4, theoretical investigation on the CO<sub>2</sub>



insertion into the Cu(I)-H and Cu-CH<sub>3</sub> bonds is presented, in comparing it with the similar C<sub>2</sub>H<sub>4</sub> insertion into the Cu(I)-H and Cu(I)-CH<sub>3</sub> bonds. Following issues are mainly discussed;

- 1) to offer detailed knowledge on the CO<sub>2</sub> insertion into the Cu-R bond, such as geometry change, electron redistribution, and transition state structure,
- 2) to estimate the activation energy and the reaction energy,
- 3) to compare the CO<sub>2</sub> insertion with the C<sub>2</sub>H<sub>4</sub> insertion, and
- 4) to explain the difference in the insertion reaction between CO<sub>2</sub> and C<sub>2</sub>H<sub>4</sub>.

In chapter 5, insertion of CO<sub>2</sub> into the Rh(I)-H bond of RhH(PH<sub>3</sub>)<sub>3</sub> is theoretically investigated. Also, in this chapter, detailed knowledge on the CO<sub>2</sub> insertion into the Rh(I)-H bond is presented like in chapter 4;

- 1) to make clear geometry change, electron distribution, and changes in bonding nature in the CO<sub>2</sub> insertion into the Rh(I)-H bond,
- 2) to estimate activation energy and reaction energy of CO<sub>2</sub> insertion into the Rh(I)-H bond, and
- 3) to compare the Rh(I) complex with the Cu(I) complex in the CO<sub>2</sub> insertion based on the energy decomposition analysis.

In chapter 6, the similar CO<sub>2</sub> insertion into the Rh(III)-H bond of [RhH<sub>2</sub>(PH<sub>3</sub>)<sub>3</sub>]<sup>+</sup> is theoretically investigated with the following purposes;

- 1) to estimate activation energy and reaction energy of CO<sub>2</sub> insertion into the Rh(III)-H bond,
- 1) to clarify the differences in reactivity between high and low oxidation states of Rh in CO<sub>2</sub> insertion, and

- 2) to predict a favorable transition-metal complex for CO<sub>2</sub> insertion.

In chapter 7, an oxidation addition of the Si-X (X = H, C, and Si) bond to the Pd(0) complex is theoretically investigated. Following aims are mainly examined.

- 1) to offer detailed information on the oxidative addition, such as the geometry of transition state, the activation energy, and the reaction energy,
- 2) to compare the reactivity of the Pd(0) complex with that of the Pt analogue, and
- 3) to clarify the reason that the activation energy of the Pd(0) reaction system is lower than that of the Pt reaction system, in spite of the lower exothermicity.

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## **Part I**

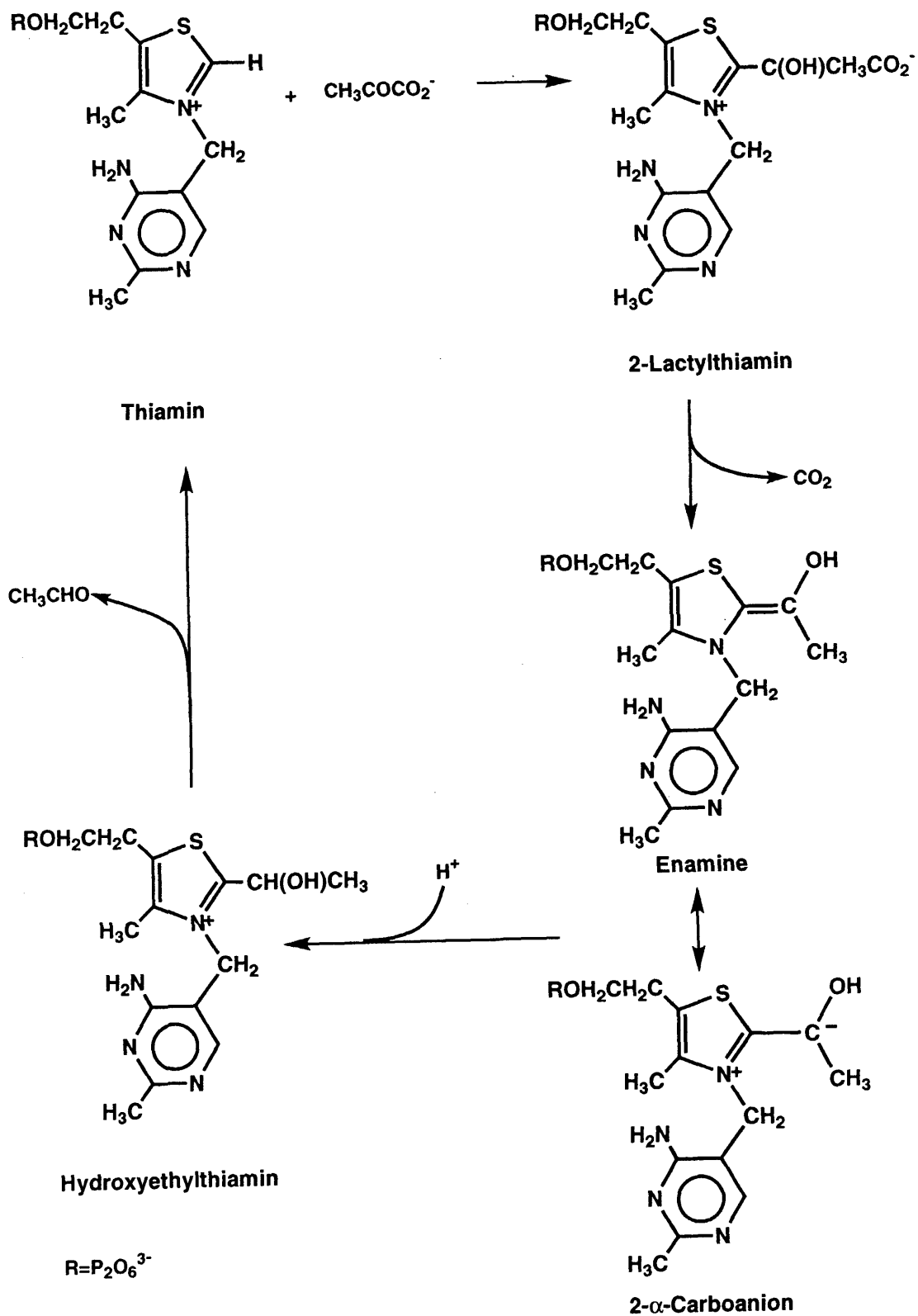
# **Coenzyme Catalyses of Carboxylation and Decarboxylation**

## Decarboxylation of 2-Lactylthiazolium Cation

### 2.1 Introduction

Thiamin diphosphate (TDP) is a coenzyme participating in the enzymatic decarboxylation of pyruvate.<sup>1</sup> The reaction mechanism of the pyruvate decarboxylation has been proposed by Breslow, as shown in Scheme 2.1.<sup>2</sup> In this mechanism, lactyl-TDP (LTDP), an enamine (or  $2\alpha$ -carboanion) species, and hydroxyethyl-TDP (HETDP) are involved as key intermediates. So far, there have been reported several experimental results supporting this reaction mechanism. For instance, HETDP was isolated from yeast pyruvate decarboxylase.<sup>3</sup> In addition, Krampitz et al. succeeded the chemical synthesis of HETDP and reported that HETDP was converted to acetaldehyde and thiamin diphosphate by wheat germ pyruvate decarboxylase.<sup>4</sup> Also, LTDP and lactylthiamin (a model of LTDP) were chemically synthesized, and their reaction behaviors have been investigated.<sup>5,6</sup> In particular, experimental results of Lienhard et al.<sup>7</sup> are worthy of note, here; the decarboxylation of 2-lactyl-3,4-dimethylthiazolium cation proceeds with the high activation barrier of 31.2 kcal/mol in water but with the very small activation barrier in ethanol. From these results, they proposed that the desolvation action of the enzyme might be a major cause of catalysis in thiamine pyrophosphate-dependent enzymatic reactions.

Although several important results have been reported



Scheme 2.1

on LTDP and HETDP as described above, the enamine intermediate has not been chemically synthesized and its existence has not been directly confirmed yet, probably owing to its high reactivity. Recently, Kluger et al. provided experimental support to the enamine intermediate.<sup>8</sup> In addition, there has been reported Jordan's interesting result indicating that the enamine intermediate is indeed on the reaction pathway.<sup>9</sup> Molecular orbital calculations are also expected to offer several valid informations on the enamine species.

In this chapter, AM1 and ab initio MO/MP2 calculations are carried out on the decarboxylation reaction of 2-lactylthiazolium, a model of LTDP. Also, decarboxylation reactions of 2-lactyloxazolium and 2-lactylimidazolium are investigated, in an attempt to compare their reactivities with the 2-lactylthiazolium reactivity. It is our intention with this chapter to present (1) good understanding of the decarboxylation reaction of 2-lactylthiazolium, (2) theoretical evidence of the enamine intermediate, and (3) a clear comparison of the decarboxylation reactivity between thiazolium, oxazolium, and imidazolium cations.

## **2.2 Computational Details**

AM1 calculations were carried out with MOPAC program (version 3.0),<sup>10</sup> where AM1 standard parameters<sup>11</sup> were employed except for MNDO parameters used for the S atom.<sup>12</sup> Ab initio closed-shell Hartree-Fock (HF) and MP2 calculations were performed with Gaussian 82 and 86 programs.<sup>13</sup> MINI-1 basis set<sup>14a,b</sup> was used for geometry

optimization at the HF level. 6-31G<sup>15</sup> and MIDI-4<sup>14a,c</sup> basis sets were employed for MP2 calculations.

In AM1 calculations, geometries of reactants, transition states, and products were optimized with Davidon-Fletcher-Powell method, where the azolium ring was assumed to be planar. This assumption seems reasonable because 2-lactylthiazolium is destabilized in energy by the out-of-plane distortion of its N-H bond. Geometry changes caused by the decarboxylation were investigated, taking the C<sup>2 $\alpha$</sup> -CO<sub>2</sub> distance as a reaction coordinate (see Figure 2.1 for C<sup>2</sup>, C<sup>2 $\alpha$</sup> , etc.).

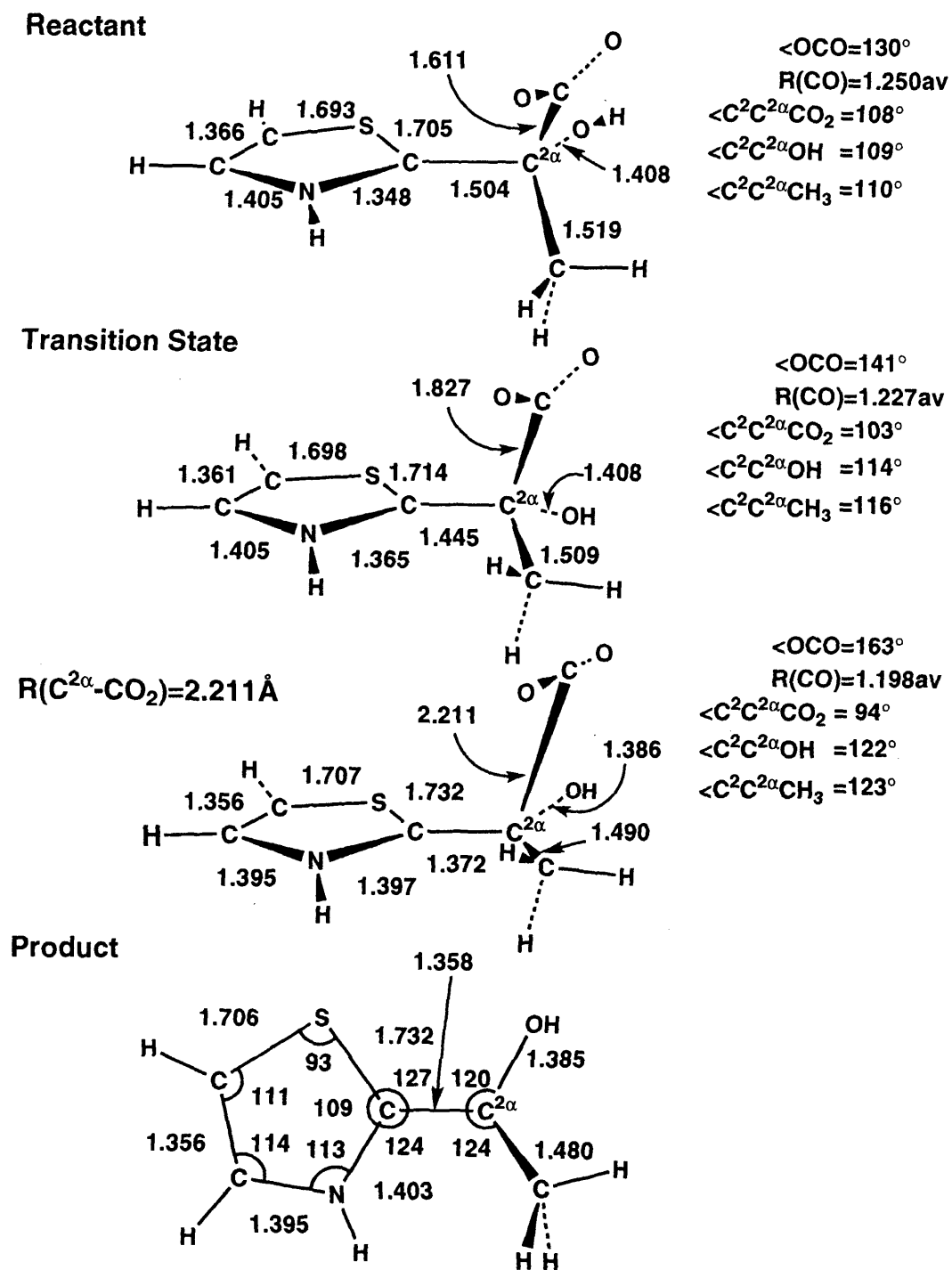
In ab initio MO calculations, geometries were optimized with the energy gradient method at the HF level, where the geometry of the thiazolium ring was taken to be the same as it in the AM1-optimized structure of 2-lactylthiazolium.<sup>17a,c</sup> This assumption is reasonable when the early stage of the decarboxylation is investigated, because AM1 calculations showed that geometry changes of the thiazolium ring were very small upon going to the TS from 2-lactylthiazolium. MP2 calculations were performed with all the core orbitals excluded from the active space.

## **2.3 Results and Discussion**

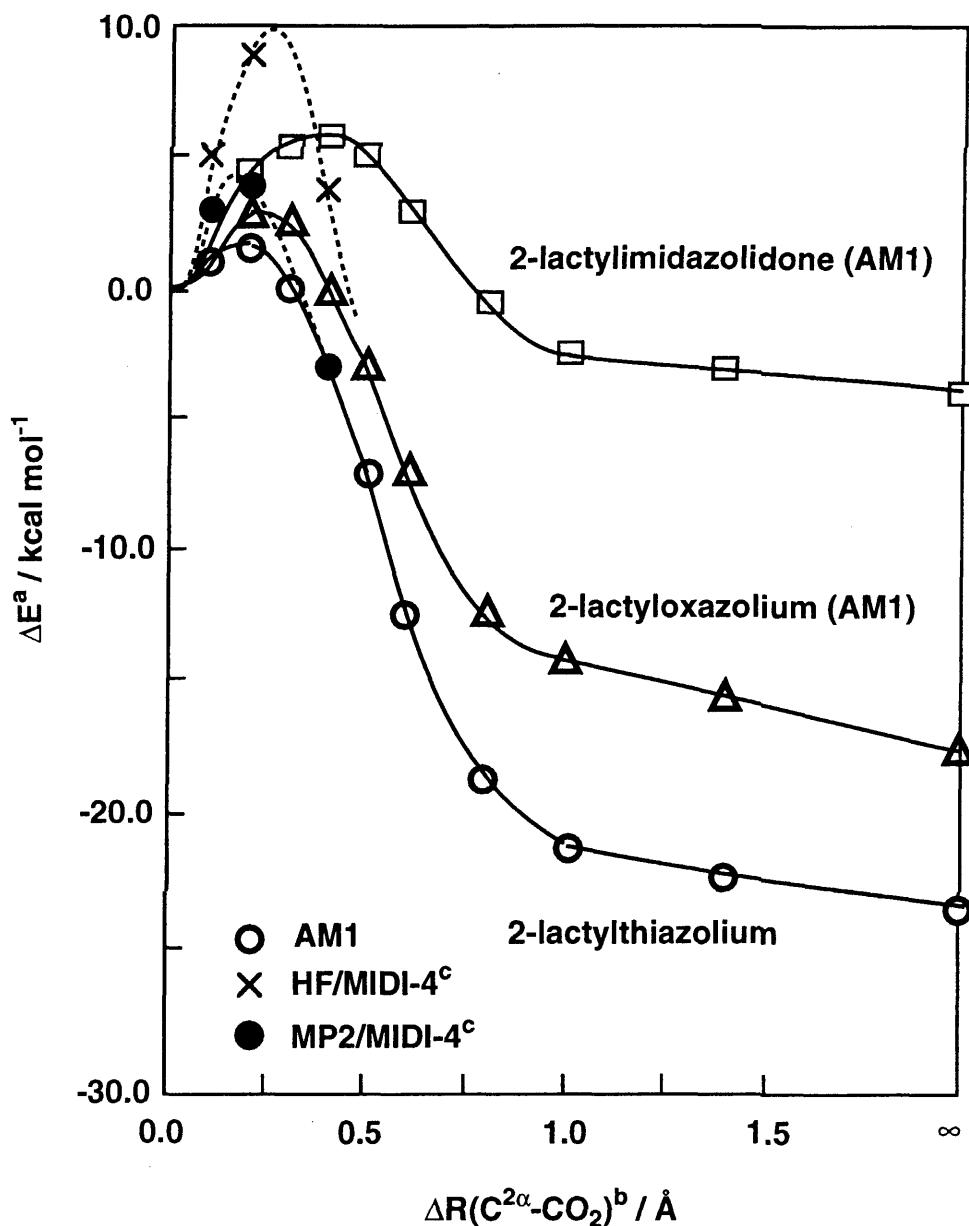
### **2-3-1 Decarboxylation Reaction of 2-Lactylthiazolium**

The geometry of 2-lactylthiazolium (**1**) optimized with the AM1 method is shown in Figure 2.1. This optimized geometry agrees well with the experimental structure of phosphalactylthiamin (methyl 2-hydroxy-2-(2-thiamin)ethylphosphonate).<sup>17b</sup> The energy change caused by





**Figure 2.1** Geometry changes caused by decarboxylation of 2-lactylthiazolium (bond distance in Å and bond angle in degree).



**Figure 2.2** Energy changes caused by decarboxylations of 2-lactylthiazolium, 2-lactyloxazolium, and 2-lactylimidazolium.

a)  $\Delta E$  represents total energy changes from 2-lactylthiazolium, 2-lactyloxazolium, and 2-lactylimidazolium. b)  $\Delta R(\text{C}^{2\alpha}\text{-CO}_2)$  means lengthening of the  $\text{C}^{2\alpha}\text{-CO}_2$  distance from 2-lactyl-azoliums. c) Results of HF/6-31G and MP2/6-31G are very close to results of HF/MIDI-4 and MP2/MIDI-4, respectively.

the decarboxylation of 2-lactylthiazolium is given in Figure 2.2 as a function of the  $C^{2\alpha}$ -CO<sub>2</sub> distance. AM1 calculations indicate that the  $C^{2\alpha}$ -CO<sub>2</sub> distance lengthens at the transition state (TS) by ca. 0.2 Å, like ab Initio MO/MP2 calculations. Thus, we can consider that the AM1 method presents reliable results on this decarboxylation reaction. Geometries of the TS (**2**) and the product (**4**) of this decarboxylation are also shown in Figure 1.1. Going to **4** from **1**, the C<sup>2</sup>-N distance is getting longer, the C<sup>2</sup>-C<sup>2α</sup> distance is getting shorter, and the OCO, C<sup>2</sup>C<sup>2α</sup>CH<sub>3</sub> and C<sup>2</sup>C<sup>2α</sup>OH angles gradually open. These results mean that the C<sup>2</sup>-C<sup>2α</sup> single bond is changing to the double bond, the C<sup>2</sup>=N double bond to the single bond, and the CH<sub>3</sub> and OH groups are going into the plane of the C<sup>2</sup>=C<sup>2α</sup> double bond. Lengthening the  $C^{2\alpha}$ -CO<sub>2</sub> distance to 2.211 Å (i.e., going to the late stage of the reaction), the C<sup>2</sup>-C<sup>2α</sup> distance shortens to 1.363 Å and the C<sup>2</sup>-N distance lengthens to 1.397 Å, as shown by **3** in Figure 1.1. These distances of the C<sup>2</sup>-C<sup>2α</sup> and C<sup>2</sup>-N bonds are similar in magnitude to those of the C=C double and C-N single bonds, respectively, indicating that **3** is characteristic of the enamine compound. Also, the product (**4**) apparently takes the enamine structure (Figure 1.1). Thus, these results provide us with the theoretical evidence that the enamine intermediate is indeed on the reaction pathway.

AM1 calculations show that the activation barrier of this decarboxylation is considerably small ( $E_a = 1.5$  kcal/mol). Although somewhat large activation barriers, 8.9 and 9.0 kcal/mol, are evaluated by HF/MIDI-4 and HF/6-31G

**Table 2.1** Activation Barrier ( $E_a$ ) and Exothermicity ( $E_{exo}$ ) of Decarboxylations of 2-Lactylazoliums. (kcal/mol)

	Method	$R_{C2\alpha-CO2}$	$E_a$	$E_{exo}$
2-lactylthiazolium				
	AM1	0.22	1.5	23.8
	HF/MIDI-4	0.25	8.9	- <sup>b</sup>
	HF/6-31G	0.25	9.0	- <sup>b</sup>
	MP2/MIDI-4	0.17	3.9	- <sup>b</sup>
	MP2/6-31G	0.18	4.4	- <sup>b</sup>
2-lactylthiazolium <sup>c</sup> with 2 H <sub>2</sub> O				
	AM1	0.30	5.6	14.7
2-lactylthiazolium <sup>d</sup> with 3 H <sub>2</sub> O				
	AM1	0.32	19.0	-2.1 <sup>e</sup>
2-lactyloxazolium				
	AM1	0.18	2.8	18.1
2-lactylimidazolium				
	AM1	0.42	6.4	3.9

a) Bond lengthening at TS. b) Not calculated.<sup>18</sup> c) 2 molecules of water were added to the reaction system.<sup>19a</sup> d) 3 molecules of water were added to the reaction system.<sup>19b</sup> e) endothermic

calculations respectively, inclusion of electron correlation by the MP2 method substantially decreases the activation barrier to 3.9 (MP2/MIDI-4) and 4.4 kcal/mol (MP2/6-31G), as shown in Table 2.1 Corresponding to this small activation barrier, the exothermicity ( $E_{exo}$ ) calculated for this

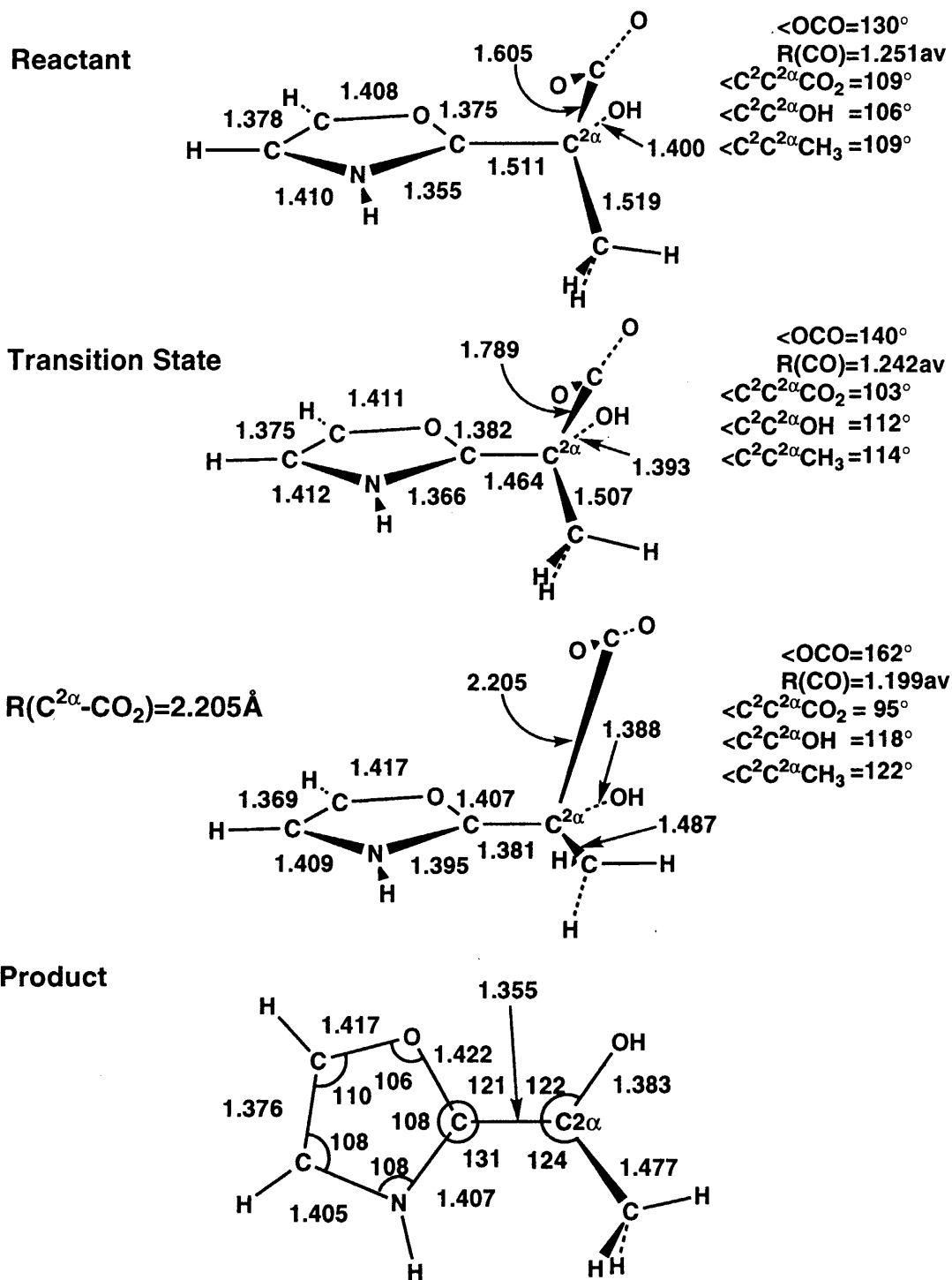
decarboxylation is extremely large;  $E_{\text{exo}} = 23.8$  kcal/mol (AM1 calculation).<sup>18</sup> All these results suggest that the decarboxylation of 2-lactylthiazolium proceeds very easily in non-polar solvents. In such a polar solvent as water, the situation would change. 2-Lactylthiazolium is considered as a zwitter-ion because the CO<sub>2</sub> part is negatively charged and the thiamin ring is positively charged. On the other hand, products (enamine and CO<sub>2</sub>) are neutral. Thus, a polar solvent stabilizes 2-lactylthiazolium more than the products, which would increase the activation barrier and decrease the exothermicity. In order to examine how water molecules influence this decarboxylation, we carried out AM1 calculations on this decarboxylation reaction in the presence of several water molecules. First, let us investigate the case where two water molecules interact with the CO<sub>2</sub> part of 2-lactylthiazolium. Positions of water molecules are roughly optimized.<sup>19a</sup> These two water molecules increase the activation barrier to 5.6 kcal/mol and decrease the exothermicity to 14.7 kcal/mol. Then, let us investigate the case where one additional water molecule is placed so as to interact with the N atom of the thiazolium ring. Again, the position of this water molecule is roughly optimized,<sup>19b</sup> whereas the positions of the other two water molecules are not re-optimized. This new water molecule further increases the activation barrier to 19.0 kcal/mol and significantly decreases the exothermicity to -2.1 kcal/mol (i.e., the reaction becomes endothermic). These results are consistent with Lienhard's experiment that

the decarboxylation reaction of a lactylthiazolium derivative, 2-(1-carboxy-1-hydroxyethyl)-3,4-dimethylthiazolium chloride, proceeds very rapidly in ethanol but very slowly in water.<sup>7</sup> In other words, the desolvation of the reaction system seems one of the important roles of thiamin diphosphate.

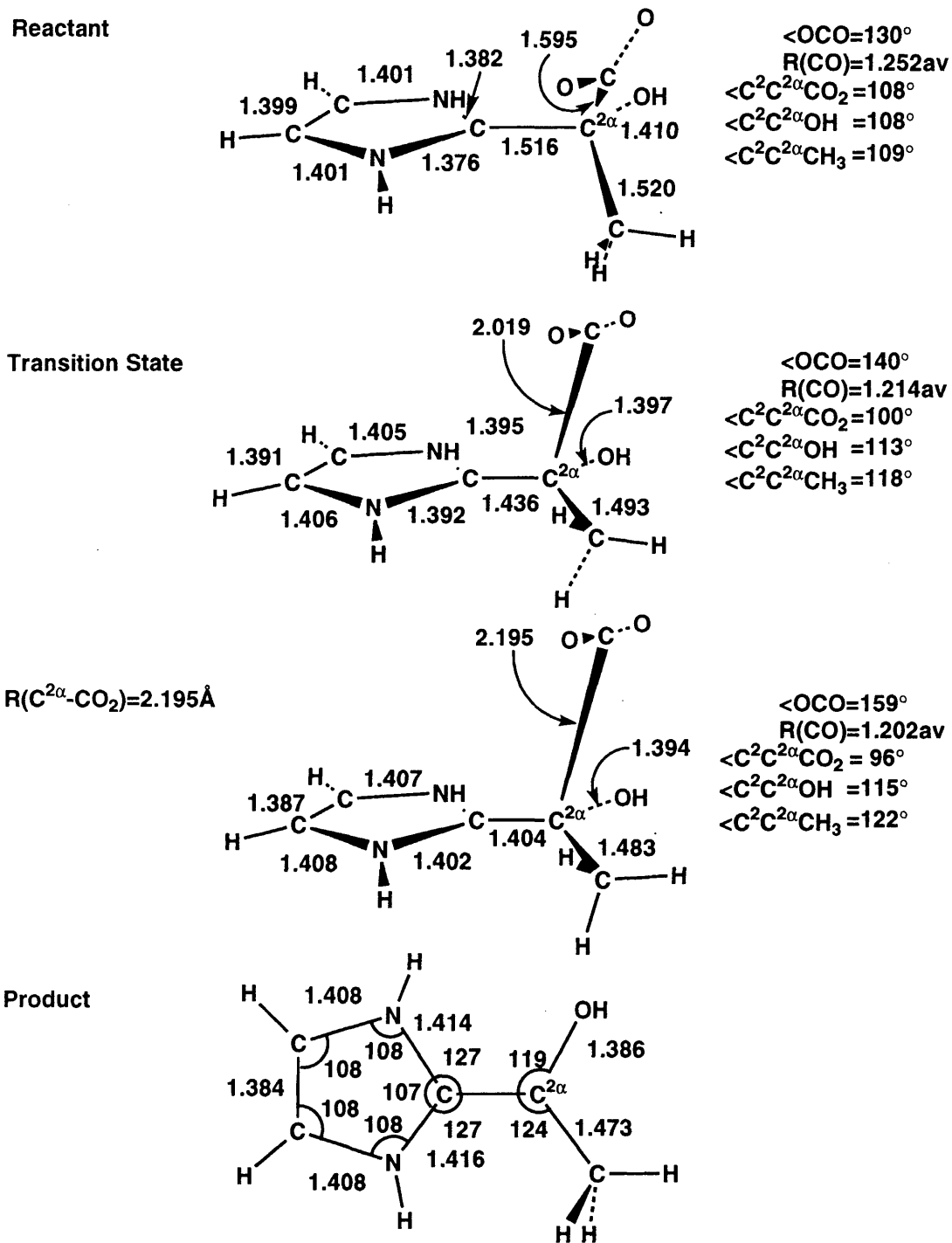
### **2-3-2 Decarboxylation Reactions of 2-Lactyloxazolium and 2-Lactylimidazolium**

These decarboxylation reactions are investigated with the AM1 method, where the  $C^{2\alpha}$ -CO<sub>2</sub> distance is taken as a reaction coordinate like in the decarboxylation of 2-lactylthiazolium. Geometry changes caused by these decarboxylations are given in Figures 2.3 and 2.4. As these decarboxylations proceed (i.e., as the  $C^{2\alpha}$ -CO<sub>2</sub> distance lengthens), the C<sup>2</sup>-N distance is getting longer, the C<sup>2</sup>-C<sup>2 $\alpha$</sup>  distance is getting shorter, and the OCO, C<sup>2</sup>C<sup>2 $\alpha$</sup> CH<sub>3</sub> and C<sup>2</sup>C<sup>2 $\alpha$</sup> OH angles gradually open, like in the decarboxylation of 2-lactylthiazolium. Consequently, 2-lactyloxazolium and 2-lactylimidazolium change to **7** (Figure 2.3) and **11** (Figure 2.4) respectively, at the late stage of the reaction. Both **7** and **11** are characteristic of enamine compounds. Furthermore, products (**8** and **12**) of these reactions take the enamine structure like the product **4** of the 2-lactylthiazolium decarboxylation.

The activation barrier calculated with the AM1 method increases in the order 2-lactylthiazolium (1.5 kcal/mol) < 2-lactyloxazolium (2.8 kcal/mol) < 2-lactylimidazolium (6.4 kcal/mol), and the exothermicity decreases in the order



**Figure 2.3** Geometry changes caused by decarboxylation of 2-lactyloxazolium (bond distance in Å and bond angle in degree).



**Figure 2.4** Geometry changes caused by decarboxylation of 2-lactylimidazolium (bond distance in Å and bond angle in degree).



2-lactylthiazolium (23.8 kcal/mol) > 2-lactyloxazolium (18.1 kcal/mol) > 2-lactylimidazolium (3.9 kcal/mol). Thus, the decarboxylation of 2-lactylthiazolium proceeds the most easily but that of 2-lactylimidazolium proceeds with the most difficulty in these three decarboxylations.

It is interesting to compare geometries of the TS in these decarboxylations. As described above, the C<sup>2</sup>-C<sup>2α</sup> bond changes to its double bond but the C<sup>2</sup>-N bond changes to its single bond upon going to the product from the reactant. To indicate how much the C<sup>2</sup>-C<sup>2α</sup> single bond changes to its double bond at the TS, a factor f<sub>1</sub> is defined as follows;  $f_1 = \frac{R(C-C)_P - R(C-C)_{TS}}{R(C-C)_R - R(C=C)_P}$ , where such subscripts as, P, R, and TS, represent product, reactant, and transition state, respectively. Apparently, f<sub>1</sub> is 0 % for the C<sup>2</sup>-C<sup>2α</sup> single bond and 100 % for the C<sup>2</sup>=C<sup>2α</sup> double bond. Also, a factor, f<sub>2</sub>, is defined on the C<sup>2</sup>-N bond, to illustrate how much the C<sup>2</sup>=N double bond changes to its single bond at the TS;  $f_2 = \frac{R(C=N)_R - R(C-N)_{TS}}{R(C=N)_R - R(C-N)_P}$ . Apparently, f<sub>2</sub> is 0 % for the C<sup>2</sup>=N double bond and 100 % for the C<sup>2</sup>-N single bond. These factors, f<sub>1</sub> and f<sub>2</sub>, are considered as measures indicating the character of TS. As listed in Table 2.2, these f<sub>1</sub> and f<sub>2</sub> exhibit interesting differences between 2-lactylimidazolium and the other two; f<sub>1</sub>=38 % and f<sub>2</sub>=31 % in the decarboxylation of 2-lactylthiazolium, f<sub>1</sub>=30 % and f<sub>2</sub>=21 % in the decarboxylation of 2-lactyloxazolium, f<sub>1</sub>=58 % and f<sub>2</sub>=40 % in the decarboxylation of 2-lactylimidazolium. These results suggest that the decarboxylation of 2-lactylimidazolium reaches TS more late than the other decarboxylations.

**Table 2.2** Measures of C<sup>2</sup>-C<sup>2 $\alpha$</sup>  bond lengthening (f<sub>1</sub>) and C<sup>2</sup>-N<sup>3</sup> bond shortening (f<sub>2</sub>), and Pauling's bond order (n) of the C<sup>2</sup>-C<sup>2 $\alpha$</sup>  and C<sup>2</sup>-N<sup>3</sup> bonds at the transition state of the decarboxylation of 2-lactylazoliums.

	Measure of change in bond distance		Pauling's bond order	
	f <sub>1</sub> <sup>a</sup>	f <sub>2</sub> <sup>b</sup>	n <sub>C2-C2<math>\alpha</math></sub> <sup>c</sup>	n <sub>C2-N3</sub> <sup>c</sup>
2-lactylthiazolium	38 %	31 %	1.323	1.615
2-lactyloxazolium	30 %	21 %	1.232	1.727
2-lactylimidazolium	58 %	40 %	1.466	1.516

a) f<sub>1</sub> is the measure indicating how much the C<sup>2</sup>-C<sup>2 $\alpha$</sup>  bond changes to the double bond from the single bond (see text).

b) f<sub>2</sub> is the measure indicating how much the C<sup>2</sup>-N bond changes to the single bond from the double bond (see text).

c) Pauling's bond order;  $n = \exp[(R_1 - R_n)/C]$ , where R<sub>1</sub> and R<sub>n</sub> are bond lengths for bonds of order unity and n, respectively. C is estimated so as that n=1 for the single bond and n=2 for the double bond.

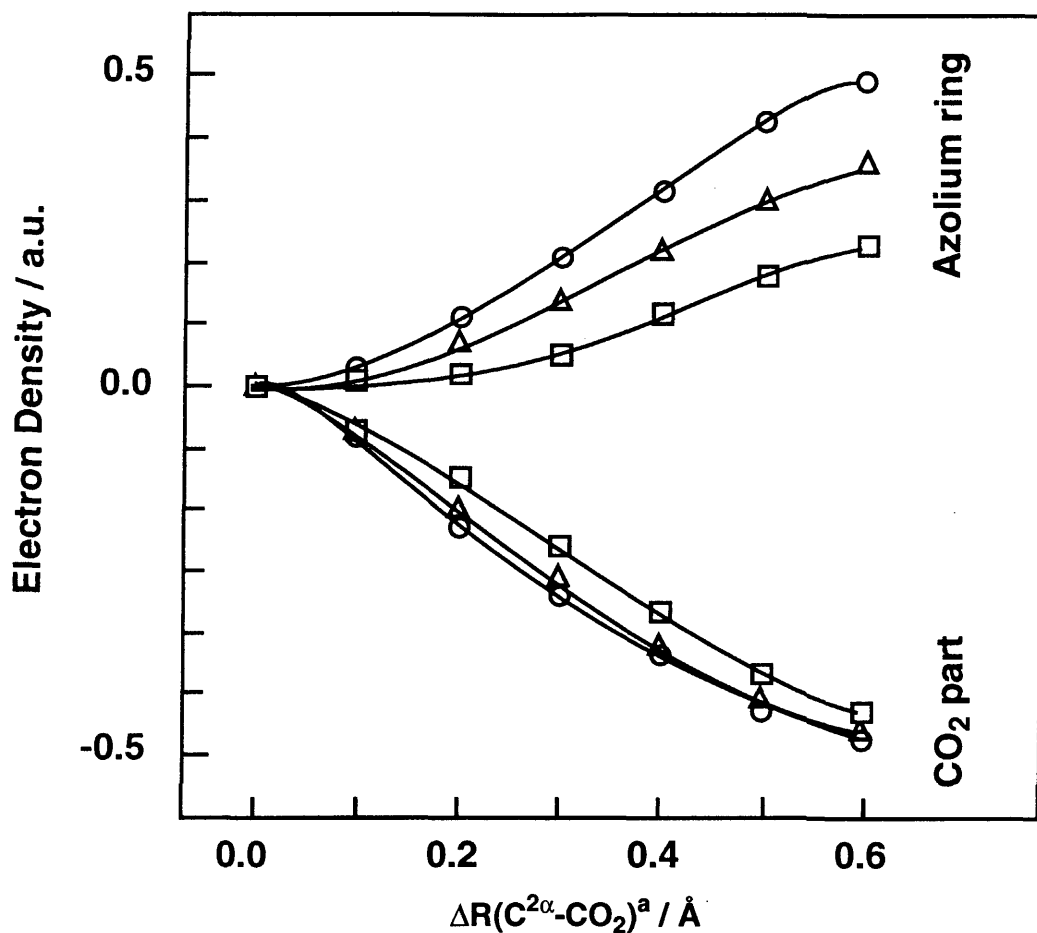
Pauling's bond order is also useful in discussing the character of TS. As shown in Table 2.2, the decarboxylation of 2-lactylimidazolium exhibits the greater value of the C<sup>2</sup>-C<sup>2 $\alpha$</sup>  bond order and the smaller value of the C<sup>2</sup>-N one at the TS than the other decarboxylations, indicating that in the 2-lactylimidazolium decarboxylation, the C<sup>2</sup>-C<sup>2 $\alpha$</sup>  single bond changes to its double bond and the C<sup>2</sup>=N double bond changes to its single bond at the TS, to a greater extent, than in the other decarboxylations. These results again

suggest that the decarboxylation of 2-lactylimidazolium reaches TS more late than the others.

### **2-3-3 Electron Redistribution in These Decarboxylations and Factors Determining the Reactivity of Azolium**

As the decarboxylation proceeds, the electron density of the CO<sub>2</sub> part decreases but that of the azolium ring increases, as clearly shown in Figure 2.5. The greatest change is caused by the decarboxylation of 2-lactylthiazolium. This means that the thiazolium ring is the most electron-withdrawing (i.e. the least electron-donating) in these three azoliums.

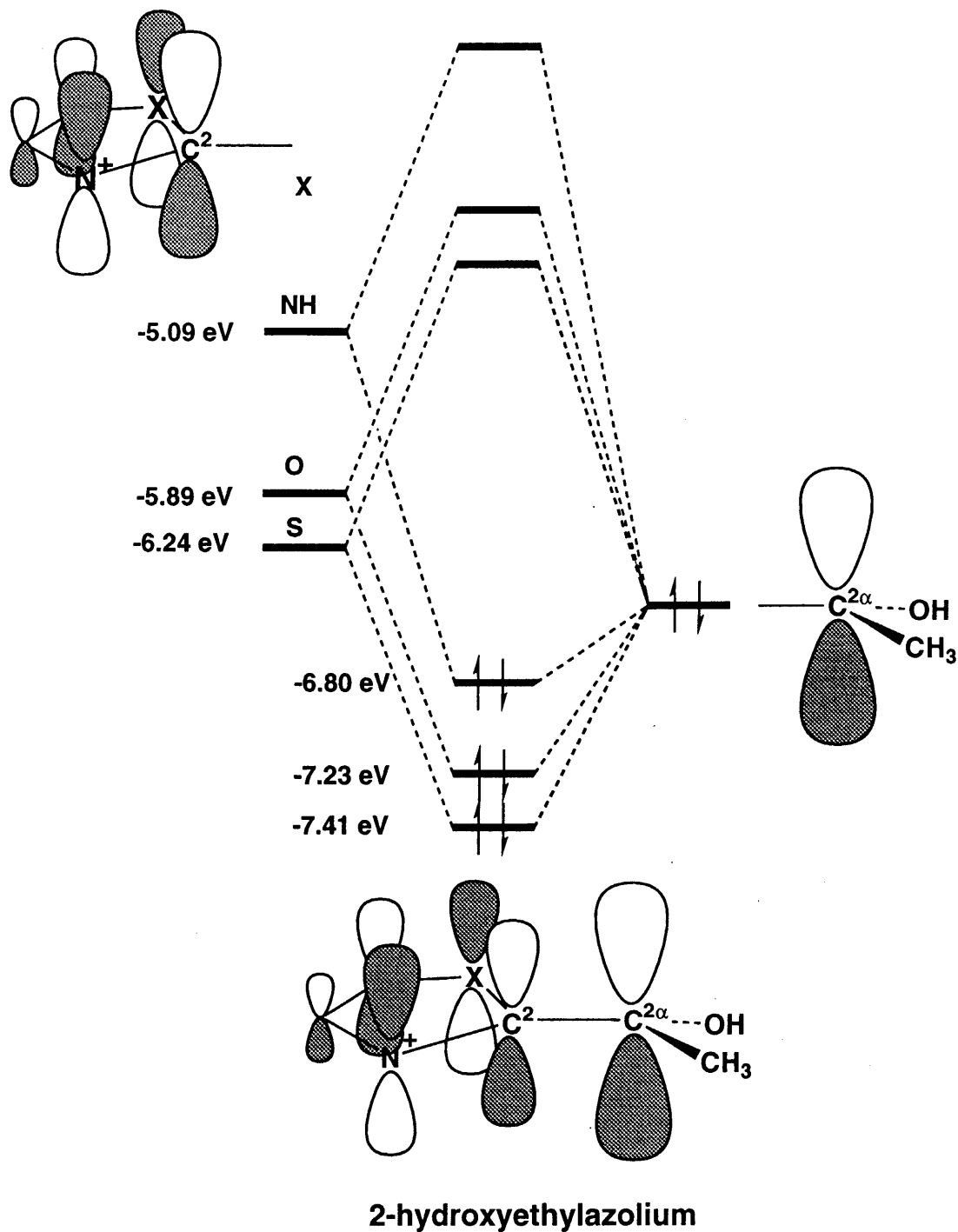
It is worthwhile investigating whether or not the decarboxylation reactivity is related to the electron-withdrawing character of the azolium ring. The more the azolium ring is electron-withdrawing, the more its  $\pi^*$  orbital lies low in energy. Thus, let us inspect the relation between the  $\pi^*$  orbital of the azolium ring and the decarboxylation reactivity of 2-lactylazolium. Since a neutral CO<sub>2</sub> molecule eliminates from 2-lactylazolium, 2-lactylazolium is considered to consist of CO<sub>2</sub> and such a remaining fragment as 2-hydroxyethylthiazolium (**10**), 2-hydroxyethylloxazolium (**11**), and 2-hydroxyethylimidazolium (**12**). These fragments, **10**, **11**, and **12**, are calculated with the AM1 method, where their geometries are taken to be the same as in the TS. Here, we should notice HOMO of 2-hydroxyethylazolium because the charge transfer from Lewis base to CO<sub>2</sub> is considered important to the CO<sub>2</sub> binding with



**Figure 2.5** Changes in electron density of the CO<sub>2</sub> part and azolium-ring caused by decarboxylations of 2-lactylthiazolium, 2-lactyloxazolium, and 2-lactylimidazolium.

a)  $\Delta R(C^{2\alpha}-CO_2)$  means lengthening of the C<sup>2 $\alpha$</sup> -CO<sub>2</sub> distance caused by the decarboxylation from 2-lactylazoliums.

the base.<sup>20</sup> As schematically shown in Figure 2.6, their HOMO mainly consists of the C<sup>2 $\alpha$</sup> p <sub>$\pi$</sub>  orbital into which the  $\pi^*$  orbital of the azolium ring mixes in a bonding way. Because the  $\pi^*$  orbital of the azolium ring rises in energy in the order thiazolium < oxazolium < imidazolium, the bonding



**Figure 2.6** Schematical representation of interaction between CO<sub>2</sub> and the C<sup>2α</sup> atom at Transition State.

mixing between the  $\pi^*$  orbital of the azolium ring and the  $C^{2\alpha}p_{\pi}$  orbital weakens in the order **10** > **11** > **12**, and therefore, HOMO of 2-hydroxyethylazolium rises in energy in the order **10** < **11** < **12**, as shown in Figure 2.6. Thus, the charge transfer from 2-hydroxyethylazolium to  $CO_2$  becomes strong in the order **10** < **11** < **12**, which leads to the weakest  $C^{2\alpha}-CO_2$  interaction in 2-lactylthiazolium and the strongest  $C^{2\alpha}-CO_2$  interaction in 2-lactylimidazolium. Consequently, the decarboxylation of 2-lactylthiazolium proceeds the most easily but that of 2-lactylimidazolium occurs with the most difficulty in these 2-lactylazoliums examined.

In summary, the decarboxylation reactivity of 2-lactylazolium can be related to the electron-withdrawing ability of the azolium ring, as follows: Since the  $\pi^*$  orbital of the thiazolium ring lies at the lowest energy level in these azoliums examined, thiazolium is the most electron-withdrawing, and at the same time, HOMO of 2-hydroxyethylthiazolium lies at the lowest energy level in these 2-hydroxyethylazoliums. In 2-lactylthiazolium, therefore, the  $CO_2$  binding with the  $C^{2\alpha}$  atom is the weakest in these 2-lactylazoliums, which results in the easiest decarboxylation of 2-lactylthiazolium. In other words, the greatest decarboxylation reactivity of 2-lactylthiazolium comes from the most electron-withdrawing ability of the thiazolium ring. These results are consistent with Breslow's proposal that the thiazolium ring serves as an electron sink for the decarboxylation process.<sup>2</sup>

Finally, let us discuss briefly the reason that the  $\pi^*$

orbital of the thiazolium ring lies at the lowest energy level in these azoliums. Compared to the O atom of oxazolium and the NH group of imidazolium, the S atom of thiazolium possesses highly polarizable and diffuse orbitals, which would stabilize the  $\pi^*$  orbital of the thiazolium ring in energy and would enhance the electron-withdrawing ability of the thiazolium ring.

#### 2.4 Conclusions

AM1 and ab initio MO/MP2 calculations are carried out on the decarboxylation reaction of 2-lactylthiazolium, a model of thiamin diphosphate. For the decarboxylation, the calculated activation barrier ( $E_a$ ) is very small and the calculated exothermicity ( $E_{exo}$ ) is considerably large;  $E_a = 1.5$  kcal/mol (AM1), 3.9 kcal/mol (MP2/MIDI-4), 4.4 kcal/mol (MP2/6-31G), and  $E_{exo} = 23.8$  kcal/mol (AM1). Two water molecules interacting with the  $CO_2$  part of 2-lactylthiazolium increase the activation barrier to 5.6 kcal/mol and decrease the exothermicity to 14.7 kcal/mol. An additional water molecule interacting with the thiazolium ring further increases the activation barrier to 19.0 kcal/mol and significantly decreases the exothermicity to -2.1 kcal/mol (i.e., the reaction is endothermic). This result agrees well with Lienhard's experiment.

As the decarboxylation proceeds, the  $C^2-C^{2\alpha}$  and  $C^2-N$  bonds are changing to the corresponding double and single bonds, respectively, and the product takes the typical enamine structure. This theoretical result, as well as Jordan's experiments, clearly indicates that the enamine is

indeed on the reaction pathway.

Decarboxylation reactions of 2-lactyloxazolium and 2-lactylimidazolium are investigated, to compare their reactivities with that of 2-lactylthiazolium. Products of their decarboxylations also take the enamine structure. In their decarboxylations, the activation barrier is slightly higher than that of 2-lactylthiazolium; 2.8 kcal/mol for 2-lactyloxazolium and 6.4 kcal/mol for 2-lactylimidazolium (AM1 calculation). The exothermicity is somewhat smaller in 2-lactyloxazolium (18.1 kcal/mol) and significantly smaller in 2-lactylimidazolium (3.9 kcal/mol) than in 2-lactylthiazolium. Thus, the decarboxylation reactivity decreases in the order thiazolium > oxazolium > imidazolium. This decreasing order is interpreted in terms of the  $\pi^*$  orbital of the azolium ring. Since the energy level of its  $\pi^*$  orbital lowers in the order imidazolium > oxazolium > thiazolium, HOMO of 2-hydroxyethylazolium lowers in the same order, which results in the most weak  $C^{2\alpha}$ -CO<sub>2</sub> binding of 2-lactylthiazolium. Accordingly, the decarboxylation of 2-lactylthiazolium proceeds the most easily. The  $\pi^*$  orbital of the azolium ring would be stabilized in energy by highly polarizable and diffuse orbitals of the S atom.



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- (17) (a) The optimized geometry of the thiazolium ring by the AM1 method agrees well with the experimental structure.<sup>17b</sup> The ab initio MO method overestimated bond lengths of the thiazolium ring by 0.06 Å ~ 0.2 Å, when either MINI-1, STO-3G, or 3-21G was employed. Only when a d-polarization function is added on the S atom, the optimized geometry agrees well with the experimental structure.<sup>17b</sup> (b) A. Turano, W. Furey, J. Pletcher, M. Sax, D. Pike, and R. Kluger, J. Am. Chem. Soc., **104**, 3089 (1982). (c) In ab initio MO calculations, the reaction coordinate, C<sup>2α</sup>-CO<sub>2</sub> distance, is increased with an increment of 0.2 Å, and the geometry was optimized at each C<sup>2α</sup>-CO<sub>2</sub> distance. The TS was located by least-square fitting of total energies.
- (18) Since the structure of the thiazolium's five-membered ring is considerably different between **1** and the enamine product, the thiazolium ring in the product should be re-optimized for calculation of the exothermicity. However, such optimization is much time-consuming in ab initio MO calculations, because

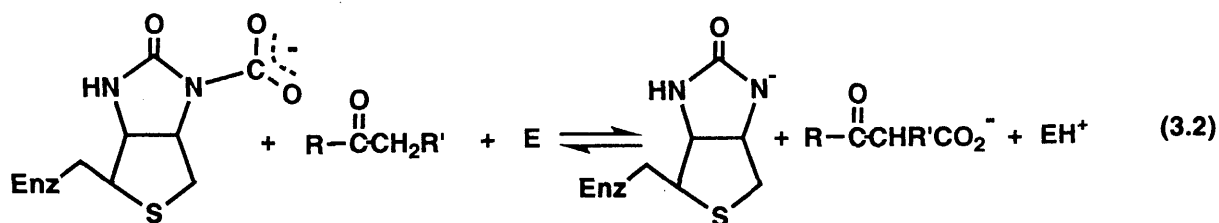
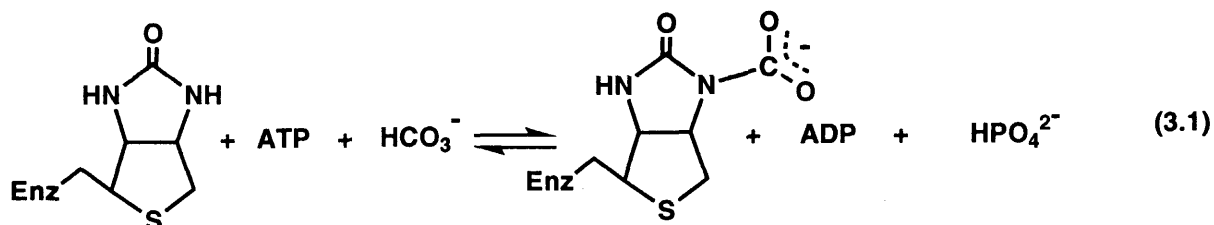
use of a d-polarization function is indispensable to obtain good geometry of the five-membered ring.<sup>17a</sup> Thus, the exothermicity was not calculated by the ab initio MO/MP2 method.

- (19) (a) Water molecules are placed in the CO<sub>2</sub> plane, where waters approach the O atom of CO<sub>2</sub> with the H atom in the lead. The approaching angle of H<sub>2</sub>O (<COH) and the distance between O of CO<sub>2</sub> and H of H<sub>2</sub>O are optimized.
- (b) A water molecule is placed above the thiazolium ring, perpendicularly to the ring, where the O atom of water molecule approaches the N atom of thiazolium. The N-O distance and the approaching angle of H<sub>2</sub>O are optimized.
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**Structure and Bonding Nature of  
Carboxyimidazolidone,  
a Model of Carboxybiotin.**

### 3.1 Introduction

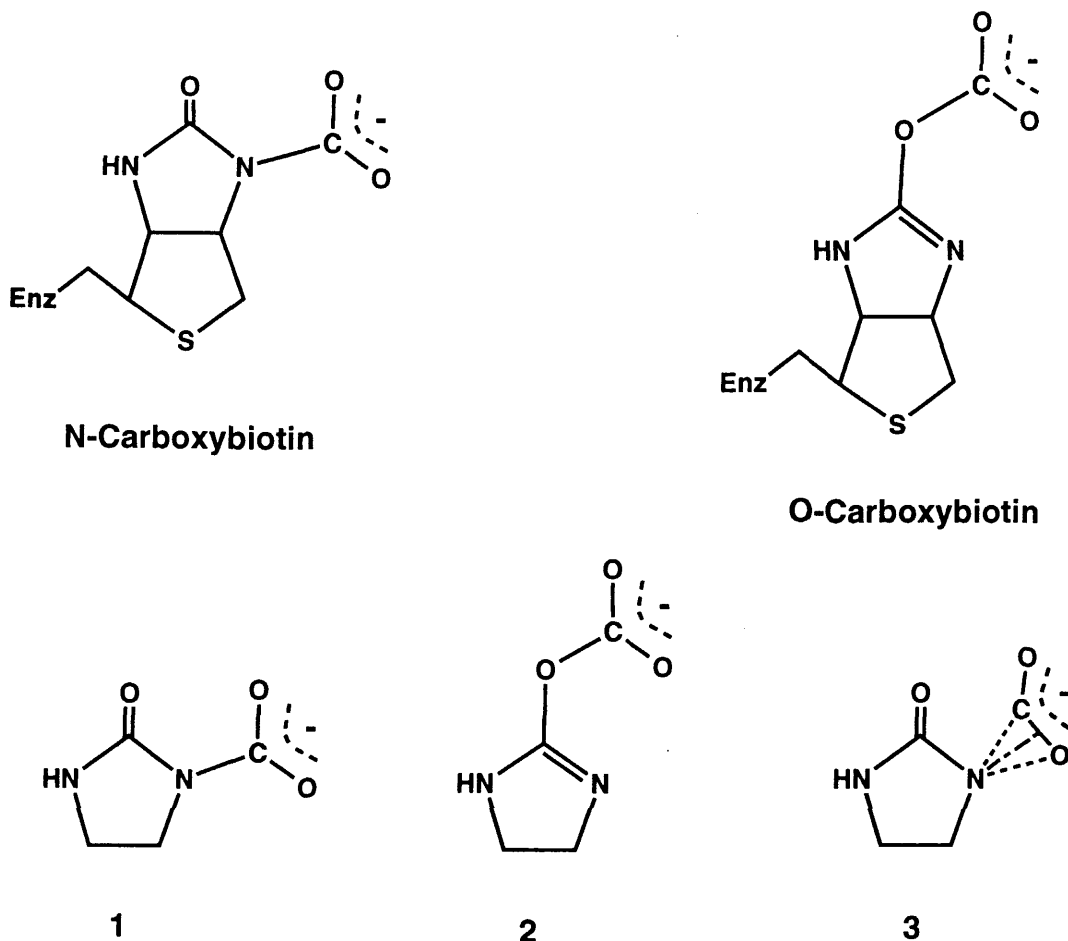
The reaction mechanism of the biotin-mediated CO<sub>2</sub> metabolism has been actively investigated as reviewed recently,<sup>1</sup> because biotin serves as a cofactor in a number of important enzymic carboxylation reactions of organic substrates.<sup>2-4</sup> For instance, the pioneering work of Lynen et al. clearly indicated that enzymic carboxyl-transfer reaction proceeds via a carboxybiotin intermediate.<sup>2</sup> The reaction mechanism accepted now is summarized as follows;<sup>1</sup> (1) N-carboxybiotin is formed from biotin, bicarbonate, and ATP (eq 3.1), accompanied with conversion of ATP to ADP



and inorganic phosphate,<sup>2,3</sup> and then (2) the carboxyl group transfers from N-carboxybiotin to an organic substrate with the deprotonation of substrate by either enzyme or biotin

itself (eq 3.2).<sup>4-6</sup> Although many elegant experimental works have been carried out to clarify the reaction mechanism,<sup>1</sup> there still remain several important issues to be examined. One of those issues is the reactivity of N-carboxybiotin. Because N-carboxybiotin is considered to be inherently unreactive,<sup>7</sup> it must be activated to perform the carboxyl-transfer reaction. Kluger et al.<sup>8</sup> proposed that the carboxyl group becomes reactive by the rotation around the N-CO<sub>2</sub> bond because such rotation would destroy the resonance preserved in the most stable planar conformation. The other proposal was presented by Perrin and Dwyer, in which the CO<sub>2</sub> group of carboxybiotin is considered to be activated by proton donor or cationic species.<sup>9</sup> Detailed knowledge on geometry, stability, bonding nature, and electron distribution of carboxybiotin would be helpful to discuss the reaction mechanism. Not only experimental works but also theoretical works are necessary to present such knowledge. However, only a few of theoretical works have been carried out to our knowledge,<sup>8,10</sup> in which rather simple compounds were adopted as a model of biotin.

In this chapter, we carried out ab initio MO/MP4, SD-CI, and coupled cluster with double substitution (CCD) calculations of N-carboxyimidazolidone **1**, O-carboxyimidazolidone **2**, and the  $\eta^2$ -side-on carboxyimidazolidone **3**, where imidazolidone was adopted here as a model of biotin (Scheme 3.1). Our purposes of this chapter are (1) to offer fundamental knowledge necessary for systematically theoretical investigation of biotin; for instance, reliability of model, basis set effects, and correlation effects on geometry and stability, (2) to present such



**Scheme 3.1**

detailed information of imidazolidone and carboxy-imidazolidone as geometry, bonding nature, electron distribution, and reactivity, (3) to make a clear comparison between N-carboxyimidazolidone and O-carboxyimidazolidone, because O-carboxybiotin was proposed previously<sup>11</sup> but any information has not been reported on it, and (4) to examine the stability of the  $\eta^2$ -side-on carboxyimidazolidone; this structure has not been discussed at all, whereas both  $\eta^1$ -C and  $\eta^2$ -side-on CO<sub>2</sub> adducts have been reported in transition-

metal complexes.<sup>12</sup>

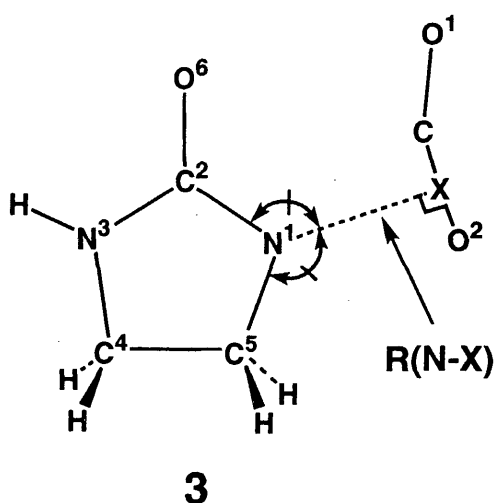
### 3.2 Computational Details

Ab initio closed-shell Hartree-Fock (HF), MP2 to MP4SDQ, SD-CI, and CCD calculations were carried out with Gaussian 86<sup>13a</sup> and 92<sup>13b</sup> programs. 3-21G,<sup>14</sup> 6-31G,<sup>15</sup> and 6-31+G<sup>16</sup> basis sets were used in these calculations, where d-polarization functions<sup>17</sup> were added to N and O of imidazolidone. In SD-CI calculations, the contribution of higher-order excited configurations were estimated, according to Davidson,<sup>18</sup> Davidson-Silver,<sup>19</sup> and Pople et al.<sup>20</sup> In CCD calculations, the contribution of single and triple substitutions was evaluated through forth-order with CCD wave functions.<sup>21</sup> In all the calculations at the correlated level, core orbitals were excluded from the active space.

Geometry optimization was performed with the energy gradient method at HF and MP2 levels, using 3-21G set. In the optimization, the five-membered ring of imidazolidone was assumed to be in the C<sub>s</sub> symmetry because the five-membered ring of methylbiotin has been experimentally reported to be planar.<sup>22</sup> Such important geometrical parameters as the N-CO<sub>2</sub> distance of N-carboxyimidazolidone **1**, the O-CO<sub>2</sub> distance of O-carboxyimidazolidone **2**, and the geometry of the CO<sub>2</sub> part were re-optimized at the MP2 level, using 3-21G set, where the geometry of imidazolidone was assumed to be the same as the HF-optimized structure. This assumption seems reasonable, as will be discussed below.

Full geometry optimization of  $\eta^2$ -side-on carboxyimidazolidone **3** led to **1**. Thus, the geometry of **3** was optimized at R(N-X) = 2.0, 2.2 and 2.4 Å under the





**Scheme 3.2**

constraint that the N-X line bisecting the  $C^2N^1C^5$  angle is perpendicular to the C=O bond, where X is the center of the C=O bond (see Scheme 3.2).

In order to investigate the interaction between  $CO_2$  and deprotonated imidazolidone, we carried out energy decomposition analysis proposed by Morokuma et al.<sup>23</sup> In this analysis, the interaction energy (INT) is defined as the stabilization energy of carboxyimidazolidone relative to imidazolidone<sup>-</sup> and  $CO_2$  taking their distorted structures in carboxyimidazolidone (eq 3.3), where deprotonated imidazolidone is abbreviated as imidazolidone<sup>-</sup> and negative charge of carboxyimidazolidone is not described here for brevity. The deformation energy (DEF) is defined as the destabilization energy which is necessary to distort  $CO_2$  and imidazolidone<sup>-</sup> from their equilibrium structures to their distorted structures taken in **1** and **2** (eq 3.4);

$$INT = E_t(\text{Imd-CO}_2) - E_t(\text{Imd})_{\text{dist}} - E_t(\text{CO}_2)_{\text{dist}}, \quad (3.3)$$

$$\text{DEF} = E_t(\text{Imd})_{\text{dist}} - E_t(\text{Imd})_{\text{eq}} + E_t(\text{CO}_2)_{\text{dist}} - E_t(\text{CO}_2)_{\text{eq}}, \quad (3.4)$$

where Imd means imidazolidone<sup>-</sup>, and subscripts of "eq" and "dist" represent the equilibrium structure and the distorted one respectively. BE is the sum of INT and DEF, which corresponds to the negative value of usual binding energy (eq 3.5). INT is further divided into several chemically meaningful terms at the HF level, as shown in eq 3.6.

$$\begin{aligned} \text{BE} &= \text{INT} + \text{DEF} \\ &= E_t(\text{Imd-CO}_2) - E_t(\text{Imd})_{\text{eq}} - E_t(\text{CO}_2)_{\text{eq}} \end{aligned} \quad (3.5)$$

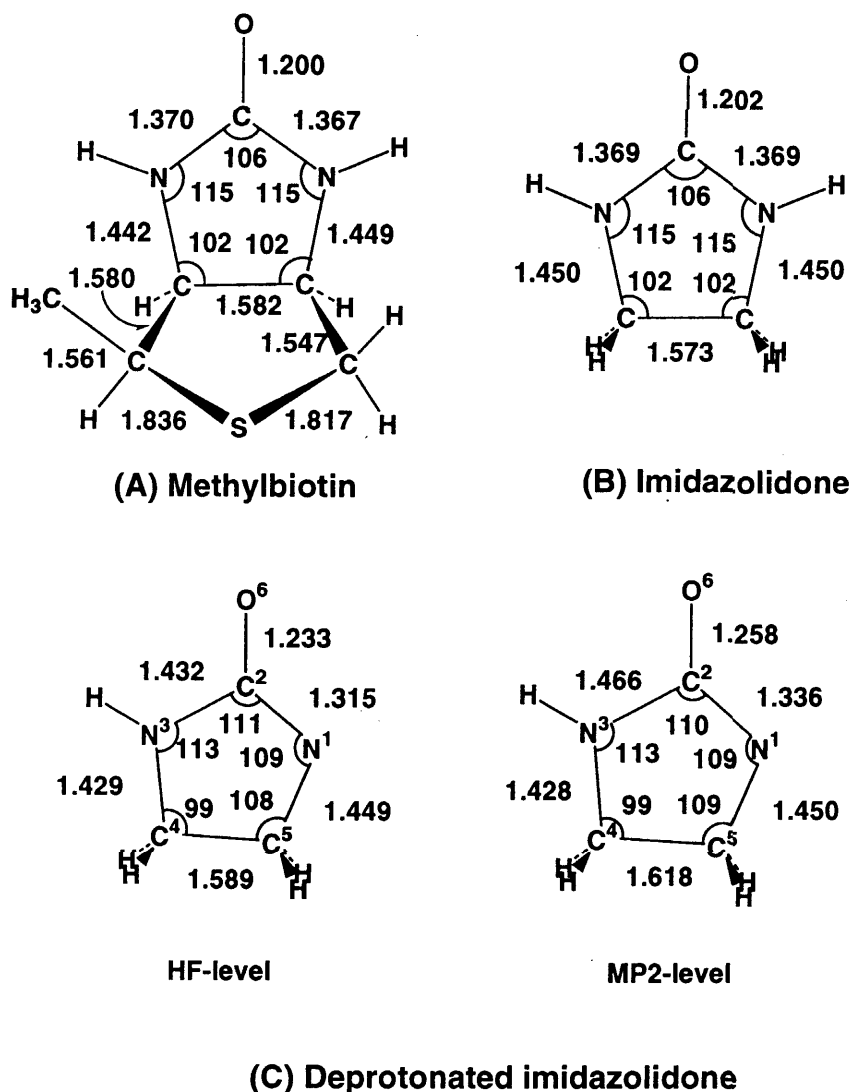
$$\begin{aligned} \text{INT} &= \text{ES} + \text{EX} + \text{CTPLXA}(\text{Imd} \rightarrow \text{CO}_2) \\ &\quad + \text{CTPLXB}(\text{Imd} \rightarrow \text{CO}_2) + \text{R} \end{aligned} \quad (3.6)$$

ES is the electrostatic (coulombic) interaction between imidazolidone<sup>-</sup> and CO<sub>2</sub>. EX is the exchange repulsion arising from Pauli exclusion principle between imidazolidone<sup>-</sup> and CO<sub>2</sub>. CTPLXA consists of the charge transfer (CT) from imidazolidone<sup>-</sup> to CO<sub>2</sub>, the polarization of CO<sub>2</sub>, and their coupling term. CTPLXB consists of the CT from CO<sub>2</sub> to imidazolidone<sup>-</sup>, the polarization of imidazolidone<sup>-</sup>, and their coupling term. R is a higher order coupling term. From the definition, a negative value means stabilization in energy for all these terms (vice versa). Although this analysis is based on the HF approximation, the bonding nature of **1** and **2** would be reliably compared by this analysis because the relative stabilities of **1** and **2** are essentially the same at both HF and correlated levels (vide infra). IMSPAC program was used for this analysis.<sup>24</sup>

### 3.3 Results and Discussion

#### 3-3-1 A Comparison of Biotin with Imidazolidone

First, we will examine whether imidazolidone can be



**Figure 3.1** Optimized geometries of methylbiotin, imidazolidone, and deprotonated imidazolidone

adopted as a reasonable model of biotin or not. As shown in Figure 3.1A, the HF-optimized geometry of methylbiotin agrees well with the experimental structure of d(+)-biotin.<sup>22</sup> Also, the HF-optimized geometry of imidazolidone (Figure 3.1B) is almost the same as the corresponding part of the HF-optimized methylbiotin. Furthermore, imidazolidone has

**Table 3.1** Atomic population and energy levels of  $\pi$  and  $\pi^*$  orbitals ( $\epsilon(\pi)$  and  $\epsilon(\pi^*)$ ) of methylbiotin and imidazolidone<sup>a</sup>

	methylbiotin	imidazolidone
Atomic Population		
N <sup>1</sup>	7.94	7.93
C <sup>2</sup>	4.60	4.61
C <sup>4</sup>	7.93	7.93
C <sup>5</sup>	5.59	6.15
O <sup>6</sup>	5.93	6.15
	8.79	8.79
Orbital Energy (eV)		
$e(\pi)$	-10.19	-10.18
$e(\pi^*)$	7.35	7.36

a) The 6-31G basis set was used, where a d-polarization function was added to N and O atoms of imidazolidone and methylbiotin.

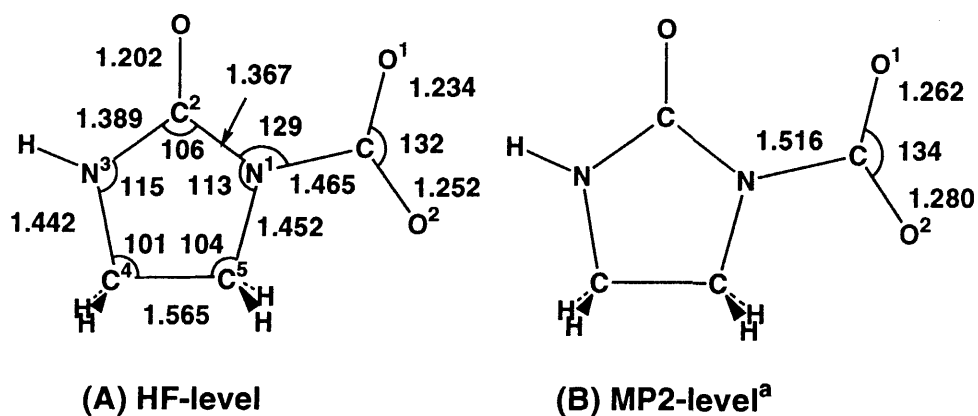
almost the same atomic populations and  $\pi$  and  $\pi^*$  orbitals at almost the same energy as those of methylbiotin, as compared in Table 3.1. From these results, imidazolidone seems to be a reasonable model of biotin.

In order to examine correlation effects on geometry, imidazolidone<sup>-</sup> was optimized at both HF and MP2 levels (Figure 3.1C). Introduction of electron correlation expectedly lengthens the C<sup>2</sup>-O<sup>6</sup>, N<sup>1</sup>-C<sup>2</sup>, and C<sup>4</sup>-C<sup>5</sup> bonds. The difference in geometry between MP2 and HF levels is not,

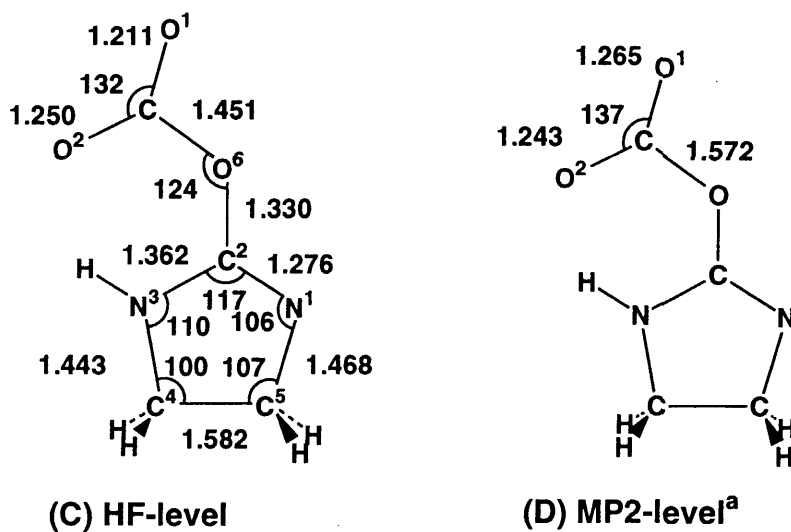
however, significant. For instance, discrepancies in bond length and bond angle are less than 0.05 Å and 4° respectively. Further, the energy levels of  $\pi$  and  $\pi^*$  orbitals do not change so much upon going to the MP2-optimized geometry from the HF-optimized one;  $\epsilon(\pi) = -4.26$  eV,  $\epsilon(\pi^*) = 12.60$  eV for the HF-optimized geometry, and  $\epsilon(\pi) = -4.31$  eV,  $\epsilon(\pi^*) = 12.42$  eV for the MP2-optimized geometry. Thus, the HF-optimized geometry of the imidazolidone ring seems reasonable for investigating the interaction between imidazolidone ring and CO<sub>2</sub>.

### **3-3-2 Geometries and the CO<sub>2</sub> Binding Energies (be) of N-Carboxyimidazolidone and O-Carboxyimidazolidone**

Optimized geometries of N-carboxyimidazolidone **1** and O-carboxyimidazolidone **2** are shown in Figure 3.2. Several interesting features are observed; (1) the CO<sub>2</sub> part significantly distorts in both **1** and **2**; the C=O distance is considerably longer than that of the free CO<sub>2</sub> molecule and the OCO angle is remarkably closed. The CO<sub>2</sub> part in **1** is more distorted than in **2**. (2) It is noted that the geometry of CO<sub>2</sub> in **1** and **2** resembles well the  $\eta^1$ -C coordinated CO<sub>2</sub> complexes of transition metal, such as M[Co<sup>I</sup>(R-salen)(CO<sub>2</sub>)],<sup>25</sup> Rh<sup>I</sup>Cl(diars)<sub>2</sub>(CO<sub>2</sub>),<sup>26</sup> and Ru(bpy)<sub>2</sub>(CO)( $\eta^1$ -CO<sub>2</sub>).<sup>27</sup> (3) In both **1** and **2**, the CO<sub>2</sub> part is on the molecular plane of imidazolidone. The perpendicular structure is less stable than the planar one by ca. 6 kcal/mol for **1** and 10 kcal/mol for **2** at the MP4(SDQ)/6-31G level. This energy difference is much smaller than that calculated previously for the simple model compound (H<sub>2</sub>NCONH-CO<sub>2</sub>).<sup>8</sup> There are several reasons for this



### N-Carboxyimidazolidone



### O-Carboxyimidazolidone

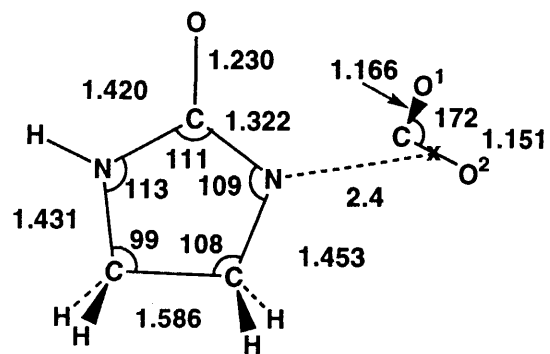
**Figure 3.2** Optimized geometries of N-carboxyimidazolidone and O-carboxyimidazolidone

a) The CO<sub>2</sub> parts in **1** and **2** were re-optimized at the MP2 level, using 3-21G set, where the geometry of imidazolidone was assumed to be the same as the HF-optimized structure.

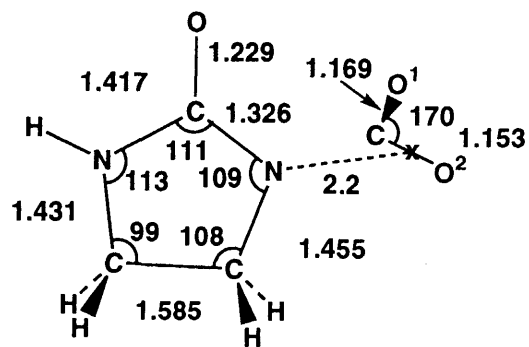
difference; the basis sets used are different, electron correlation is included in this thesis but was not in the previous work, and the more realistic model is adopted here than in the previous work.<sup>8</sup> Thus, the energy difference evaluated here seems more reliable. (4) Introduction of electron correlation lengthens the C=O distance like it in the free CO<sub>2</sub> molecule. Also, the N-CO<sub>2</sub> and O-CO<sub>2</sub> distances considerably lengthen upon introducing electron correlation, whereas the OCO angle little changes. This means that consideration of electron correlation is necessary for investigating model compounds of carboxybiotin.

In the  $\eta^2$ -side-on carboxyimidazolidone **3**, the C=O bond distances are optimized to be 1.16 and 1.17 Å, and the OCO angle is 167° at R(N-X) = 2.0 Å. This geometry of the CO<sub>2</sub> part is less distorted than in **1** and **2** (Figure 3), which suggests that the interaction between CO<sub>2</sub> and imidazolidone<sup>-</sup> is weak in this  $\eta^2$ -CO<sub>2</sub> adduct (vide infra).

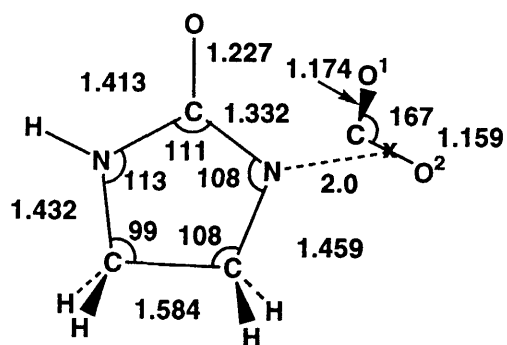
The binding energy of CO<sub>2</sub> in **1** and **2** was calculated with MP4SDQ/6-31G, MP4SDQ/6-31+G, SD-CI/6-31G and CCD/6-31G methods, where basis set super-position error was corrected with the counter-poise method.<sup>28</sup> Although the binding energy more or less fluctuates at MP2 and MP3 levels, almost the same binding energy was calculated at MP4, SD-CI, and CCD levels (see Table 3.2). Hereafter, we discuss relative stabilities of **1**, **2**, and **3**, based on MP4, SD-CI, and CCD calculations. Although use of the 6-31+G basis set including diffuse s and p functions on CO<sub>2</sub> yields somewhat smaller binding energy than the 6-31G basis set, the energy difference between **1** and **2** is little influenced by addition of such diffuse functions, and the CO<sub>2</sub> binding



3a



3b



3c

**Figure 3.3** Geometry of  $\eta^2$ -side-on carboxyimidazoidone<sup>a</sup>

a) Geometry optimization was performed under an assumption that the N-X line bisecting the CNC angle is perpendicular to the C=O bond, where X is the center of the C=O bond.



**Table 3.2** Correlation and basis set effects on the CO<sub>2</sub> binding energy (be) of N-carboxyimidazolidone **1** and O-carboxy-imidazolidone **2** (kcal/mol)

	N-carboxy- imidazolidone <b>1</b>	O-carboxy- imidazolidone <b>2</b>	
	6-31G <sup>a</sup>		
	be	be	Δbe
HF	40.1 (34.6) <sup>c</sup>	17.4 (11.5) <sup>c</sup>	22.6 (22.5) <sup>c</sup>
MP2	33.2 (27.2)	22.5 (16.5)	10.7 (10.6)
MP3	39.9 (33.8)	27.9 (21.9)	12.0 (11.9)
MP4DQ	38.0 (31.9)	25.7 (19.7)	12.3 (12.2)
MP4SDQ	37.4 (31.3)	21.9 (16.0)	11.6 (11.5)
SDCI	40.0 (33.9)	27.7 (21.9)	18.1 (18.0)
SDCI (D) <sup>d</sup>	39.9 (33.8)	27.2 (21.2)	12.0 (11.9)
SDCI (DS) <sup>e</sup>	38.8 (32.7)	27.2 (21.8)	11.1 (10.9)
SDCI (P) <sup>f</sup>	38.9 (32.9)	27.2 (21.2)	11.8 (11.7)
CCD	38.1 (32.0)	26.1 (20.1)	12.0 (11.9)

Continued to be the next page

	6-31+G <sup>a</sup>		
	be	be	$\Delta$ be
HF	34.7(29.3)	12.3( 8.3)	22.4(21.0)
MP2	24.8(19.4)	15.0(11.0)	9.8( 8.4)
MP3	32.6(27.2)	21.2(17.2)	11.4(10.0)
MP4DQ	30.5(25.1)	18.8(14.8)	11.7(10.3)
MP4SDQ	29.8(24.4)	18.7(14.7)	11.1( 9.7)

a) A d-polarization function was added to N and O atoms of imidazolidone. b) Dbe = difference in binding energy between **1** and **2** c) In parenthesis; basis set super position error was corrected with the counter-poise method.<sup>28</sup> d) D = Davidson's correction for higher order excitations.<sup>18</sup> e) DS = Davidson-Silver's correction for higher order excitations.<sup>19</sup> f) P = Pople's correction for higher order excitations.<sup>20</sup>

energy of **1** is much larger than that of **2** in all the calculations. It should be, therefore, clearly concluded that N-carboxyimidazolidone is more stable than O-carboxyimidazolidone. This conclusion is in accord with the experimental result that N-carboxybiotin was isolated in the biotin-dependent enzymic reactions.<sup>7c</sup>

The binding energy of N-carboxybiotin was experimentally estimated to be ca. 20 kcal/mol.<sup>29</sup> This experimental value is much smaller than the binding energy calculated here. However, the experimental value of the binding energy would correspond to the energy difference between N-carboxyimidazolidone and the imidazolidone<sup>-</sup>-H<sub>2</sub>O adduct, because the binding energy was estimated in water. The

**Table 3.3** Changes in total energy caused by  $\eta^2$ -side-on approach of CO<sub>2</sub> to deprotonated imidazolidone (kcal/mol)<sup>a</sup>

R(N-X) <sup>b</sup> (Å)	∞	2.4	2.4	2.4
HF	0.0	-4.3	3.9	20.6
MP2	0.0	-5.1	2.1	17.5
MP3	0.0	-5.7	1.6	17.0
MP4DQ	0.0	-5.3	2.2	17.7
MP4SDQ	0.0	-5.4	1.8	17.2

a) The 6-31G set was used, where a d-polarization function was added to N and O atoms of imidazolidone. Negative values mean stabilization. b) The N-X line which bisects the C<sup>2</sup>N<sup>1</sup>C<sup>5</sup> angle is perpendicular to the C=O bond of CO<sub>2</sub>, where X is the center of the C=O bond (see Scheme 2).

energy difference between N-carboxyimidazolidone and the imidazolidone<sup>-</sup>-H<sub>2</sub>O adduct is calculated to be ca. 18 kcal/mol at the MP4SDQ/6-31G level. This value is almost the same as the experimental value. From these results, we can expect that the binding energy of carboxybiotin is correctly estimated at the present computational level.

The binding energy (BE) of **3** is given in Table 3.3. Although slight stabilization in energy is observed at R(N-X) = 2.4 Å, the binding energy is too small, compared with those of **1** and **2**. Furthermore, this structure becomes unstable rapidly, as the R(N-X) distance shortens to a usual interacting distance. Also, geometry optimization of **3**

without any constraint led to **1**. All these results clearly indicate that the  $\eta^2$ -side-on carboxybiotin does not exist in biotin-dependent enzymic reactions.

### **3-3-3 Electron Distribution of N-Carboxy-imidazolidone, O-Carboxyimidazolidone, and $\eta^2$ -Side-on Carboxy-imidazolidone**

Several interesting changes in Mulliken populations are observed, as shown in Table 3.4: (1) The electron population of the CO<sub>2</sub> part increases upon formation of carboxy-imidazolidone **1**, **2**, and **3**, which indicates that the charge-transfer from imidazolidone<sup>-</sup> to CO<sub>2</sub> strongly occurs. (2) The electron population on CO<sub>2</sub> becomes greater in the order **3** < **2** < **1**, which corresponds to the increasing order of the CO<sub>2</sub> binding energy of CO<sub>2</sub>. (3) The O<sup>1</sup> and O<sup>2</sup> atomic populations expectedly increase but the C atomic population unexpectedly decreases in spite of the strong charge-transfer from imidazolidone<sup>-</sup> to CO<sub>2</sub>. All these features of the electron distribution are essentially the same as those reported in  $\eta^1$ -C coordinated CO<sub>2</sub> complexes of transition-metal.<sup>30</sup>

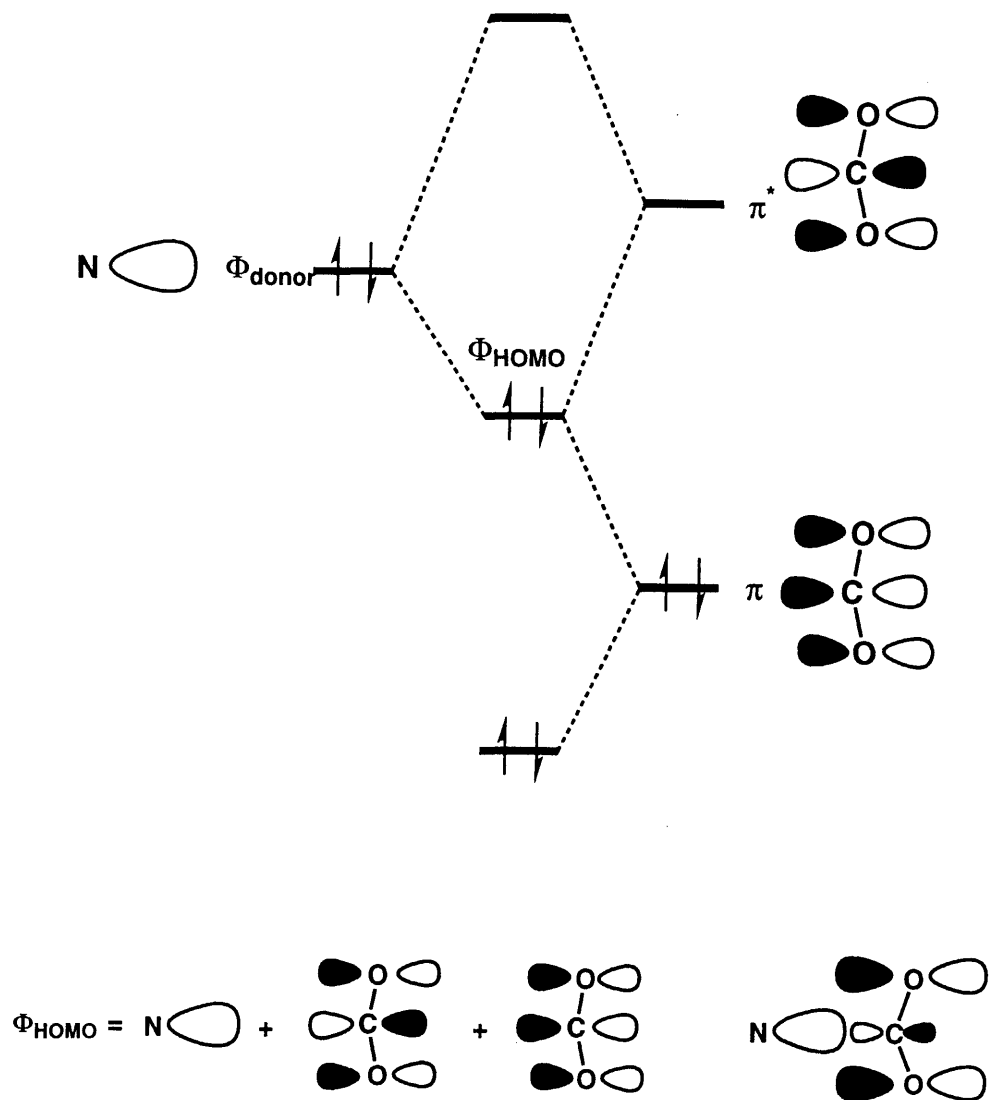
This electron distribution is interpreted in terms of the orbital mixing shown in Scheme 3.3. The HOMO of imidazolidone<sup>-</sup> little interacts with the  $\pi^*$  orbital of CO<sub>2</sub> because it is a  $\pi$ -type orbital. The donor orbital ( $\phi_{\text{donor}}$ ) of imidazolidone<sup>-</sup> is the next HOMO (Figure 3.4A), which is a lone pair type orbital expanding on both N and O atoms. The orbital mixing is mainly composed of the bonding overlap between the  $\phi_{\text{donor}}$  orbital and the CO<sub>2</sub>  $\pi^*$  orbital. The CO<sub>2</sub>  $\pi$  orbital mixes into the  $\phi_{\text{donor}}-\pi^*$  bonding overlap in an anti-bonding way with  $\phi_{\text{donor}}$  because the  $\pi$  orbital lies lower in

**Table 3.4** Electron redistribution by the formation of carboxyimidazolidone<sup>a</sup>

	N-carboxy- imidazolidone <b>1</b>	O-carboxy- imidazolidone <b>2</b>	h <sup>2</sup> -side-on-carboxy- imidazolidone <sup>b</sup> <b>3</b>
CO <sub>2</sub>	+0.47(+0.35) <sup>c</sup>	+0.40(+0.34) <sup>c</sup>	+0.11
C	-0.17(-0.27)	-0.15(-0.12)	-0.03
O <sup>1</sup>	+0.28(+0.28)	+0.31(+0.31)	+0.02
O <sup>2</sup>	+0.35(+0.34)	+0.25(+0.24)	+0.12
N <sup>1</sup>	+0.19(+0.25)	-0.07(-0.09)	-0.10
O <sup>6</sup>	-0.15(-0.12)	-0.03(-0.13)	-0.03

a) The positive values mean increase of electron population. The 6-31G set was used, where a d-polarization function was added to N and O atoms of imidazolidone. b) R(N-X) = 2.4 Å (see Scheme 2 for R(N-X)). c) In parenthesis; The 6-31+G set was used, where a d-polarization function was added to N and O atoms of imidazolidone.

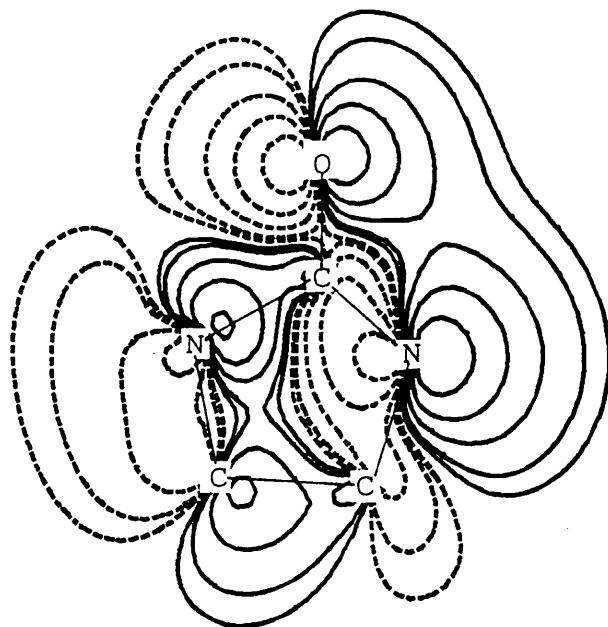
energy than  $\phi_{\text{donor}}$ . As clearly shown in Scheme 3.3, this orbital mixing reduces the contribution of the C  $p_{\pi}$  orbital but enlarges the contribution of the O  $p_{\pi}$  orbitals. The 26a<sub>1</sub> orbital of **1** and **2** arises from this orbital mixing (Figure 3.4B and 3.4C), in which the C  $p_{\pi}$  orbital almost disappears but the O  $p_{\pi}$  orbitals are considerably large, according to the above-described orbital mixing. As a result, the C atomic population decreases but the O<sup>1</sup> and O<sup>2</sup> atomic



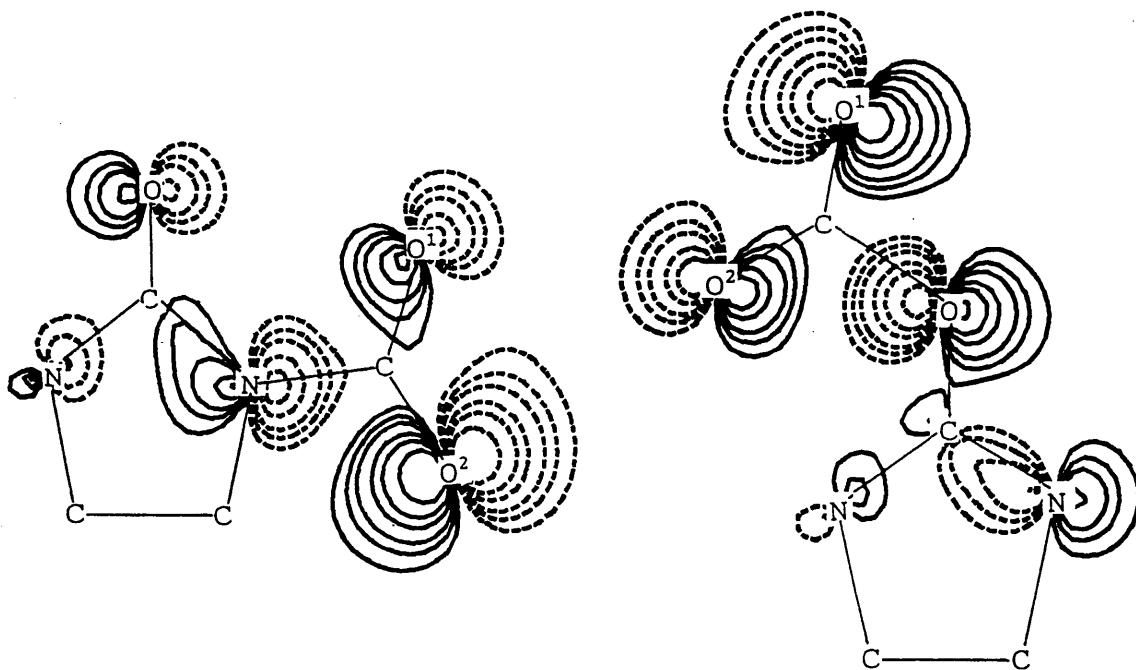
**Scheme 3.3**

populations increase upon formation of carboxyimidazolidone.

Finally, we will mention here the electron distribution of **3**. As described above, the CO<sub>2</sub> electron population of **3** increases least in three carboxy-imidazolidones, which is



(A) next HOMO ( $\Phi_{\text{donor}}$ )



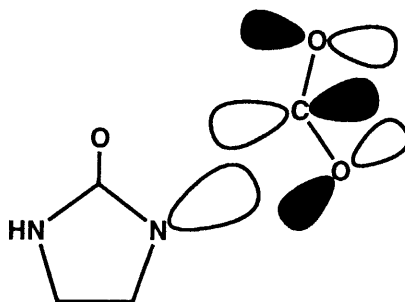
(B)  $\Psi(26a_1)$  of N-Carboxyimidazolidone

(C)  $\Psi(26a_1)$  of N-Carboxyimidazolidone

**Figure 3.4** Contour maps of the next HOMO of deprotonated imidazolidone and next HOMO ( $26a_1$ ) of N- and O-carboxy-imidazolidone

Contour values are  $\pm 0.3$ ,  $\pm 0.2$ ,  $\pm 0.15$ ,  $\pm 0.1$ ,  $\pm 0.075$ , and  $\pm 0.05$ .

consistent with the least distorted geometry of CO<sub>2</sub> in **3**. These results are interpreted in terms of  $\phi_{\text{donor}}$  of imidazolidone<sup>-</sup>; because  $\phi_{\text{donor}}$  includes lone pair type expansion at N and O atoms, the  $\eta^2$ -side-on approach of CO<sub>2</sub> cannot yield good overlap with  $\phi_{\text{donor}}$ , as shown in Scheme 3.4.



**Scheme 3.4**

Thus, the charge transfer from imidazolidone<sup>-</sup> to CO<sub>2</sub> does not occur strongly in **3**. This seems to be the main reason that the electron population of CO<sub>2</sub> increases only slightly and **3** is much less stable than **1** and **2**.

### **3-3-4 Determining Factors for the Binding Energy of CO<sub>2</sub>**

Because **3** is apparently unfavorable as discussed above, we will concentrate our discussion on the bonding nature of **1** and **2**. Their bonding nature was investigated with the energy decomposition analysis (EDA).

First, we will inspect **1** because it is the most stable. As shown in Table 3.5, the ES stabilization cannot overwhelm the EX repulsion. This means that the static interaction, which corresponds to the sum of ES and EX, does not contribute to the stabilization of **1**, and the charge-



transfer interaction is necessary to stabilize **1**. Of CTPLXA and CTPLXB, the CTPLXA term yields much greater stabilization energy than the CTPLXB term. This is consistent with the electron distribution that the CO<sub>2</sub> electron population significantly increases upon formation of **1**, since this term involves the charge-transfer from imidazolidone<sup>-</sup> to CO<sub>2</sub> as a main contributor. Thus, the charge-transfer from imidazolidone<sup>-</sup> to CO<sub>2</sub> is primarily important in **1** not only from the point of view of electron distribution but also from the point of view of binding energy. Similar results are also observed in **2** (Table 3.5).

Now, let us compare **1** and **2**, in order to clarify the reason that **1** is more stable than **2**. **1** receives greater stabilization energies from ES, CTPLXA, and CTPLXB terms but suffers greater destabilization energy from the EX term than does **2** at their equilibrium geometries. Thus, we cannot find clearly factors to stabilize **1** more than **2** by comparing **1** and **2** at their equilibrium geometries. In our previous EDA studies of transition metal complexes,<sup>23c,31</sup> we compared two complexes, M<sup>a</sup>L<sup>a</sup> and M<sup>b</sup>L<sup>b</sup>, at the inter-fragment distance which yielded the same EX repulsion. When two complexes exhibit the same EX values, we can consider that M<sup>a</sup> contacts with L<sup>a</sup> to a similar extent that M<sup>b</sup> does with L<sup>b</sup>, because the EX repulsion arises from the overlap of electron clouds between M<sup>a</sup> and L<sup>a</sup> (or between M<sup>b</sup> and L<sup>b</sup>). When the R(O-CO<sub>2</sub>) distance of **2** is shortened to 1.441 Å, the EX repulsion of **2** becomes almost the same as that of **1**. This geometry of **2** is named **2'** (see Table 3.5). Apparently, the outstanding difference is observed at the CTPLXA term; **1** can receive greater stabilization energy from this term than **2**. The ES

**Table 3.5** Energy decomposition analysis of the interaction between CO<sub>2</sub> and deprotonated imidazolidone in N-carboxyimidazolidone **1** and O-carboxyimidazolidone **2** (kcal/mol)<sup>a</sup>

	<b>1</b>	<b>2</b>	<b>2'</b> <sup>c</sup>
R(X-CO <sub>2</sub> ) <sup>b</sup>	1.516	1.572	1.441
BE	-40.1	-17.4	-19.5
DEF			
total	58.6	60.5	60.5
CO <sub>2</sub>	6.4	46.3	46.3
Imd	52.2	14.2	14.2
INT	-98.7	-77.9	-80.0
ES	-201.1	-139.5	-195.8
EX	321.2	209.2	322.5
CTPLXA (Imd→CO <sub>2</sub> )	-160.9	-103.7	-139.5
CTPLXB (CO <sub>2</sub> →Imd)	-52.7	-38.8	-62.3
R	-5.2	-5.1	-4.9

a) A negative value means stabilization in energy. The 6-31G basis set was used, where a d-polarization function was added to N and O atoms of imdazolidone. b) X = N or O. c) **2'**; The geometry was taken to be the same as **2** except that the O-CO<sub>2</sub> distance was shortened (1.441 Å) to give the same EX value as that of **1**.

stabilization energy is also larger in **1** than in **2**. Although **2** receives the greater stabilization energy from the CTPLXB term than **1** does, its difference is about one-half of the difference in the CTPLXA term. From these results, it is clearly concluded that the stronger CT interaction from imidazolidone<sup>-</sup> to CO<sub>2</sub> is a main factor to stabilize **1** more than **2**. This conclusion is easily understood by considering  $\phi_{\text{donor}}$  of imidazolidone<sup>-</sup>. As shown in Figure 3.4A,  $\phi_{\text{donor}}$  expands more largely on the N atom than on the O atom. Thus, CO<sub>2</sub> can form the stronger CT interaction by approaching to the N atom than by approaching to the O atom.

### 3-3-5 Reactivity of CO<sub>2</sub> in Carboxyimidazolidone

The knowledge on the reactivity of CO<sub>2</sub> in carboxyimidazolidone is potentially useful in understanding the enzymic function of biotin. The reactivity would strongly depend on electron distribution and frontier orbitals. The O atom of CO<sub>2</sub> becomes much negatively charged in carboxyimidazolidone (vide supra). This means that the coulombic interaction between the O atom and a cationic species would be easily formed in carboxyimidazolidone. Frontier orbital energies are given in Table 3.6. The 26a<sub>1</sub> orbital receives considerable contribution from the O p<sub>π</sub> orbitals (Figure 3.4B and 3.4C). This 26a<sub>1</sub> orbital lies at a higher energy than the non-bonding π orbital (HOMO) of the free CO<sub>2</sub> molecule like in NiF(NH<sub>3</sub>)<sub>4</sub>(η<sup>1</sup>-CO<sub>2</sub>) which was calculated as a model of the Ni<sup>I</sup>(cyclam)(CO<sub>2</sub>) complex.<sup>30c</sup> Furthermore, the nπ orbitals localized on the CO<sub>2</sub> part of carboxyimidazolidone lie much higher in energy than in the

**Table 3.6** Frontier orbital energies of carboxyimidazolidone<sup>a</sup>

Compound		Frontier Orbital	
N-carboxyimidazolidone	<b>1</b>	26a <sub>1</sub>	-6.3 eV
		nπ <sub>⊥</sub>	-5.3 eV
		nπ <sub>∥</sub>	-5.8 eV
O-carboxyimidazolidone	<b>2</b>	26a <sub>1</sub>	-7.6 eV
		nπ <sub>⊥</sub>	-6.6 eV
		nπ <sub>∥</sub>	-7.2 eV
NiF(NH <sub>3</sub> ) <sub>4</sub> (η <sup>1</sup> -CO <sub>2</sub> ) <sup>30b</sup>		HOMO	-8.2 eV
		nπ	-11.0 eV
free CO <sub>2</sub>		nπ	-14.6 eV

a) The 6-31G set was used, where a d-polarization function was added to N and O atoms of imidazolidone. b) nπ<sub>⊥</sub>; non-bonding π orbital of the CO<sub>2</sub> part. The subscript "⊥" represents that nπ orbital is perpendicular to the molecular plane of carboxyimidazolidone. c) nπ<sub>∥</sub>; non-bonding π orbital of CO<sub>2</sub> part. The subscript "∥" represents that the nπ orbitals is on the molecular plane of the carboxyimidazolidone.

free CO<sub>2</sub> molecule, probably because of strong charge-transfer from imidazolidone<sup>-</sup> to the CO<sub>2</sub> π\* orbital. Thus, an electrophile can react with the CO<sub>2</sub> part of **1** and **2** more easily than with the free CO<sub>2</sub>. In conclusion, CO<sub>2</sub> is much activated to an electrophile in both charge and frontier controlled reactions. This suggests the possibility that the CO<sub>2</sub> part in carboxybiotin would interact with some electrophile or cationic center and would be activated for the carboxyl-transfer reaction.

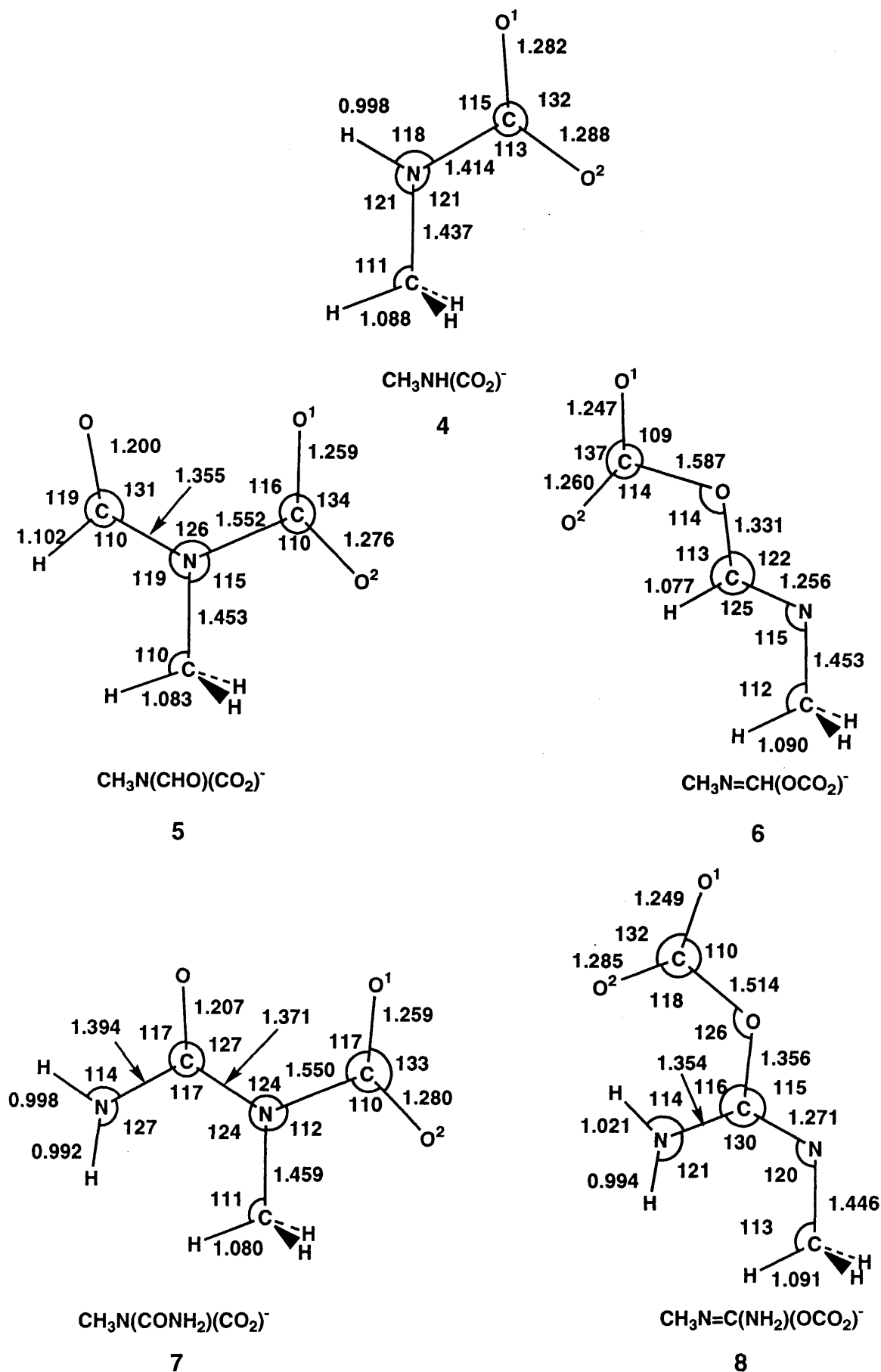
Also, we mention here that the above-described feature of CO<sub>2</sub> is quite the same as that observed in η<sup>1</sup>-C coordinated CO<sub>2</sub> complexes of transition metal.<sup>30</sup> Considering that η<sup>1</sup>-C coordinated CO<sub>2</sub> complexes of transition metal serve as a catalyst in many electrocatalytic reduction of CO<sub>2</sub>,<sup>32</sup> we can expect that carboxyimidazolidone is useful as an organic catalyst for the similar electrochemical reduction of CO<sub>2</sub> like transition metal complexes.

### 3-3-6 Reliable Model of Carboxybiotin

It is necessary to adopt a simple but reliable model for investigating theoretically the function of biotin.

CH<sub>3</sub>NH(CO<sub>2</sub>)<sup>-</sup> **4**, CH<sub>3</sub>N(CHO)(CO<sub>2</sub>)<sup>-</sup> **5**, CH<sub>3</sub>N=CH(OCO<sub>2</sub>)<sup>-</sup> **6**, CH<sub>3</sub>N(CONH<sub>2</sub>)(CO<sub>2</sub>)<sup>-</sup> **7**, and CH<sub>3</sub>N=C(NH<sub>2</sub>)(OCO<sub>2</sub>)<sup>-</sup> **8** are considered to be a candidate for a model of carboxybiotin. However, little has been known on the CO<sub>2</sub> binding energy, electron distribution, and energy levels of their frontier orbitals. We carried out MP4SDQ/6-31+G//MP2/3-21G calculations<sup>33</sup> on them and compared them with carboxyimidazolidone.

As shown in Figure 3.5, the geometry of **4** is considerably different from that of **1**; for instance, the N-



**Figure 3.5** Optimized geometries of  $\text{CH}_3\text{NH}(\text{CO}_2)^-$  **4**,  $\text{CH}_3\text{N}(\text{CHO})(\text{CO}_2)^-$  **5**,  $\text{CH}_3\text{N}=\text{CH}(\text{OCO}_2)^-$  **6**,  $\text{CH}_3\text{N}(\text{CONH}_2)(\text{CO}_2)^-$  **7**, and  $\text{CH}_3\text{N}=\text{C}(\text{NH}_2)(\text{OCO}_2)^-$  **8**

CO<sub>2</sub> distance of **4** is much shorter and the C-O<sup>1</sup> and C-O<sup>2</sup> distances are much longer than those in **1**. Consistent with these geometrical features, the binding energy (be) of **4** is much greater than that of **1** (Table 3.7). Also, the CO<sub>2</sub> electron population of CO<sub>2</sub> in **4** is considerably larger than that of **1** (Table 3.7). These results indicate that **4** is not appropriate as a model of carboxybiotin appropriate as a model of carboxybiotin.

**5** is considered to be a better model than **4** because the carbonyl group exists at the neighboring position of the active N atom like biotin (see Figure 3.5). The N-CO<sub>2</sub> distance of **5** is somewhat longer than that of **1**, while the C-O<sup>1</sup> and C-O<sup>2</sup> distances of **5** are similar to those of **1**. Thus, the geometrical features are improved upon going to **5** from **4**. The CO<sub>2</sub> binding energy of **5** is, however, much smaller than that of **1**. **6** is also examined as a model of **2**. Although the O-CO<sub>2</sub> distance (1.59 Å) is almost the same as it in **2**, the CO<sub>2</sub> binding energy is much smaller than that of **2**. Although the difference in the binding energy ( $\Delta be$ ) is similar to that between **1** and **2**, the CO<sub>2</sub> electron population of **5** is unexpectedly smaller than that of **6** unlike **1** and **2**. From these results, **5** and **6** would be better models than **4**, but they are still unreasonable for quantitative investigation of biotin.

**7** is considered to be a better model than **5**, because **7** has the urea structure like **1** (Figure 3.5). In fact, the CO<sub>2</sub> geometry in **7** is similar to that in **1**, whereas the N-CO<sub>2</sub> distance of **7** is calculated to be somewhat longer than that of **1**. The CO<sub>2</sub> binding energy is only 2-3 kcal/mol smaller than that of **1**. In **8** which is a model of **2**, the O-CO<sub>2</sub>

**Table 3.7** Binding energy (be) and the electron population of CO<sub>2</sub> in CH<sub>3</sub>NH(CO<sub>2</sub>)<sup>-</sup> **4**, CH<sub>3</sub>N(CHO)(CO<sub>2</sub>)<sup>-</sup> **5**, CH<sub>3</sub>N=CH(OCO<sub>2</sub>)<sup>-</sup> **6**, CH<sub>3</sub>NH(CONH<sub>2</sub>)(CO<sub>2</sub>)<sup>-</sup> **7**, and CH<sub>3</sub>N=C(NH<sub>2</sub>)(OCO<sub>2</sub>)<sup>-</sup> **8** (kcal/mol).

	CH <sub>3</sub> NH(CO <sub>2</sub> ) <sup>-</sup> <b>4</b>	CH <sub>3</sub> N(CHO)(CO <sub>2</sub> ) <sup>-</sup> <b>5</b>	CH <sub>3</sub> N=CH(OCO <sub>2</sub> ) <sup>-</sup> <b>6</b>
be			
HF	78.4	30.2	19.2(11.0) <sup>b</sup>
MP2	61.8	21.4	5.9(15.5)
MP3	72.2	28.9	15.8(13.1)
Mp4DQ	69.7	26.8	13.0(13.8)
MP4SDQ	69.1	26.2	11.2(15.0)
CO <sub>2</sub>	+0.53	+0.38	+0.43

	CH <sub>3</sub> N(CONH <sub>2</sub> )(CO <sub>2</sub> ) <sup>-</sup> <b>7</b>	CH <sub>3</sub> N=C(NH <sub>2</sub> )(OCO <sub>2</sub> ) <sup>-</sup> <b>8</b>
be		
HF	31.0	23.0(8.0) <sup>c</sup>
MP2	22.9	17.1(5.8)
MP3	30.3	25.6(4.7)
Mp4DQ	28.1	22.6(5.5)
MP4SDQ	27.5	21.4(6.1)
CO <sub>2</sub>	+0.37	+0.38

a) The 6-31G+ set was used, where a d-polarization function was added to N and O atoms of CH<sub>3</sub>NH<sup>-</sup>, CH<sub>3</sub>N(CHO)<sup>-</sup>, CH<sub>3</sub>N(CONH<sub>2</sub>), and deprotonated imidazolidone. b) In parentheses are differences in binding energy between CH<sub>3</sub>N(CHO)(CO<sub>2</sub>)<sup>-</sup> and CH<sub>3</sub>N=CH(OCO<sub>2</sub>)<sup>-</sup>. c) In parentheses are differences in binding energy between CH<sub>3</sub>N(CONH<sub>2</sub>)(CO<sub>2</sub>)<sup>-</sup> and CH<sub>3</sub>N=C(NH<sub>2</sub>)(OCO<sub>2</sub>)<sup>-</sup>.



distance is somewhat shorter and the CO<sub>2</sub> binding energy is slightly larger than those of **2**. These results show that **7** and **8** seem to be reasonable models of **1** and **2** respectively, and that the urea structure of biotin is important in the CO<sub>2</sub>-binding function of biotin.

### 3.4 Conclusions

Imidazolidone can be adopted as a reasonable model of biotin because imidazolidone and methylbiotin have very similar geometry, electron distribution, and  $\pi$  and  $\pi^*$  orbital energies. However, more simple compounds such as CH<sub>3</sub>NH<sub>2</sub> and CH<sub>3</sub>NH(CHO) are considered not to be a good model unlike imidazolidone. CH<sub>3</sub>NH(CONH<sub>2</sub>) seems reasonable as a model of biotin, because the CO<sub>2</sub> binding energy to CH<sub>3</sub>NH(CONH<sub>2</sub>) is almost the same as that of carboxyimidazolidone. These results suggest that the urea structure is important in the CO<sub>2</sub> binding function of biotin.

In N-carboxyimidazolidone **1** and O-carboxyimidazolidone **2**, CO<sub>2</sub> lies on the molecular plane. The perpendicular structure is less stable than the planar one by ca. 6 kcal/mol for **1** and 10 kcal/mol for **2** at the MP4(SDQ)/6-31G level. The binding energy of CO<sub>2</sub> in **1** is much greater than that of **2** by ca. 12 kcal/mol, indicating that **1** is more stable than **2**. This is in accord with the experimental result that N-carboxybiotin was isolated in the biotin-dependent enzymic reactions.<sup>7c</sup> The CO<sub>2</sub> binding energy of  $\eta^2$ -side-on carboxyimidazolidone **3** is much smaller than those of **1** and **2**, and geometry optimization of **3** led to **1**. Thus, the  $\eta^2$ -side-on CO<sub>2</sub> adduct would not exist in the reaction of

biotin.

In carboxyimidazolidone, the charge-transfer from imidazolidone<sup>-</sup> to CO<sub>2</sub> strongly occurs. The electron population of CO<sub>2</sub> increases in the order **3** < **2** < **1**. The O<sup>1</sup> and O<sup>2</sup> atomic populations increase but the C atomic population decreases upon formation of carboxyimidazolidones, **1** and **2**. This electron distribution can be interpreted in terms of the bonding interaction between  $\phi_{\text{donor}}$  of imidazolidone<sup>-</sup> and the CO<sub>2</sub>  $\pi^*$  orbital into which the  $\pi$  orbital of CO<sub>2</sub> mixes in an anti-bonding way with  $\phi_{\text{donor}}$ .

Energy decomposition analysis of the interaction between imidazolidone<sup>-</sup> and CO<sub>2</sub> also shows that the charge-transfer from imidazolidone<sup>-</sup> to CO<sub>2</sub> (the CTPLXA term) largely contributes to the CO<sub>2</sub> binding energy. The difference in stability between **1** and **2** mainly arises from this term. This is because the donor orbital (the next HOMO) of imidazolidone<sup>-</sup> expands more largely on the N atom than on the O atom. Consequently, **1** can receive greater stabilization energy from the CTPLXA term than **2**.

Geometries, electron distribution, and frontier orbitals of **1** and **2** resemble well those of  $\eta^1$ -C coordinated CO<sub>2</sub> complexes of transition metal, such as [Co(alcn)<sub>2</sub>( $\eta^1$ -CO<sub>2</sub>)]<sup>-</sup> (alcn = HNCHCHCHO<sup>-</sup>), RhCl(ASH<sub>3</sub>)<sub>4</sub>( $\eta^1$ -CO<sub>2</sub>)], and NiF(NH<sub>3</sub>)<sub>4</sub>( $\eta^1$ -CO<sub>2</sub>).<sup>30</sup> Considering that the several  $\eta^1$ -C coordinated CO<sub>2</sub> complexes of transition metal serve as a key intermediate in electrochemical reduction of CO<sub>2</sub>,<sup>32</sup> we can expect that biotin, imidazolidone, and their analogues would be useful as an organic catalyst for CO<sub>2</sub> reduction.

The CO<sub>2</sub> part in **1** is considerably activated for an electrophile. Thus, there is a possibility that the

electrophile or cationic species interacts with the O atom of CO<sub>2</sub> to activate it for the carboxyl-transfer reaction.

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- (33) This means that geometry is optimized at the MP2-level using the 3-21G basis set, and then, MP4SDQ calculation is carried out on the optimized geometry using the 6-31+G basis set. d-Polarization function was added to N and O of model compounds.

## **Part II**

# **Catalyses of Transition-metal Complexes Related to Activation of Small Molecules**



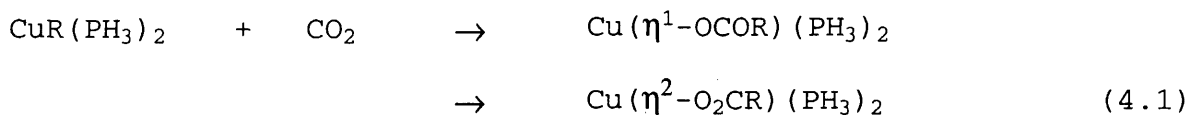
## Chapter 4

### **CO<sub>2</sub> and C<sub>2</sub>H<sub>4</sub> Insertion into a Cu(I)-R Bond (R = H, CH<sub>3</sub>, or OH).**

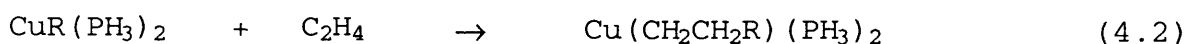
#### **4.1 Introduction**

CO<sub>2</sub> insertion into the M-R (R = H, CH<sub>3</sub>, or OR) bond has received considerable interest in the chemistry of CO<sub>2</sub> fixation<sup>1</sup> because similar insertion reactions of alkene, alkyne and CO are involved as key processes in many homogeneous catalytic cycles.<sup>2</sup> Actually, many examples of the catalytic CO<sub>2</sub> conversion into organic chemicals involve the CO<sub>2</sub> insertion as an important elementary step.<sup>3-12</sup> General knowledge on the CO<sub>2</sub> insertion is, therefore, necessary to understanding well the CO<sub>2</sub> fixation and finding a new efficient catalyst for the CO<sub>2</sub> fixation. In this context, experimental investigation of the CO<sub>2</sub> insertion has been actively carried out, in which various valid information has been reported.<sup>13-32</sup> Not only experimental work but also theoretical one is expected to offer such general knowledge. However, only few MO studies have been carried out on the CO<sub>2</sub> insertion.<sup>33,34</sup> In those studies, the geometry of transition state (TS) has not been optimized, and calculations at the correlated level have not been performed except for preliminary MP2 calculations of the CO<sub>2</sub> insertion into the Cu(I)-H and Cu(I)-CH<sub>3</sub> bonds.<sup>33</sup>

In this chapter, the CO<sub>2</sub> insertion into the Cu(I)-R bond (R = H, CH<sub>3</sub>, or OH) is theoretically investigated with the ab initio MO/MP4, SD-CI, and CCD (coupled cluster (doubles)) methods.



This reaction is selected here, considering that there are many experimental reports on the insertion reactions of CO<sub>2</sub> into Cu(I)-alkyl,<sup>13c-e,16b,e,18,26,27g</sup> Cu(I)-hydride,<sup>28</sup> and Cu-alkoxide bonds.<sup>13g,16a,d,f</sup> Aims of this chapter are (1) to optimize the geometry of the TS, (2) to estimate the activation energy and the energy of reaction, (3) to reveal characteristic features of the CO<sub>2</sub> insertion by comparing it with the C<sub>2</sub>H<sub>4</sub> insertion (eq 4.2), and (4) to clarify the



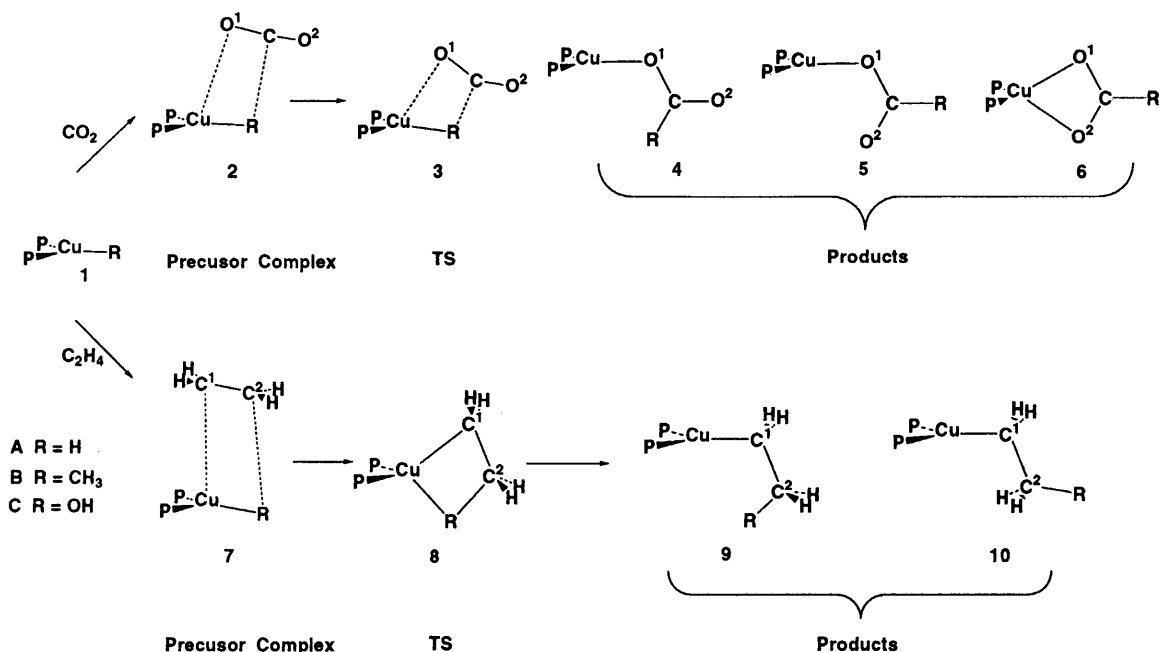
factors determining the ease of the CO<sub>2</sub> insertion. Points of departure from previous works<sup>33,34</sup> are on presenting (i) the detailed knowledge of the TS structure and (ii) discussion based on the calculations at the correlated level.

#### 4.2 Computational Details

Ab initio closed-shell Hartree-Fock (HF), MP2 - MP4(SDQ), SD-CI, and coupled cluster (doubles; CCD) calculations were carried out with Gaussian 86<sup>35a</sup> and 92<sup>35b</sup> programs, where four kinds of basis sets were employed. In the small basis set (BS I), core electrons of Cu (up to 3p) were replaced with effective core potentials (ECP1) proposed by Hay et al.<sup>36</sup> and its 3d, 4s, and 4p valence orbitals were represented with a (3s 2p 5d)/ [2s 2p 2d] set. Usual MIDI-3<sup>37</sup> and (4s)/[2s]<sup>38</sup> sets were used for C, O, and H respectively. STO-2G<sup>39</sup> sets were employed for PH<sub>3</sub>. In the

second (BS II), core electrons of Cu (up to 2p) were replaced with effective core potentials (ECP2), and its valence orbitals (3s, 3p, 3d, 4s, and 4p) were represented with a (5s 5p 5d)/[3s 3p 3d] set.<sup>40</sup> Usual MIDI-4 sets<sup>37</sup> were used for C, O, and P, and the (4s)/[2s] set was employed for H.<sup>38</sup> In the third (BS III), an all electron type basis set was used for Cu; Huzinaga's (13s 7p 4d) primitive set<sup>37</sup> was augmented with one diffuse d primitive function ( $\zeta = 0.141$ )<sup>41</sup> and two p primitive functions describing the valence 4p orbital, and the resultant (13s 9p 5d) primitive set was contracted to a [5s 4p 3d] set. For the other atoms, the same basis sets as those in the BS II were used. In the fourth (BS IV), (9s 5p)/[3s 2p]<sup>38</sup> sets were used for C and O. For Cu, a (14s 9p 5d) primitive set of Wachters<sup>42</sup> was augmented with one diffuse d primitive function ( $\zeta = 0.1491$ ) presented by Hay<sup>43</sup> and two p primitive functions ( $\zeta = 0.155065$  and  $0.046199$ ) describing the valence 4p orbitals.<sup>44</sup> The resultant (14s 11p 6d) primitive set was contracted to a [5s 4p 3d] set. For PH<sub>3</sub>, the same basis sets as those in the BS II and BS III were used. The BS I set was used only for geometry optimization, the BS II - IV for examination of basis set effects, and the BS III for investigation of energy changes, electron redistribution, and change in bonding nature by the insertion reactions. Calculations at the correlated level were performed with all the core orbitals excluded from an active space.

Both insertion reactions of CO<sub>2</sub> and C<sub>2</sub>H<sub>4</sub> are considered to proceed via the precursor complexes (PC) and TS, as shown in Chart 4.1. Geometries of CO<sub>2</sub>, C<sub>2</sub>H<sub>4</sub>, CuR(PH<sub>3</sub>)<sub>2</sub> **1** (see Chart 4.1 for **1** - **10**), PC (**2**, **7**), TS (**3**, **8**), and products



**Chart 4.1**

(4 - 6, 9, 10) were optimized with the energy gradient method at the HF level, in which the geometry of PH<sub>3</sub> was fixed to the experimental structure of the free PH<sub>3</sub> molecule.<sup>45</sup> There are several possible isomers in the products; See 4 - 6 in the CO<sub>2</sub> insertion and 9 and 10 in the C<sub>2</sub>H<sub>4</sub> insertion. **4A** and **4B** could not be optimized since they converted to **5A** and **5B**, respectively, with no barrier,<sup>33</sup> where A and B represent R = H and R = CH<sub>3</sub>, respectively. Their MO calculations were carried out under assumption that the geometry of the OC(O)R group and the Cu-O distance are the same as those in **5A** and **5B**. Because **5B** converted to **6B** with no barrier, the geometry of **5B** was optimized with the Cu-O<sup>1</sup> bond fixed on the Cu(PH<sub>3</sub>)<sub>2</sub> plane. Geometries of **9A** and **9B** were optimized under constraint of the C<sub>s</sub> symmetry. In the CO<sub>2</sub> insertion into the Cu-OH bond, PC and TS could not

be optimized because this reaction proceeded with no barrier at both HF and correlated levels (vide infra). Geometry changes by this insertion were optimized, taking the distance between O of OH and C of CO<sub>2</sub> as a reaction coordinate.

### **4.3 Results and Discussion**

#### **4-3-1 Effects of Basis Set and Electron Correlation on the CO<sub>2</sub> and C<sub>2</sub>H<sub>4</sub> Insertions**

Prior to detailed discussion, we will briefly examine basis set effects on the CO<sub>2</sub> insertion into the Cu-H bond. As shown in Table 4.1, the activation energy ( $E_a$ ) and the energy difference between the PC and the product ( $\Delta E$ ) significantly decrease upon going to the BS V from the BS VI,<sup>33b</sup> whereas only the basis set for Cu is different between BS V and BS VI; in the BS VI, a (3s 2p 5d)/[2s 2p 2d] set is employed with the ECP1,<sup>36</sup> but in the BS V, an all electron type basis set<sup>42</sup> is used (see footnotes a and b of Table 4.1 for BS V and BS VI). Similarly,  $E_a$  and  $\Delta E$  considerably decrease upon going to BS II from BS I, where ECP's for Cu is changed on going to BS II from BS I. On the other hand, BS II, BS III, and BS IV yield similar values for  $E_a$  and  $\Delta E$ , where basis sets for ligand atoms are improved upon going to BS IV from BS II. From these results, we can conclude that (1)  $E_a$  and  $\Delta E$  little depend on the basis sets of ligand atoms but significantly depend on the ECPs for Cu, (2) Huzinaga's basis set and Wachters' one for Cu give similar results on  $E_a$  and  $\Delta E$ , (3) the basis set involving the ECP1 yields considerably different results from others, and (4) the BS II involving ECP2 yields almost the same results as

**Table 4.1** Effects of Basis Set and Electron Correlation for CO<sub>2</sub> Insertion into Cu-H Bond (kcal/mol)

	CO <sub>2</sub> Insertion						C <sub>2</sub> H <sub>4</sub> Insertion
	BS-I	BS-II	BS-III	BS-IV	BS-V <sup>a</sup>	BS-VI <sup>b</sup>	BS-III
$E_a^c$							
HF	7.0	3.7	4.2	1.6	12.5	5.4	24.9
MP2		7.9	8.3	9.0	12.9		2.7
MP3		1.3	2.2	2.1			11.6
MP4 (DQ)			6.5				
MP4 (SDQ)			7.9				
SD-CI		3.2	4.5	4.2			6.8
SD-CI+D <sup>d</sup>		2.8	5.3	5.0			2.0
SD-CI+DS <sup>e</sup>		2.3	4.2	4.1			12.6
SD-CI+P <sup>f</sup>		2.4	4.3	4.1			9.9
$\Delta E^g$							
HF	-38.9	-50.4	-48.5	-53.8	-37.5	-56.8	-13.5
MP2		-34.5	-30.1	-34.3	-29.1		-19.4
MP3		-49.0	-43.9	-48.3			-15.7
MP4 (DQ)			-36.0				
MP4 (SDQ)			-33.1				
SD-CI		-46.6	-43.1	-45.5			-16.9
SD-CI+D <sup>d</sup>		-45.2	-41.0	-43.3			-16.8
SD-CI+DS <sup>e</sup>		-42.9	-40.0	-41.0			-16.3
SD-CI+P <sup>f</sup>		-44.3	-39.7	-41.9			-16.4

a) BS V (BS II of ref. 33b); The basis set for Cu was the same as it is in BS I, while the basis sets for the other parts were the same as those in BS VI. b) BS VI (BS III of ref. 33b); The basis sets for Cu, C, and O were the same as those in BS III, while MIDI-3 was used for PH<sub>3</sub>. c)  $E_a$  = the energy difference between the transition state and the precursor complex (PC). d) D = the Davidson's correction for higher order excitations.<sup>47</sup> e) DS = the Davidson and Silver's corrections for higher order excitations.<sup>48</sup> f) P = the Pople's for higher order excitations.<sup>49</sup> g)  $\Delta E$  = the energy difference between product and PC.

the better basis sets such as the BS III and BS IV. Thus, use of either BS II or better basis sets is necessary in estimating the energy change. Very recently, use of ECP2 has also been recommended.<sup>46</sup>

Then, we will inspect the correlation effects on  $E_a$  and  $\Delta E$ . Unexpectedly,  $E_a$  of the  $\text{CO}_2$  insertion little changes upon introducing electron correlation, except that the  $E_a$  value slightly fluctuates at the MP2 level. On the other hand, introduction of electron correlation considerably changes the  $E_a$  of the  $\text{C}_2\text{H}_4$  insertion and the  $\Delta E$  of both  $\text{CO}_2$  and  $\text{C}_2\text{H}_4$  insertion reactions. An important result to be noted is that both  $E_a$  of the  $\text{C}_2\text{H}_4$  insertion and  $\Delta E$  of  $\text{CO}_2$  and  $\text{C}_2\text{H}_4$  insertion reactions considerably fluctuate at MP2 - MP4(SDQ) levels, demonstrating that the MP2 - MP4(SDQ) methods are not reliable in investigating these insertion reactions. On the other hand, SD-CI and CCD methods give similar results on  $E_a$  and  $\Delta E$ , suggesting that these methods are reliable. Discussion presented here is based on the SD-CI and CCD calculations with the BS-III.

#### **4-3-2 Relative Stabilities of the Products and the Energy of Reaction**

The energies of reaction are given in Tables 4.2 and 4.3 as an energy difference between the products and the sum of reactants, **1A** +  $\text{CO}_2$ , **1A** +  $\text{C}_2\text{H}_4$ , **1B** +  $\text{CO}_2$ , and **1B** +  $\text{C}_2\text{H}_4$ , where a negative value represents a stabilization energy (vice versa).

In the product of the  $\text{CO}_2$  insertion, **6A** and **6B** are calculated to be the most stable in **4A** - **6A** and **4B** - **6B**, respectively, suggesting that  $\text{Cu}(\eta^2\text{-O}_2\text{CR})(\text{PH}_3)_2$  is a final

**Table 4.2** Energy Change by the CO<sub>2</sub> Insertion into Cu-R (R = H, CH<sub>3</sub>) bond (kcal/mol).

compd		HF	MP2	MP3	MP4	
					DQ	SDQ
$\text{CuH}(\text{PH}_3)_2 + \text{CO}_2 \rightarrow \text{Cu}(\eta^2\text{-O}_2\text{CH})(\text{PH}_3)_2$						
$\text{CuH}(\text{PH}_3)_2$ ( <b>1A</b> ) + CO <sub>2</sub>		0.0 <sup>a</sup>	0.0 <sup>b</sup>	0.0 <sup>c</sup>	0.0 <sup>d</sup>	0.0 <sup>e</sup>
$\text{CuH}(\text{PH}_3)_2(\text{CO}_2)$	<b>2A</b>	-3.6	-4.4	-5.1	-4.4	-4.5
Transtion State	<b>3A</b>	0.6	3.9	-2.9	2.1	3.4
$\text{Cu}(\eta^1\text{-OCOH})(\text{PH}_3)_2$	<b>4A</b>	-36.2	-19.6	-32.7	-25.5	-22.3
	<b>5A</b>	-50.9	-32.2	-46.0	-38.4	-35.2
$\text{Cu}(\eta^2\text{-O}_2\text{CH})(\text{PH}_3)_2$	<b>6A</b>	-52.1	-34.5	-49.0	-40.4	-37.0
$\text{Cu}(\text{CH}_3)(\text{PH}_3)_2 + \text{CO}_2 \rightarrow \text{Cu}(\eta^2\text{-O}_2\text{CCH}_3)(\text{PH}_3)_2$						
$\text{Cu}(\text{CH}_3)(\text{PH}_3)_2$ ( <b>1B</b> ) + CO <sub>2</sub>		0.0 <sup>k</sup>	0.0 <sup>l</sup>	0.0 <sup>l</sup>	0.0 <sup>m</sup>	0.0 <sup>n</sup>
$\text{Cu}(\text{CH}_3)(\text{PH}_3)_2(\text{CO}_2)$	<b>2B</b>	-2.1	-5.4	-4.9	-5.0	-5.2
Transtion State	<b>3B</b>	7.3	9.8	0.6	7.9	10.5
$\text{Cu}(\eta^1\text{-OCOCH}_3)(\text{PH}_3)_2$	<b>4B</b>	-26.3	-10.5	-25.3	-17.4	-13.2
	<b>5B</b>	-58.4	-35.7	-52.1	-43.7	-39.0
$\text{Cu}(\eta^2\text{-O}_2\text{CCH}_3)(\text{PH}_3)_2$	<b>6B</b>	-59.5	-37.5	-54.2	-45.3	-40.7

(Continued to be the next page)



		SD-CI				CCD
		no <sup>aa</sup>	D <sup>ab</sup>	DS <sup>ac</sup>	p <sup>ae</sup>	
CuH(PH <sub>3</sub> ) <sub>2</sub> ( <b>1A</b> )+CO <sub>2</sub>		0.0 <sup>k</sup>	0.0 <sup>l</sup>	0.0 <sup>m</sup>	0.0 <sup>n</sup>	0.0 <sup>o</sup>
CuH(PH <sub>3</sub> ) <sub>2</sub> (CO <sub>2</sub> )	<b>2A</b>	-4.5	-4.9	-5.0	-5.0	-4.7
Transtion State	<b>3A</b>	0.0	-0.4	-0.8	-0.7	-0.4
Cu(η <sup>1</sup> -OCOH)(PH <sub>3</sub> ) <sub>2</sub>	<b>4A</b>	-31.5	-30.0	-28.4	-28.7	
	<b>5A</b>	-45.4	-43.6	-42.1	-42.0	
Cu(η <sup>2</sup> -O <sub>2</sub> CH)(PH <sub>3</sub> ) <sub>2</sub>	<b>6A</b>	-47.6	-45.9	-44.5	-44.7	-44.7
Cu(CH <sub>3</sub> )(PH <sub>3</sub> ) <sub>2</sub> ( <b>1B</b> )+CO <sub>2</sub>		0.0 <sup>p</sup>	0.0 <sup>q</sup>	0.0 <sup>r</sup>	0.0 <sup>s</sup>	
Cu(CH <sub>3</sub> )(PH <sub>3</sub> ) <sub>2</sub> (CO <sub>2</sub> )	<b>2B</b>	-4.3	-4.8	-5.2	-5.1	
Transtion State	<b>3B</b>	5.6	4.9	4.1	4.2	
Cu(η <sup>1</sup> -OCOCH <sub>3</sub> )(PH <sub>3</sub> ) <sub>2</sub>	<b>4B</b>	-23.5	-22.1	-20.6	-20.9	
	<b>5B</b>	-52.0	-49.5	-47.1	-47.5	
Cu(η <sup>2</sup> -O <sub>2</sub> CCH <sub>3</sub> )(PH <sub>3</sub> ) <sub>2</sub>	<b>6B</b>	-53.7	-51.4	-49.1	-49.5	

a) E <sub>t</sub> (HF)	=	-2509.2289	k) E <sub>t</sub> (HF)	=	-2548.2017
b) E <sub>t</sub> (MP2)	=	-2510.0320	l) E <sub>t</sub> (MP2)	=	-2549.1011
c) E <sub>t</sub> (MP3)	=	-2509.9304	m) E <sub>t</sub> (MP3)	=	-2549.0048
d) E <sub>t</sub> (MP4(DQ))	=	-2510.0158	n) E <sub>t</sub> (MP4(DQ))	=	-2549.0930
e) E <sub>t</sub> (MP <sub>4</sub> (SDQ))	=	-2510.0628	o) E <sub>t</sub> (MP <sub>4</sub> (SDQ))	=	-2549.1425
f) E <sub>t</sub> (SDCI)	=	-2509.8562	p) E <sub>t</sub> (SDCI)	=	-2548.8976
g) E <sub>t</sub> (SDCI+(D))	=	-2509.9585	q) E <sub>t</sub> (SDCI+(D))	=	-2549.0193
h) E <sub>t</sub> (SDCI+(DS))	=	-2510.0080	r) E <sub>t</sub> (SDCI+(DS))	=	-2549.0848
i) E <sub>t</sub> (SDCI+(P))	=	-2509.9977	s) E <sub>t</sub> (SDCI+(P))	=	-2549.0731
j) E <sub>t</sub> (CCD)	=	-2509.9929	(hartree)		

aa) No correction was made for higher order excitations. ab) D = Davidson's correction for higher order excitations.<sup>47</sup> ac) DS = Davidson and Silver's correction for higher order excitations.<sup>48</sup> ad) P = Pople's correction for higher order excitations.<sup>48</sup>

**Table 4.3** Energy Change by the C<sub>2</sub>H<sub>4</sub> Insertion into Cu-R (R = H, CH<sub>3</sub>) bond (kcal/mol).

compd		HF	MP2	MP3	MP4	
					DQ	SDQ
$\text{CuH}(\text{PH}_3)_2 + \text{C}_2\text{H}_4 \rightarrow \text{Cu}(\text{C}_2\text{H}_5)(\text{PH}_3)_2$						
CuH(PH <sub>3</sub> ) <sub>2</sub> ( <b>1A</b> ) + C <sub>2</sub> H <sub>4</sub>		0.0 <sup>a</sup>	0.0 <sup>b</sup>	0.0 <sup>c</sup>	0.0 <sup>d</sup>	0.0 <sup>e</sup>
CuH(PH <sub>3</sub> ) <sub>2</sub> (C <sub>2</sub> H <sub>4</sub> )	<b>7A</b>	1.6	-1.3	-1.4	-0.9	-1.2
Transtion State	<b>8A</b>	24.9	1.4	10.2	5.9	0.8
	<b>9A</b>	-8.8	-17.6	-14.1	-14.8	-16.4
Cu(C <sub>2</sub> H <sub>5</sub> )(PH <sub>3</sub> ) <sub>2</sub>	<b>10A</b>	-11.9	-20.7	-17.1	-16.1	-19.5
$\text{Cu}(\text{CH}_3)(\text{PH}_3)_2 + \text{C}_2\text{H}_4 \rightarrow \text{Cu}(\text{C}_3\text{H}_7)(\text{PH}_3)_2$						
Cu(CH <sub>3</sub> )(PH <sub>3</sub> ) <sub>2</sub> ( <b>1B</b> ) + C <sub>2</sub> H <sub>4</sub>		0.0 <sup>k</sup>	0.0 <sup>l</sup>	0.0 <sup>m</sup>	0.0 <sup>n</sup>	0.0 <sup>o</sup>
Cu(CH <sub>3</sub> )(PH <sub>3</sub> ) <sub>2</sub> (C <sub>2</sub> H <sub>4</sub> )	<b>7B</b>	1.3	-3.0	-2.1	-2.4	-2.8
Transtion State	<b>8B</b>	39.1	20.4	24.2	24.7	22.5
	<b>9B</b>	-6.0	-12.7	-11.5	-11.3	-11.5
Cu(C <sub>3</sub> H <sub>7</sub> )(PH <sub>3</sub> ) <sub>2</sub>	<b>10B</b>	-13.9	-20.3	-18.5	-18.6	-18.9

(Continued to be the next page)

		SD-CI.				CCD
		no <sup>aa</sup>	D <sup>ab</sup>	DS <sup>ac</sup>	pad	
CuH(PH <sub>3</sub> ) <sub>2</sub> ( <b>1A</b> )+C <sub>2</sub> H <sub>4</sub>		0.0 <sup>f</sup>	0.0 <sup>g</sup>	0.0 <sup>h</sup>	0.0 <sup>i</sup>	0.0 <sup>j</sup>
CuH(PH <sub>3</sub> ) <sub>2</sub> (C <sub>2</sub> H <sub>4</sub> )	<b>7A</b>	-0.4	-0.9	-1.3	-1.2	-0.8
Transtion State	<b>8A</b>	12.2	9.0	6.7	7.2	9.7
	<b>9A</b>	-14.2	-14.6	-14.5	-14.4	
Cu(C <sub>2</sub> H <sub>5</sub> )(PH <sub>3</sub> ) <sub>2</sub>	<b>10A</b>	-17.3	-17.7	-17.6	-17.6	-16.4
Cu(CH <sub>3</sub> )(PH <sub>3</sub> ) <sub>2</sub> ( <b>1B</b> )+C <sub>2</sub> H <sub>4</sub>		0.0 <sup>p</sup>	0.0 <sup>q</sup>	0.0 <sup>r</sup>	0.0 <sup>s</sup>	
Cu(CH <sub>3</sub> )(PH <sub>3</sub> ) <sub>2</sub> (C <sub>2</sub> H <sub>4</sub> )	<b>7B</b>	-1.3	-0.4	1.0	-2.2	
Transtion State	<b>8B</b>	28.6	25.7	23.4	23.8	
	<b>9B</b>	-11.0	-11.4	-11.2	-11.2	
Cu(C <sub>3</sub> H <sub>7</sub> )(PH <sub>3</sub> ) <sub>2</sub>	<b>10B</b>	-18.4	-18.6	-18.3	-18.3	

a) E <sub>t</sub> (HF)	=	-2399.8294	k) E <sub>t</sub> (HF)	=	-2438.3989
b) E <sub>t</sub> (MP2)	=	-2400.4584	l) E <sub>t</sub> (MP2)	=	-2439.5275
c) E <sub>t</sub> (MP3)	=	-2400.4085	m) E <sub>t</sub> (MP3)	=	-2439.4829
d) E <sub>t</sub> (MP4(DQ))	=	-2400.4869	n) E <sub>t</sub> (MP4(DQ))	=	-2439.5641
e) E <sub>t</sub> (MP <sub>4</sub> (SDQ))	=	-2400.5232	o) E <sub>t</sub> (MP <sub>4</sub> (SDQ))	=	-2439.6029
f) E <sub>t</sub> (SDCI)	=	-2400.3548	p) E <sub>t</sub> (SDCI)	=	-2439.5458
g) E <sub>t</sub> (SDCI+(D))	=	-2400.4393	q) E <sub>t</sub> (SDCI+(D))	=	-2439.5020
h) E <sub>t</sub> (SDCI+(DS))	=	-2400.4794	r) E <sub>t</sub> (SDCI+(DS))	=	-2439.5565
i) E <sub>t</sub> (SDCI+(P))	=	-2400.4701	s) E <sub>t</sub> (SDCI+(P))	=	-2439.5275
j) E <sub>t</sub> (CCD)	=	-2400.4669	(hartree)		

aa) No correction was made for higher order excitations. ab) D = Davidson's correction for higher order excitations.<sup>47</sup> ac) DS = Davidson and Silver's correction for higher order excitations.<sup>48</sup> ad) P = Pople's correction for higher order excitations.<sup>48</sup>

product of the CO<sub>2</sub> insertion.<sup>33</sup> Relative stabilities of these products have been discussed in the previous work<sup>33b</sup> and the discussion is omitted here. Both CO<sub>2</sub> insertion reactions into the Cu-H and Cu-CH<sub>3</sub> bonds are significantly exothermic, and the exothermicity of the former is slightly greater than that of the latter.

In the product of the C<sub>2</sub>H<sub>4</sub> insertion, **10A** and **10B** are calculated to be more stable than **9A** and **9B** respectively, indicating that **10A** and **10B** are final products. The exothermicity of the C<sub>2</sub>H<sub>4</sub> insertion reaction hardly depends on the kind of R.

One of the differences between CO<sub>2</sub> insertion and C<sub>2</sub>H<sub>4</sub> insertion is that the former is much more exothermic than the latter. This difference is rationalized in terms of bond energies.<sup>50</sup> In the CO<sub>2</sub> insertion into the Cu-CH<sub>3</sub> bond, the CH<sub>3</sub>-C(O)O- bond is newly formed, and the Cu-CH<sub>3</sub> and C=O bonds change to the Cu-OC(O)CH<sub>3</sub> and C-O bonds respectively. Thus, the exothermicity (E<sub>exo</sub>) is approximately represented by eq 4.3;

$$\begin{aligned}
 E_{\text{exo}} &= E(\text{Cu-OC(O)CH}_3) + E(\text{C-O}) + E(\text{CH}_3\text{-C(O)O-}) - E(\text{Cu-CH}_3) \\
 &\quad - E(\text{C=O}) \\
 &= \{E(\text{Cu-OC(O)CH}_3) - E(\text{Cu-CH}_3)\} + \{E(\text{C-O}) - E(\text{C=O})\} \\
 &\quad + E(\text{CH}_3\text{-C(O)O-}) \quad (4.3)
 \end{aligned}$$

In the C<sub>2</sub>H<sub>4</sub> insertion into the Cu-CH<sub>3</sub> bond, the Cu-CH<sub>3</sub> and C=C bonds change to the Cu-C<sub>3</sub>H<sub>7</sub> and -CH<sub>2</sub>-CH<sub>2</sub>- bonds respectively, and the -CH<sub>2</sub>-CH<sub>3</sub> bond is newly formed. In this case, E<sub>exo</sub> is approximately represented, as follows;

$$\begin{aligned}
E_{\text{exo}} &= E(\text{Cu-C}_3\text{H}_7) - E(\text{Cu-CH}_3) + E(-\text{CH}_2-\text{CH}_3) \\
&\quad + E(-\text{CH}_2-\text{CH}_2-) - E(\text{C}=\text{C}) \\
&\sim \{E(-\text{CH}_2-\text{CH}_2-) - E(\text{>C}=\text{C})\} + E(-\text{CH}_2-\text{CH}_3) \quad (4.4)
\end{aligned}$$

where  $E(\text{Cu-CH}_3)$  is considered to be almost the same as  $E(\text{Cu-C}_3\text{H}_7)$ .

A difference between C=O and C-O bond energies which is involved in eq 4.3 can be estimated from the energy difference ( $\Delta E_{r-1}$ ) between right- and left-hand sides of eq 4.5, as follows;



$$\Delta E_{r-1} = E(\text{H-H}) + E(\text{=C=O}) - E(\text{=C-O}) - E(\text{=C-H}) - E(\text{H-H}) \quad (4.6a)$$

$$E(\text{=C=O}) - E(\text{=C-O}) = \Delta E_{r-1} - E(\text{H-H}) + E(\text{=C-H}) + E(\text{H-H}) \quad (4.6b)$$

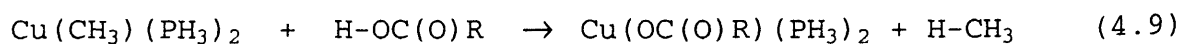
Similarly, a difference between the C=C and -CH<sub>2</sub>-CH<sub>2</sub>- bond energies is estimated from  $\Delta E_{r-1}$  of eq 4.7;



$$\Delta E_{r-1} = E(\text{H-H}) + E(\text{>C}=\text{C}) - E(\text{>C}-\text{C}) - 2 \cdot E(\text{>C-H}) \quad (4.8a)$$

$$E(\text{>C}=\text{C}) - E(\text{>C}-\text{C}) = \Delta E_{r-1} - E(\text{H-H}) + 2 \cdot E(\text{>C-H}) \quad (4.8b)$$

In these estimations, the H-H and -C-H bond energies are calculated with MP2 - MP4(SDQ) and SD-CI/BS III methods (Table 4.4), where geometries of  $\bullet\text{C}_2\text{H}_5$ ,  $\bullet\text{C(O)OH}$ , and  $\text{H-C(O)O}\bullet$  radicals are optimized with the ROHF/BS I method. A difference between Cu-CH<sub>3</sub> and Cu-OC(O)R bond energies can be evaluated, considering the energy difference between right- and left-hand sides of eq 4.9;



$$\Delta E_{r-1} = E(\text{H-CH}_3) + E(\text{Cu-OC(O)R}) - E(\text{Cu-CH}_3) - E(\text{-O-H}) \quad (4.10a)$$

**Table 4.4** Bond Energies and Their Differences (kcal/mol unit)

	E(H-H)	E(H-COOH)	E(HCOO-H)	E(H-CH <sub>3</sub> )	E(H <sub>3</sub> C-CH <sub>3</sub> )
MP2	93.2	96.3	106.3	99.4	95.0
MP3	96.5	99.2	102.5	100.1	95.6
MP4DQ	97.5	99.0	103.9	100.4	98.7
MP4SDQ	97.5	98.0	103.7	100.5	98.7
SD-CI+D <sup>a</sup>	97.9	95.0	101.6	100.2	95.6
SD-CI+DS <sup>b</sup>	97.9	93.8	102.1	100.4	96.5
SD-CI+P <sup>c</sup>	97.9	97.8	109.0	100.2	96.7

a) D = Davidson's correction for higher order excitations.<sup>47</sup> b) DS = Davidson-Silver's corrections for higher order excitations.<sup>48</sup> c) P = Pople's correction for higher order excitations.<sup>49</sup>

**Table 4.4** (Continued)

	E(H-C <sub>2</sub> H <sub>5</sub> )	E(C=O)-E(C-O)	E(C=C)-E(C-C)	E(H <sub>3</sub> C-COOH)
MP2	101.7	124.7	74.0	93.5
MP3	102.2	113.4	71.0	94.1
MP4DQ	102.4	111.0	71.8	93.0
MP4SDQ	102.3	106.5	72.0	92.0
SD-CI+D	101.9	101.2	72.0	84.0
SD-CI+DS	104.4	102.6	74.6	86.7
SD-CI+P	102.1	102.1	72.8	90.7

(Continued to be the next page)

**Table 4.4** (Continued)

---

	E(HO-COOH)	E(HO-COO-H)	E(HO-H)	E(Cu-OC(O)CH <sub>3</sub> ) - E(Cu-H)
MP2	92.1	102.7	102.5	56.1
MP3	87.0	99.4	99.6	56.5
MP4DQ	86.9	100.9	100.7	51.5
MP4SDQ	87.1	100.7	100.8	49.4
SD-CI+D	62.3	98.1	83.5	61.2
SD-CI+DS	64.3	99.5	98.7	55.6
SD-CI+P	85.7	99.1	100.1	55.7

---

**Table 4.4** (Continued)

---

	E(CuOC(O)H) - E(Cu-H)	E(CU-OCOOH) - E(Cu-OH)
MP2	47.5	32.3
MP3	43.7	39.7
MP4DQ	38.1	34.0
MP4SDQ	37.5	29.5
SD-CI+D	18.8	30.0
SD-CI+DS	34.4	29.5
SD-CI+P	34.9	28.8

---

$$E(\text{Cu-OC(O)R}) - E(\text{Cu-CH}_3) = \Delta E_{r-1} - E(\text{H-CH}_3) - E(\text{-O-H}) \quad (4.10b)$$

where -O-H and H-C(O)OR bond energies can be estimated as described above. Using these bond energies and their differences (Table 4.4), a difference in  $E_{\text{exo}}$  between  $\text{CO}_2$  and  $\text{C}_2\text{H}_4$  insertion reactions will be discussed. The difference between C=O and C-O bond energies is about 100 kcal/mol, about 30 kcal/mol greater than the difference between C=C and -CH<sub>2</sub>-CH<sub>2</sub>- bond energies. Thus, the  $E(\text{C-O}) - E(\text{C=O})$  term is not responsible for the higher exothermicity of the  $\text{CO}_2$  insertion.

The  $\text{H}_3\text{C-CH}_3$  bond energy does not differ very much from the  $\text{H}_3\text{C-C(O)OR}$  bond energy (see Table 4.4), yielding only a little difference in the exothermicity between the  $\text{CO}_2$  and  $\text{C}_2\text{H}_4$  insertion reactions. On the other hand,  $E(\text{Cu-OC(O)R})$  is larger than  $E(\text{Cu-CH}_3)$  by ca. 50 kcal/mol, indicating that the term,  $E(\text{Cu-OC(O)R}) - E(\text{Cu-CH}_3)$ , results in the greater exothermicity of the  $\text{CO}_2$  insertion than that of the  $\text{C}_2\text{H}_4$  insertion. In other words, the greater exothermicity of the  $\text{CO}_2$  insertion is due to the stronger Cu-OC(O)CH<sub>3</sub> bond than the Cu-CH<sub>3</sub> bond.

Similarly, exothermicities of the  $\text{CO}_2$  and  $\text{C}_2\text{H}_4$  insertion reactions into the Cu-H bond are represented by eqs 4.11 and 4.12, respectively.

$$\begin{aligned} E_{\text{exo}} &= E(\text{Cu-OC(O)H}) + E(\text{C-O}) + E(\text{H-C(O)OR}) \\ &\quad - E(\text{Cu-H}) - E(\text{C=O}) \\ &= E(\text{Cu-OC(O)H}) + \{E(\text{C-O}) - E(\text{C=O})\} \\ &\quad + E(\text{H-C(O)OR}) - E(\text{Cu-H}) \quad (4.11) \end{aligned}$$

$$\begin{aligned} E_{\text{exo}} &= E(\text{Cu-C}_2\text{H}_5) + E(\text{-CH}_2\text{-CH}_2\text{-}) + E(\text{H-C}_2\text{H}_5) \\ &\quad - E(\text{Cu-H}) - E(\text{>C=C<}) \end{aligned}$$



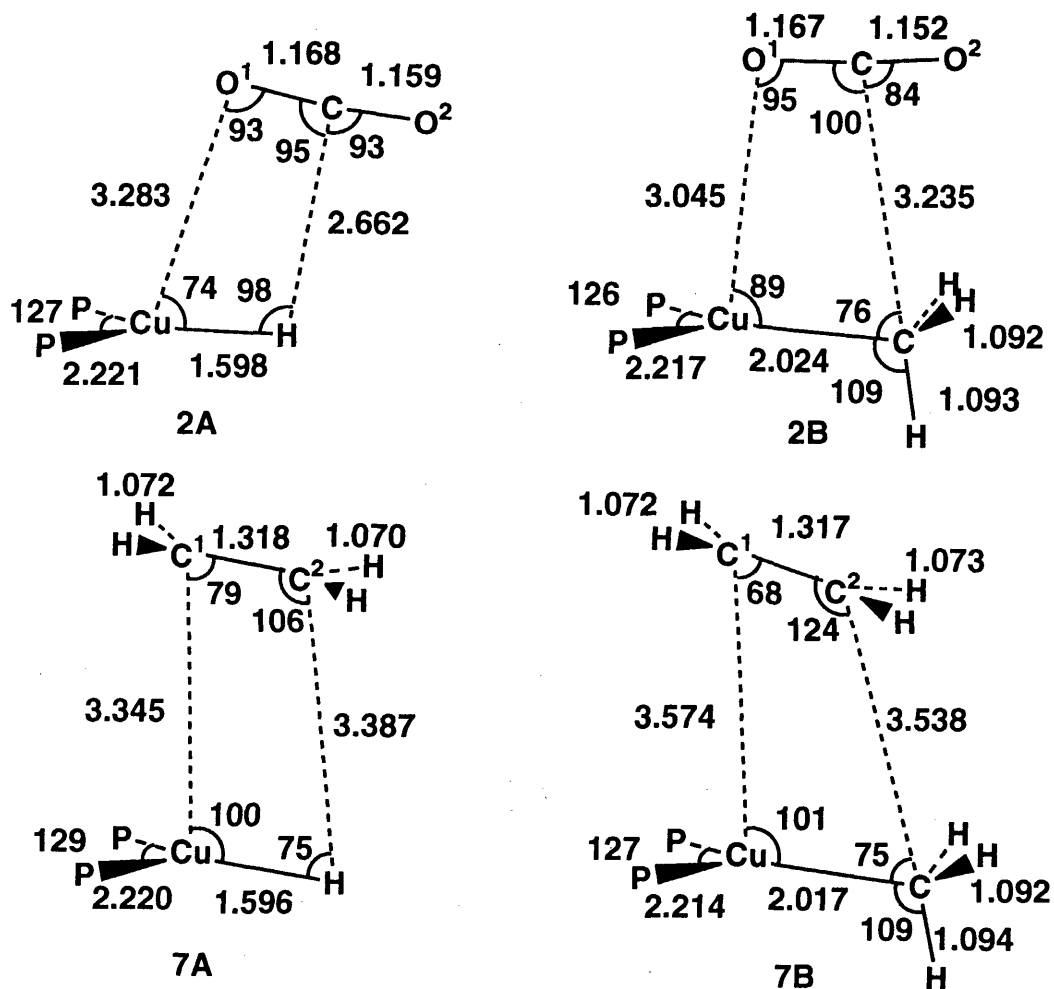
$$\begin{aligned}
= & E(\text{Cu-C}_2\text{H}_5) + \{E(-\text{CH}_2-\text{CH}_2-) - E(\text{C}=\text{C})\} \\
& + E(\text{H-C}_2\text{H}_5) - E(\text{Cu-H}) \quad (4.12)
\end{aligned}$$

The difference,  $E(\text{C}=\text{O}) - E(\text{C}-\text{O})$ , is larger than the difference,  $E(\text{C}=\text{C}) - E(-\text{CH}_2-\text{CH}_2-)$ , as discussed above.  $E(\text{H-C}(\text{O})\text{OR})$  is calculated to be similar to  $E(\text{H-C}_2\text{H}_5)$ , as shown in Table 4.4. Thus, these two terms do not lead to the greater exothermicity of the  $\text{CO}_2$  insertion into the Cu-H bond. On the other hand,  $E(\text{Cu-OC}(\text{O})\text{H})$  is much larger than  $E(\text{Cu-C}_2\text{H}_5)$ . This is a main reason for the greater exothermicity of the  $\text{CO}_2$  insertion into the Cu-H bond than that of the  $\text{C}_2\text{H}_4$  insertion.

#### 4-3-3 Geometries of Precursor Complex and Transition State

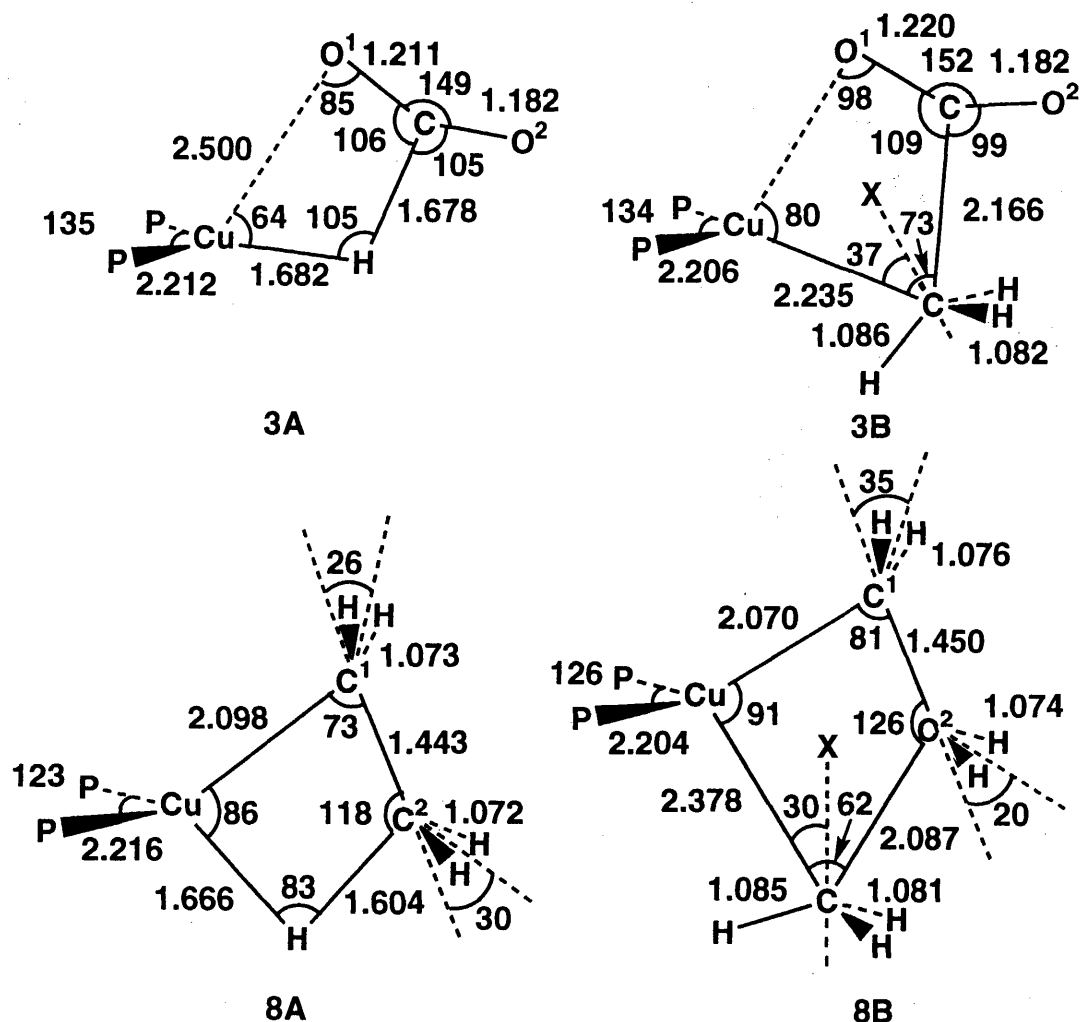
Geometries of precursor complexes (PC) and transition states (TS) are shown in Figures 4.1 and 4.2, respectively. In the PCs, the Cu- $\text{CO}_2$  and Cu- $\text{C}_2\text{H}_4$  distances are considerably long. Correspondingly, geometries of  $\text{CO}_2$ ,  $\text{C}_2\text{H}_4$ , and  $\text{CuR}(\text{PH}_3)_2$  parts only slightly distort from those of reactants. Consistent with these geometrical features, stabilization energies of PCs (Tables 4.2 and 4.3) are much smaller than that of the usual coordinate bond, indicating that  $\text{CO}_2$  and  $\text{C}_2\text{H}_4$  weakly interact with  $\text{CuR}(\text{PH}_3)_2$  like a van der Waals complex.

In the TS of the  $\text{CO}_2$  insertion into the Cu-H bond (**3A** in Figure 4.2), both C-H and Cu- $\text{O}^2$  distances between  $\text{CO}_2$  and  $\text{CuH}(\text{PH}_3)_2$  are much longer than those in the product. The Cu-H and C- $\text{O}^1$  bonds somewhat lengthen by ca. 0.1 Å and ca. 0.05 Å respectively, and the  $\text{CO}_2$  part starts to bend ( $\angle\text{OCO} = 150^\circ$ ). Similar features are observed in the TS of the  $\text{CO}_2$  insertion into the Cu- $\text{CH}_3$  bond (**3B** in Figure 4.2). There is, however, a



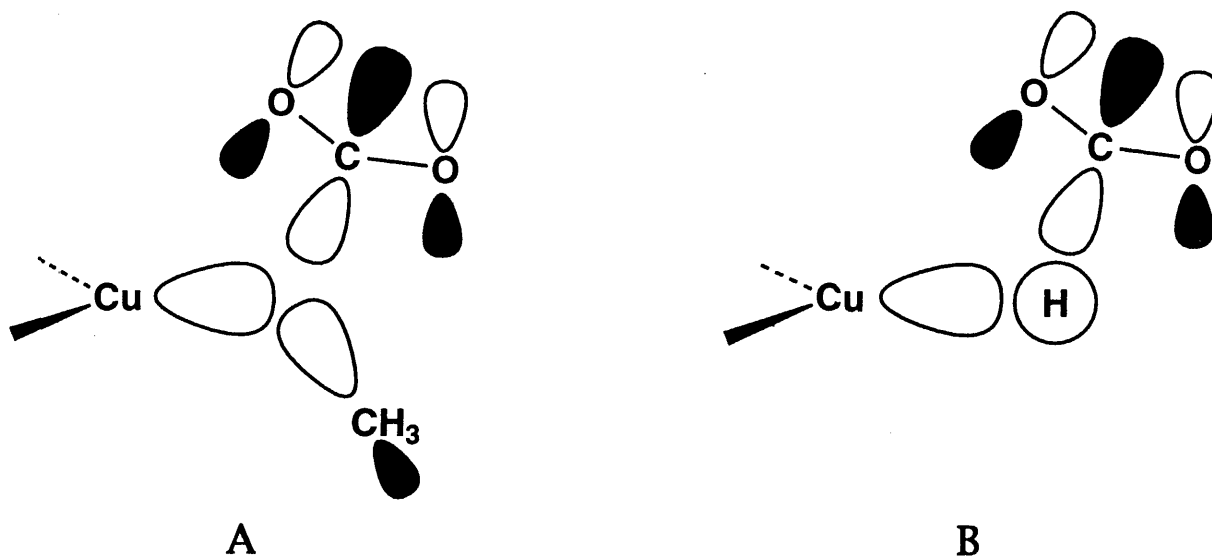
**Figure 4.1** Optimized geometries of precursor complexes in the CO<sub>2</sub> and C<sub>2</sub>H<sub>4</sub> insertions into the Cu-H and Cu-CH<sub>3</sub> bonds. Bond length in Å and angle in degree.

critical difference between **3A** and **3B**; the CH<sub>3</sub> ligand considerably moves downward and changes its direction toward the incoming CO<sub>2</sub> molecule, whereas the H ligand only slightly moves downward at the TS. This difference between CuH(PH<sub>3</sub>)<sub>2</sub> and Cu(CH<sub>3</sub>)(PH<sub>3</sub>)<sub>2</sub> is easily interpreted in terms of the valence orbitals of CH<sub>3</sub> and H ligands. Because of the highly directional sp<sup>3</sup> valence orbital, the CH<sub>3</sub> ligand must change its



**Figure 4.2** Optimized geometries of transition state in the CO<sub>2</sub> and C<sub>2</sub>H<sub>4</sub> insertions into the Cu-H and Cu-CH<sub>3</sub> bonds. Bond length in Å and angle in degree. X represents the direction of CH<sub>3</sub>.

direction toward CO<sub>2</sub> in order to form a new bond with CO<sub>2</sub>. At the same time, the CH<sub>3</sub> ligand wants to keep a bonding interaction with Cu as much as possible. Thus, the downward movement of CH<sub>3</sub> occurs to satisfy these two requisites, as schematically shown in Chart 4.2A. On the other hand, the H ligand does not need to change its position because it can form a new bond with the incoming CO<sub>2</sub>, keeping the coordinate



**Chart 4.2**

bond with Cu, due to its spherical  $1s$  valence orbital (Chart 4.2B).

The TS of the  $C_2H_4$  insertion into the Cu-R bond (H or  $CH_3$ ) exhibits interesting features (Figure 4.2), as follows; (1) the Cu-H distance slightly lengthens but the Cu- $CH_3$  bond considerably lengthens, (2) both H and  $CH_3$  ligands considerably move downward, (3) the  $C^1-C^2$  bond of  $C_2H_4$  considerably lengthens by  $0.13 \text{ \AA}$ , and the  $C^1H_2$  and  $C^2H_2$  planes are remarkably bent by 26 and 30 degrees respectively, (4) the Cu- $C^1$  distance is short ( $2.1 \text{ \AA}$ ) like it in the product, but the  $C^2-R$  bond is still long. These features suggest that the TS of the  $C_2H_4$  insertion is product-like compared to the TS of the  $CO_2$  insertion, and that the Cu- $C^1$  bond is formed prior to the formation of the  $C^2-R$  bond (remember that both Cu- $O^1$  and C-R bonds between  $CO_2$  and  $CuR(PH_3)_2$  are not formed yet at the TS

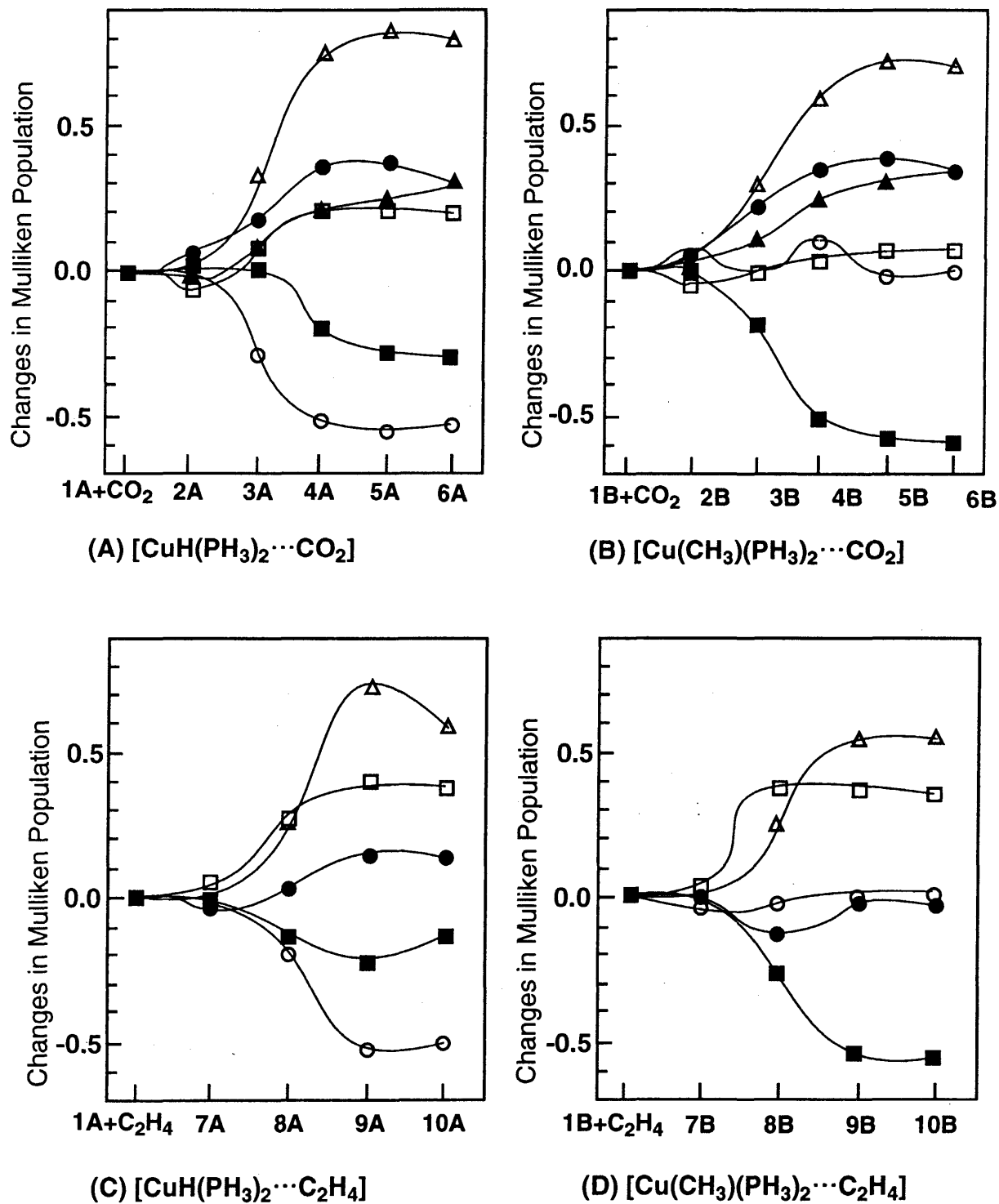
of the CO<sub>2</sub> insertion). These differences between CO<sub>2</sub> and C<sub>2</sub>H<sub>4</sub> insertion reactions will be discussed below.

Activation energies ( $E_a$ ) of these insertion reactions are given in Tables 4.2 and 4.3. Both CO<sub>2</sub> and C<sub>2</sub>H<sub>4</sub> are inserted into the Cu-H bond with lower activation energies than into the Cu-CH<sub>3</sub> bond. This result can be interpreted in terms of the valence orbitals of H and CH<sub>3</sub> ligands, again; as described above, the CuH(PH<sub>3</sub>)<sub>2</sub> part distorts at the TS to a lesser extent than the Cu(CH<sub>3</sub>)(PH<sub>3</sub>)<sub>2</sub> part because the 1s valence orbital of H is spherical but the sp<sup>3</sup> valence orbital of CH<sub>3</sub> is directional.

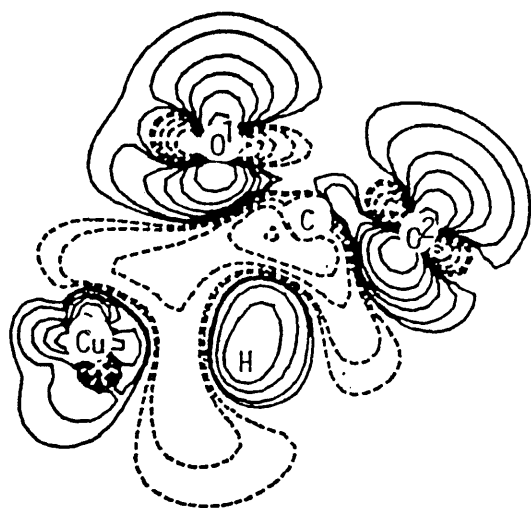
Accordingly, the insertion into the Cu-CH<sub>3</sub> bond needs higher activation energy, due to the greater distortion energy of the Cu(CH<sub>3</sub>)(PH<sub>3</sub>)<sub>2</sub> part. Consistent with this result, Darensbourg et al. experimentally suggested that CO<sub>2</sub> could be inserted into the Ni-H bond but could be not into the Ni-CH<sub>3</sub> bond.<sup>27m</sup> The other interesting result to be noted is that the C<sub>2</sub>H<sub>4</sub> insertion requires a higher activation energy than the CO<sub>2</sub> insertion, which will be discussed after investigating characters of the TS.

#### **4-3-4 Electron Redistribution in the CO<sub>2</sub> and C<sub>2</sub>H<sub>4</sub> Insertion Reactions and the Reasons for Low Activation Energy of the CO<sub>2</sub> Insertion.**

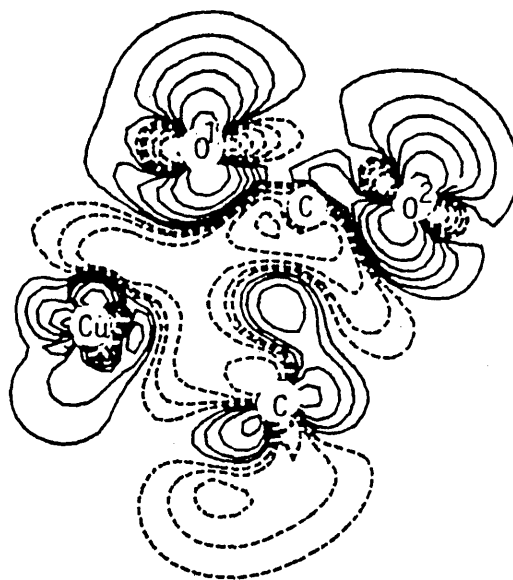
Changes in Mulliken populations by these reactions are shown in Figure 4.3. In all the insertion reactions examined, electron populations of CO<sub>2</sub> and C<sub>2</sub>H<sub>4</sub> remarkably increase as the reaction proceeds, indicating that the charge-transfer from CuR(PH<sub>3</sub>)<sub>2</sub> to CO<sub>2</sub> or C<sub>2</sub>H<sub>4</sub> takes place in these reactions. In the insertion into the Cu-H bond, electron populations of both Cu and H significantly decrease (Figures 4.3A and 4.3C). This



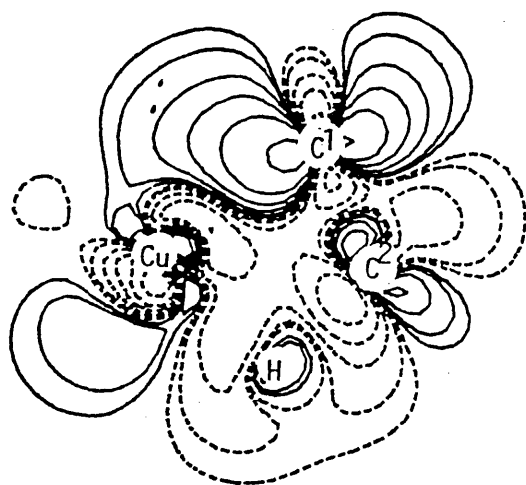
**Figure 4.3** Changes in Mulliken populations caused by  $\text{CO}_2$  and  $\text{C}_2\text{H}_4$  insertions into Cu-H and Cu- $\text{CH}_3$  bonds. (A)  $\text{CO}_2$  insertion into the Cu-H bond. (B)  $\text{CO}_2$  insertion into the Cu- $\text{CH}_3$  bond. (C)  $\text{C}_2\text{H}_4$  insertion into the Cu-H bond. (D)  $\text{C}_2\text{H}_4$  insertion into the Cu- $\text{CH}_3$  bond.



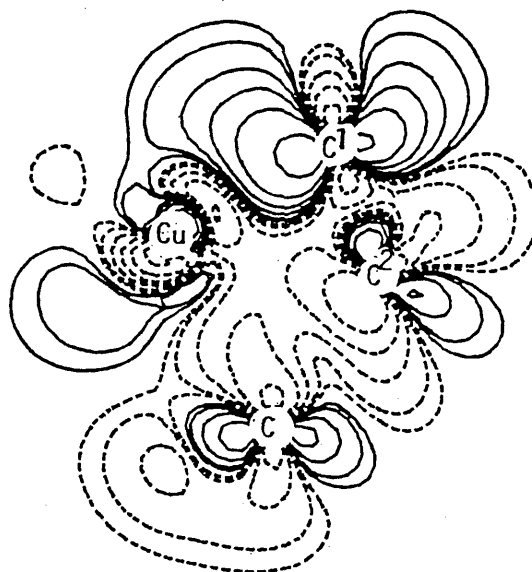
(A)  $\text{CuH}(\text{PH}_3)_2 + \text{CO}_2$



(B)  $\text{Cu}(\text{CH}_3)(\text{PH}_3)_2 + \text{CO}_2$

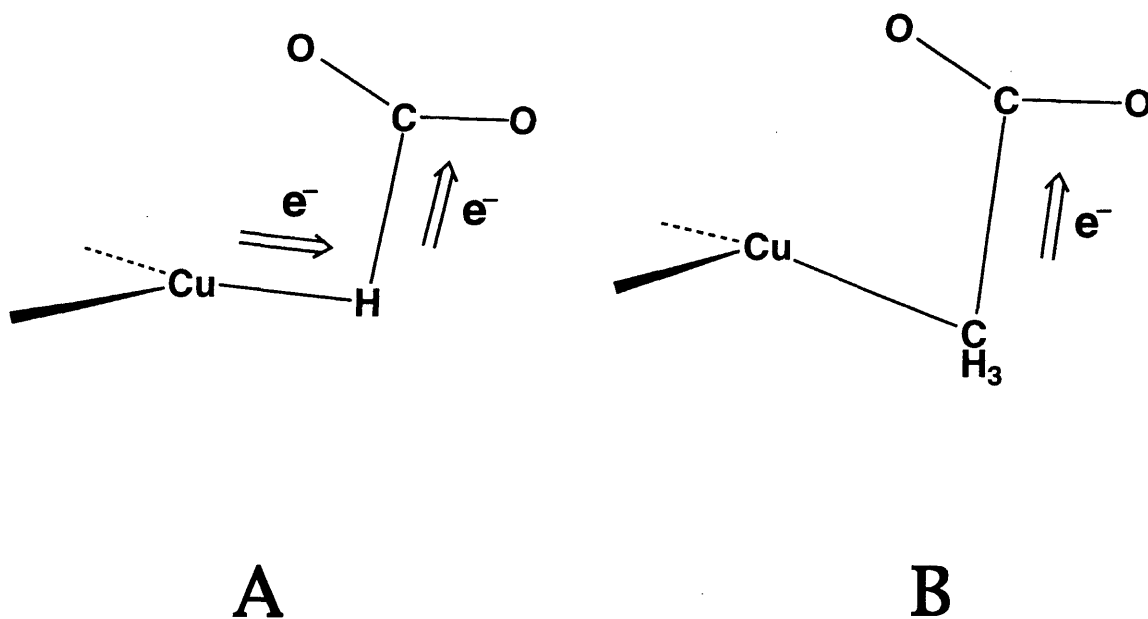


(C)  $\text{CuH}(\text{PH}_3)_2 + \text{C}_2\text{H}_4$



(D)  $\text{Cu}(\text{CH}_3)(\text{PH}_3)_2 + \text{C}_2\text{H}_4$

**Figure 4.4** Difference density maps at the transition state of  $\text{CO}_2$  and  $\text{C}_2\text{H}_4$  insertions into the Cu-H and Cu- $\text{CH}_3$  bonds (A)  $[\text{CuH}(\text{PH}_3)\cdots(\text{CO}_2)]$ , **3A**, (B)  $[\text{Cu}(\text{CH}_3)(\text{PH}_3)\cdots(\text{CO}_2)]$ , **3B**, (C)  $[\text{CuH}(\text{PH}_3)_2\cdots(\text{CO}_2)]$ , **9A**, (D)  $[\text{Cu}(\text{CH}_3)(\text{PH}_3)_2\cdots(\text{CO}_2)]$ , **9B**. Contour values are  $\pm 0.05$ ,  $\pm 0.02$ ,  $\pm 0.005$ ,  $\pm 0.002$ , and  $\pm 0.01$ .



**Chart 4.3**

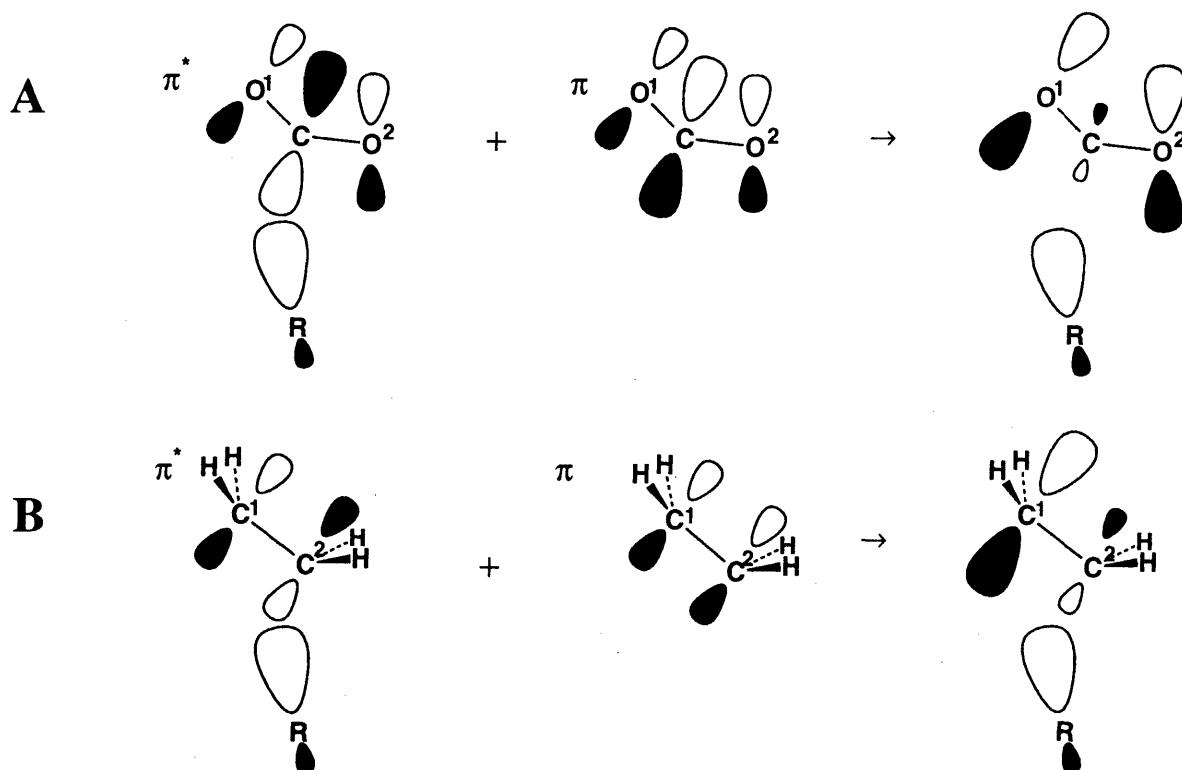
implies that the insertion into the Cu-H bond causes the charge-transfer from the H ligand to  $\text{CO}_2$  or  $\text{C}_2\text{H}_4$  concomitantly with the polarization of  $\text{CuH}(\text{PH}_3)_2$  which induces electron flow from Cu to H (Chart 4.3A). In the insertion into the Cu- $\text{CH}_3$  bond, on the other hand, electron population of  $\text{CH}_3$  considerably decreases but electron population of Cu hardly changes (Figures 4.3B and 4.3D), indicating that the insertion into the Cu- $\text{CH}_3$  bond causes only charge-transfer to  $\text{CO}_2$  or  $\text{C}_2\text{H}_4$  from the  $\text{CH}_3$  ligand (Chart 4.3B) unlike the insertion into the Cu-H bond. This difference between  $\text{R} = \text{CH}_3$  and  $\text{R} = \text{H}$  is easily interpreted in terms of the directionality of the valence orbital, again. Because the Cu- $\text{CH}_3$  bond must be broken to form a new  $\text{CH}_3\text{-CO}_2$  bond at the TS due to the directional  $\text{sp}^3$  valence orbital of  $\text{CH}_3$ , the electron flow from



Cu to CH<sub>3</sub> becomes difficult at around the TS. On the other hand, the electron flow from Cu to H can occur, because the Cu-H bond still exists at the TS due to the spherical 1s valence orbital of H.

Electron redistribution at the TS is investigated in more detail, inspecting the difference density maps (Figure 4.4); the difference density =  $\rho[\text{CuR}(\text{PH}_3)_2 \cdots \text{Sub}]_{\text{TS}} - \rho[\text{CuR}(\text{PH}_3)_2] - \rho[\text{Sub}]$ , where Sub means CO<sub>2</sub> or C<sub>2</sub>H<sub>4</sub>. An important feature found in the CO<sub>2</sub> insertion (Figures 4.4A and 4.4B) is that electron density accumulates on the terminal O atoms but slightly decreases on the central C atom. This feature arises from the HOMO,  $\Psi_{\text{HOMO}}(\text{CuR} \cdots \text{CO}_2)$ , of the reaction system. This  $\Psi_{\text{HOMO}}(\text{CuR} \cdots \text{CO}_2)$  resembles well the HOMO,  $\Psi_{\text{HOMO}}(\text{CO}_2 \cdots \text{R}^-)$ , of the CO<sub>2</sub> ⋯ R<sup>-</sup> system, as clearly shown in Figures 4.5A, 4.5B, 4.5E, and 4.5F. Both  $\Psi_{\text{HOMO}}(\text{CuR} \cdots \text{CO}_2)$  and  $\Psi_{\text{HOMO}}(\text{CO}_2 \cdots \text{R}^-)$  mainly consist of the large p<sub>π</sub> orbital of O, the very small p<sub>π</sub> orbital of C, and the HOMO of R<sup>-</sup>, which are formed through the orbital mixing among the π and π\* orbitals of CO<sub>2</sub> and the HOMO of R<sup>-</sup>. As shown in Chart 4.4A, the HOMO of R<sup>-</sup> overlaps with the π\* orbital of CO<sub>2</sub> in a bonding way, into which the π orbital of CO<sub>2</sub> mixes in an anti-bonding way with the HOMO of R<sup>-</sup> because the former lies at a lower energy than the latter. This orbital mixing decreases the p<sub>π</sub> orbital of C but enhances the p<sub>π</sub> orbital of O, which leads to accumulation of electron density on the O atoms but a slight decrease of electron density on the C atom as we have seen in Figures 4.4A and 4.4B.

In the C<sub>2</sub>H<sub>4</sub> insertion, electron density accumulates on the C<sup>1</sup> atom but decreases on the C<sup>2</sup> atom (Figures 4.4C and 4.4D). This feature is explained in terms of the HOMO of the



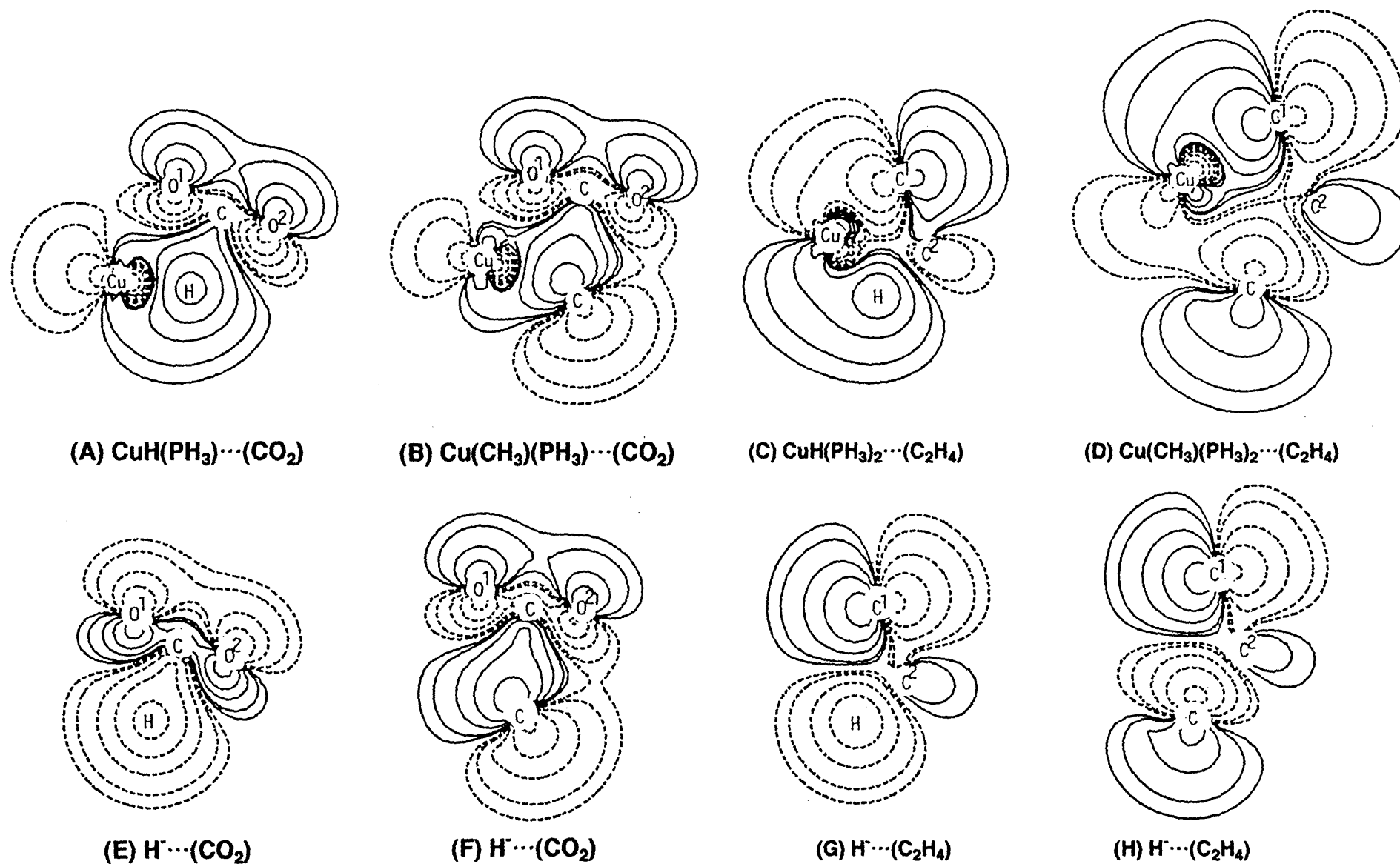
**Chart 4.4**

reaction system,  $\Psi_{\text{HOMO}}(\text{CuR}\cdots\text{C}_2\text{H}_4)$ , again. As shown in Figures 4.5C, 4.5D, 4.5G, and 4.5H, this HOMO resembles well the HOMO of the  $\text{C}_2\text{H}_4\cdots\text{R}^-$  system,  $\Psi_{\text{HOMO}}(\text{C}_2\text{H}_4\cdots\text{R}^-)$ . These HOMOs mainly consist of the large  $p_\pi$  orbital of  $\text{C}^1$ , the small  $p_\pi$  orbital of  $\text{C}^2$  and the HOMO of  $\text{R}^-$ , which are formed through the orbital mixing among the  $\pi$  and  $\pi^*$  orbitals of  $\text{C}_2\text{H}_4$  and the HOMO of  $\text{R}^-$ ; the HOMO of  $\text{R}^-$  overlaps with the  $\pi^*$  orbital of  $\text{C}_2\text{H}_4$  in a bonding way, into which the  $\pi$  orbital of  $\text{C}_2\text{H}_4$  mixes in an antibonding way with the HOMO of  $\text{R}^-$  because the former lies at lower energy than the latter, as shown in Chart 4.4B. This

orbital mixing enhances the C<sup>1</sup> p<sub>π</sub> orbital but decreases the C<sup>2</sup> p<sub>π</sub> orbital in  $\Psi_{\text{HOMO}}(\text{C}_2\text{H}_4\cdots\text{R}^-)$  and  $\Psi_{\text{HOMO}}(\text{CuR}\cdots\text{C}_2\text{H}_4)$ , which leads to an increase of electron density on the C<sup>1</sup> atom but a decrease of electron density on the C<sup>2</sup> atom.

Electron redistribution in the region between R and Sub (Sub = CO<sub>2</sub> or C<sub>2</sub>H<sub>4</sub>) is important for the insertion reaction. At the TS of the CO<sub>2</sub> insertion, electron density accumulates in this region (Figures 4.4A and 4.4B). Actually, the considerable C-R bonding overlap between CO<sub>2</sub> and CuR(PH<sub>3</sub>)<sub>2</sub> is observed in  $\Psi_{\text{HOMO}}(\text{CuR}\cdots\text{CO}_2)$  (Figures 4.5A and 4.5B). At the TS of the C<sub>2</sub>H<sub>4</sub> insertion, on the other hand, electron density decreases in this region (Figures 4.4C and 4.4D). Because  $\Psi_{\text{HOMO}}(\text{CuR}\cdots\text{C}_2\text{H}_4)$  involves the considerable C<sup>2</sup>-R bonding overlap between C<sub>2</sub>H<sub>4</sub> and CuR(PH<sub>3</sub>)<sub>2</sub> like it in the CO<sub>2</sub> insertion (Figure 4.5), the decrease in the density arises not from  $\Psi_{\text{HOMO}}(\text{CuR}\cdots\text{C}_2\text{H}_4)$  but from the other interaction, i.e., exchange repulsion between the π orbital of C<sub>2</sub>H<sub>4</sub> and the HOMO of R. Approach of C<sub>2</sub>H<sub>4</sub> to R would be difficult due to this strong exchange repulsion, which disfavors the C<sub>2</sub>H<sub>4</sub> insertion into the Cu-R bond and leads to the high activation energy. In the case of the CO<sub>2</sub> insertion, this kind of exchange repulsion would be small because the π orbital of CO<sub>2</sub> lies at considerably low in energy (-19.37 eV) than it of C<sub>2</sub>H<sub>4</sub> (-9.63 eV).<sup>51</sup> Accordingly, the C<sub>2</sub>H<sub>4</sub> insertion requires a higher activation energy than the CO<sub>2</sub> insertion.

Finally, an interaction between Cu and Sub will be investigated. At the TS of the CO<sub>2</sub> insertion, electron density decreases in the region between Cu and O<sup>1</sup> atoms (Figures 4.4A and 4.4B). At the TS of the C<sub>2</sub>H<sub>4</sub> insertion, on the other hand, electron density increases in this region.



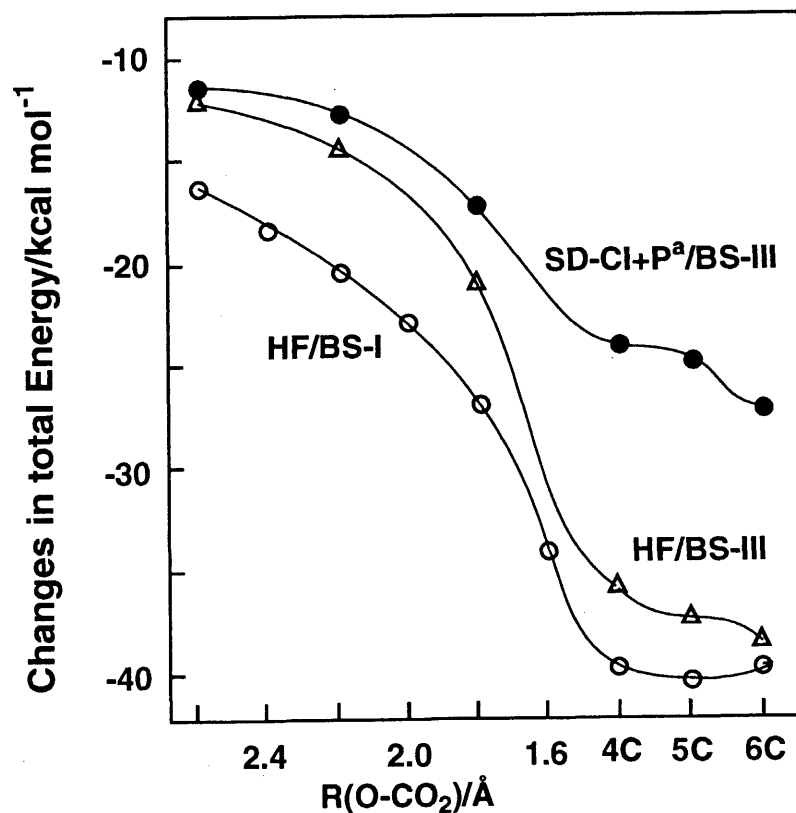
**Figure 4.5** Contour maps at the HOMOs of (A)  $[\text{CuH}(\text{PH}_3)\cdots(\text{CO}_2)]$ , **3A**, (B)  $[\text{Cu}(\text{CH}_3)(\text{PH}_3)\cdots(\text{CO}_2)]$ , **3B**, (C)  $[\text{CuH}(\text{PH}_3)_2\cdots(\text{CO}_2)]$ , **9A**, (D)  $[\text{Cu}(\text{CH}_3)(\text{PH}_3)_2\cdots(\text{CO}_2)]$ , **9B**. (E)  $\text{CO}_2\cdots\text{H}^-$ , (F)  $\text{CO}_2\cdots\text{CH}_3^-$ , (G)  $\text{C}_2\text{H}_4\cdots\text{H}^-$ , (H)  $\text{C}_2\text{H}_4\cdots\text{CH}_3^-$ . Contour values are  $\pm 0.2$ ,  $\pm 0.1$ ,  $\pm 0.05$ ,  $\pm 0.02$ , and  $\pm 0.01$ .

Consistent with this result,  $\Psi_{\text{HOMO}}(\text{CuR}\cdots\text{C}_2\text{H}_4)$  at the TS of the  $\text{C}_2\text{H}_4$  insertion involves a strong bonding interaction between Cu and  $\text{C}^1$  atoms (Figures 4.5C and 4.5D), while  $\Psi_{\text{HOMO}}(\text{CuR}\cdots\text{CO}_2)$  at the TS of the  $\text{CO}_2$  insertion involves an apparently weaker bonding interaction between Cu and  $\text{O}^1$  atoms than that between Cu and  $\text{C}^1$  atoms in  $\Psi_{\text{HOMO}}(\text{CuR}\cdots\text{C}_2\text{H}_4)$  (Figures 4.5A and 4.5B). All these results are consistent with the TS structure in which the Cu- $\text{C}^1$  distance is short at the TS of the  $\text{C}_2\text{H}_4$  insertion but the Cu- $\text{O}^1$  distance is long at the TS of the  $\text{CO}_2$  insertion. The short Cu- $\text{C}^1$  and the long Cu- $\text{O}^1$  distances are explained in terms of HOMOs,  $\Psi_{\text{HOMO}}(\text{C}_2\text{H}_4\cdots\text{R}^-)$  and  $\Psi_{\text{HOMO}}(\text{CO}_2\cdots\text{R}^-)$ . These HOMOs (Figure 4.5) are calculated to be -2.61 eV for  $\text{CO}_2\cdots\text{H}^-$ , -2.52 eV for  $\text{CO}_2\cdots\text{CH}_3^-$ , 0.56 eV for  $\text{C}_2\text{H}_4\cdots\text{H}^-$ , and 0.07 eV for  $\text{C}_2\text{H}_4\cdots\text{CH}_3^-$ , where geometries are taken to be the same as those in the TS. This means that approach of  $\text{R}^-$  to  $\text{C}_2\text{H}_4$  yields the HOMO at a considerably high energy but approach of  $\text{R}^-$  to  $\text{CO}_2$  yields the HOMO at a rather low energy; Accordingly,  $\Psi_{\text{HOMO}}(\text{C}_2\text{H}_4\cdots\text{R}^-)$  can form much stronger charge transfer interaction with Cu than does  $\Psi_{\text{HOMO}}(\text{CO}_2\cdots\text{R}^-)$ , leading to the short Cu- $\text{C}^1$  distance at the TS of the  $\text{C}_2\text{H}_4$  insertion. The Cu- $\text{O}^1$  distance is, however, rather long at the TS because the charge-transfer from  $\Psi_{\text{HOMO}}(\text{CO}_2\cdots\text{R}^-)$  to Cu is not strong very much.

#### **4-3-5 $\text{CO}_2$ Insertion Reaction into the Cu-OH Bond of $\text{Cu}(\text{OH})(\text{PH}_3)_2$**

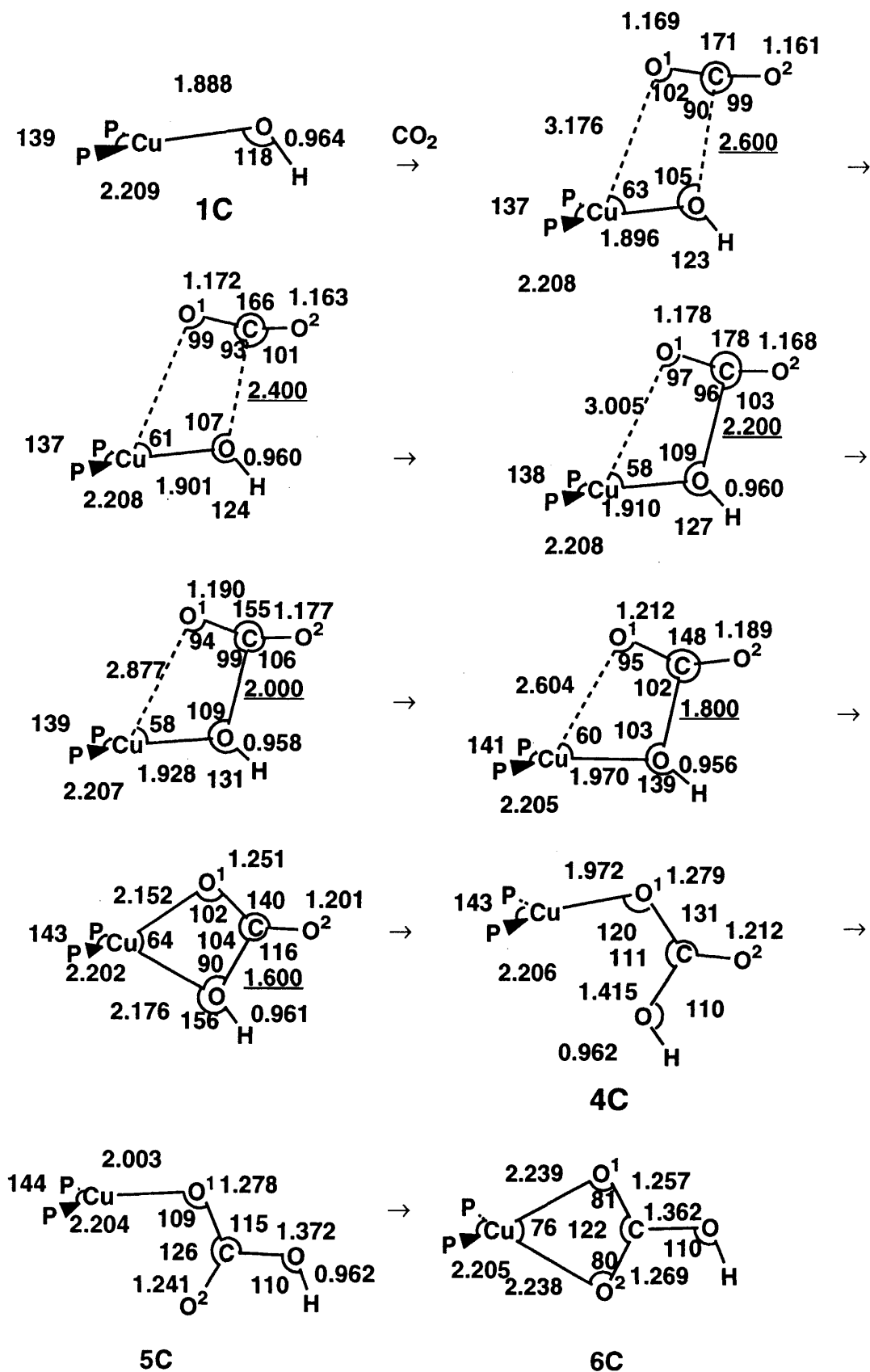
Interestingly, the  $\text{CO}_2$  insertion into the Cu-OH bond proceeds with no barrier, as clearly shown in Figure 4.6. Following geometry changes are observed (Figure 4.7); the Cu-OH distance is getting longer, the Cu- $\text{O}^1$  distance is getting

shorter, and the  $\angle O^1CO^2$  angle gradually closes. All these results represent that the Cu-OH bond is gradually broken and the Cu-O<sup>1</sup> bond is gradually formed, and the Cu-OC(O)OH bond is smoothly produced. The geometry at the late stage of this reaction is very close to that of the product, Cu( $\eta^1$ -OCOH)(PH<sub>3</sub>)<sub>2</sub> **4C** (see the geometry at R(O-CO<sub>2</sub>) = 1.6 Å). After the insertion, **4C** converts to **5C** with very small barrier (ca. 2.6 kcal/mol at the MP2/BS III level), and **5C** converts to the final product, Cu( $\eta^2$ -O<sub>2</sub>COH)(PH<sub>3</sub>)<sub>2</sub> **6C**, with no barrier (Figure 4.6).



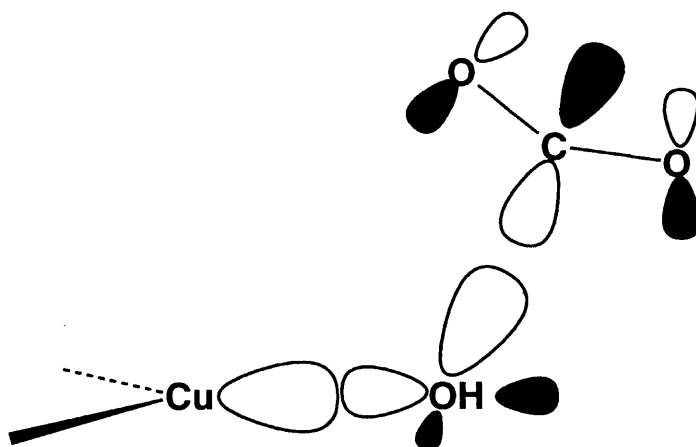
**Figure 4.6** Changes in total energy caused by the CO<sub>2</sub> insertion into the Cu-OH bond of Cu(OH)(PH<sub>3</sub>)<sub>2</sub> **1C**.  
 a) P = Pople's higher order excitaton correction.

Unexpectedly, the exothermicity of this insertion (27.1



(Continued to be the next page)

**Figure 4.7** Changes in geometry caused by the  $\text{CO}_2$  insertion into the  $\text{Cu-OH}$  bond of  $\text{Cu(OH)(PH}_3)_2$  **1C**. Bond distance in Å and bond angle in degree.



### Chart 4.5

kcal/mol for **6c** (SD-CI(P)/BS III) is calculated to be much smaller than that of the CO<sub>2</sub> insertion into Cu-H and Cu-CH<sub>3</sub> bonds, whereas CO<sub>2</sub> can insert into the Cu-OH with no barrier. The exothermicity of this insertion is approximately represented by eq 4.13,<sup>50</sup> The HO-C(O)OH bond energy is

$$\begin{aligned}
 E_{\text{exo}} &= E(\text{Cu-OC(O)OH}) + E(\text{C-O}) + E(\text{HO-C(O)OH}) \\
 &\quad - E(\text{Cu-OH}) - E(\text{C=O}) \\
 &= E(\text{Cu-OC(O)OH}) + \{E(\text{C-O}) - E(\text{C=O})\} \\
 &\quad + E(\text{HO-C(O)OH}) - E(\text{Cu-OH}) \quad (4.13)
 \end{aligned}$$

estimated to be 87 kcal/mol, only slightly smaller than the C-C(O)OH bond energy (92 kcal/mol) (Table 4.4). On the other hand, the term of  $E(\text{Cu-OC(O)OH}) - E(\text{Cu-OH})$  is calculated to be 29 kcal/mol, much smaller than the term of  $E(\text{Cu-OC(O)R}) - E(\text{Cu-R})$ , as shown in Table 4.4. Consequently, this insertion is less exothermic than the CO<sub>2</sub> insertion into the Cu-H and Cu-CH<sub>3</sub> bonds.



No activation energy of this insertion can be interpreted in terms of the HOMO of  $\text{Cu}(\text{OH})(\text{PH}_3)_2$  **1C**. Unlike the HOMOs of **1A** and **1B**, the HOMO of **1C** mainly consists of a lone-pair type orbital of  $\text{OH}^-$  which is not used for a coordinate bond with Cu (Chart 4.5). As a result, the LUMO of  $\text{CO}_2$  can easily interact with this orbital. This means that the bonding interaction between  $\text{CO}_2$  and OH is formed without weakening the Cu-OH bond. On the other hand, both H and  $\text{CH}_3$  ligands have only one valence orbital which is used for bonding with Cu in **1A** and **1B**. Accordingly, the  $\text{CO}_2$  insertion into the Cu-H bond weakens the Cu-H bond even though the 1s valence orbital of H is spherical, and the  $\text{CO}_2$  insertion into the Cu- $\text{CH}_3$  bond considerably weakens the Cu- $\text{CH}_3$  bond because of the directional  $\text{sp}^3$  valence orbital of  $\text{CH}_3$ . Thus, the  $\text{CO}_2$  insertion into the Cu-OH bond more easily occurs than the  $\text{CO}_2$  insertion into the Cu-H and Cu- $\text{CH}_3$  bonds.

#### 4.4 Conclusions

Ab initio MO/MP4, SD-CI, and CCD calculations are carried out on the insertion reactions of  $\text{CO}_2$  and  $\text{C}_2\text{H}_4$  into the Cu-R bond ( $\text{R}=\text{H}$ ,  $\text{CH}_3$ , and OH). The activation energy ( $E_a$ ) is calculated to be very low (ca. 4 - 5 kcal/mol) for the  $\text{CO}_2$  insertion, relatively high (9 - 10 kcal/mol) for the  $\text{C}_2\text{H}_4$  insertion into the Cu-H bond, and very high (23 - 30 kcal/mol) for the  $\text{C}_2\text{H}_4$  insertion into the Cu- $\text{CH}_3$  bond. These results suggest that the  $\text{C}_2\text{H}_4$  insertion into the Cu-R bond is more difficult than the  $\text{CO}_2$  insertion into the Cu-R bond. The difference of  $E_a$  between  $\text{CO}_2$  and  $\text{C}_2\text{H}_4$  insertion reactions can be interpreted in terms of the exchange repulsion between R and Sub (Sub =  $\text{CO}_2$  or  $\text{C}_2\text{H}_4$ ); because the  $\pi$  orbital of  $\text{C}_2\text{H}_4$  lies

higher in energy than that of  $\text{CO}_2$ , the exchange repulsion between  $\text{C}_2\text{H}_4$  and R is much larger than that between  $\text{CO}_2$  and R, leading to the higher  $E_a$  value of the  $\text{C}_2\text{H}_4$  insertion. The exothermicity of the  $\text{CO}_2$  insertion is much greater than that of the  $\text{C}_2\text{H}_4$  insertion. The main reason for the greater exothermicity of the  $\text{CO}_2$  insertion is that  $E(\text{Cu-OC(O)H})$  is larger than  $E(\text{Cu-C}_2\text{H}_5)$  and  $E(\text{Cu-CH}_3)$  by ca. 50 kcal/mol. The  $\text{CO}_2$  insertion into the Cu-OH bond proceeds with no barrier. This is because the HOMO of  $\text{Cu(OH)(PH}_3)_2$  is mainly consists of the lone-pair type orbital of  $\text{OH}^-$  and the bonding interaction between  $\text{CO}_2$  and OH can be formed without weakening of the Cu-OH bond. However, the  $E_{\text{exo}}$  of this insertion is smaller than that of the other  $\text{CO}_2$  insertion, since the Cu-OC(O)OH bond energy is about 29 kcal/mol larger than the Cu-OH bond energy (remember that Cu-OC(O)R bond energy is about 50 kcal/mol larger than the Cu- $\text{CH}_3$  bond energy).

From these results, one can predict a primarily important factor for the  $\text{CO}_2$  insertion that the presence of a lone-pair type orbital of R which is not used for coordination to Cu in the  $\text{CO}_2$  insertion. When the R ligand possesses such a lone-pair type orbital, the bonding interaction between this lone-pair type orbital and the LUMO of  $\text{CO}_2$  can be formed without weakening of the Cu-OH bond. This situation facilitates the  $\text{CO}_2$  insertion into the Cu-OH bond.

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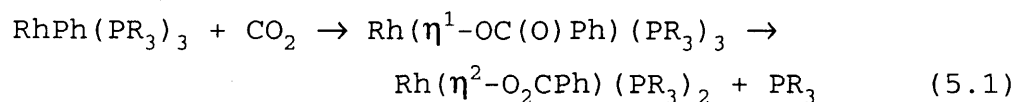
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- (51) Geometries of  $\text{CO}_2$  and  $\text{C}_2\text{H}_4$  were taken to be the same as the distorted structures like in the TSS of their insertion reactions into the Cu-H bond.

## CO<sub>2</sub> Insertion Into a Rh(I)-H Bond

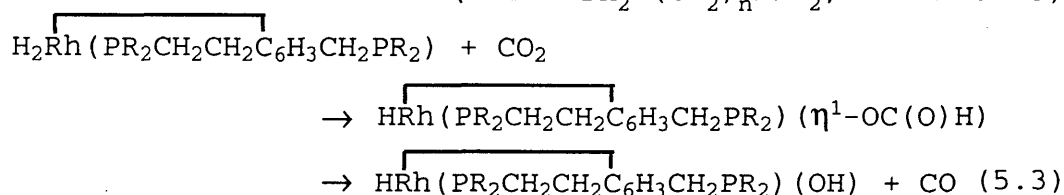
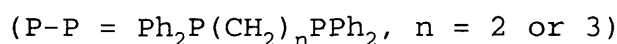
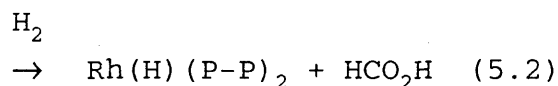
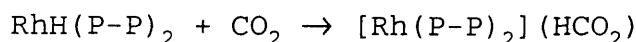
### 5.1 Introduction

Because insertion reactions of alkene, alkyne, and CO into M-H and M-R bonds are involved as key elementary processes in various catalytic cycles by transition metal complexes,<sup>1</sup> the insertion reaction of CO<sub>2</sub> into M-H and M-R bonds is believed to be of significant importance in transition-metal catalyzed CO<sub>2</sub> conversion into useful chemicals.<sup>2</sup> In this context, detailed knowledge of the insertion reaction of CO<sub>2</sub> is necessary to understanding well the catalytic CO<sub>2</sub> conversion and making its further development. To obtain such knowledge, not only experimental works but also theoretical works should be carried out on the CO<sub>2</sub> insertion because theoretical works can offer meaningful information of changes in geometry, transition state, bonding nature, electron distribution, activation energy etc. However, only a few MO studies have been reported on the insertion reactions of CO<sub>2</sub> into Cu(I)-R (R = H or CH<sub>3</sub>)<sup>3</sup> and Cr(0)-H bonds.<sup>4</sup>

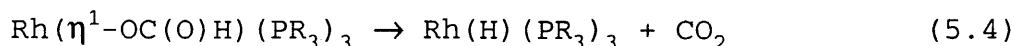
Besides insertion reactions of CO<sub>2</sub> into the Cu(I)-R and Cr(0)-H bonds, the CO<sub>2</sub> insertion reaction into the Rh-R bond (R = H, CH<sub>3</sub>, or Ph) is considered to be important because Rh complexes perform various catalytic reactions.<sup>1</sup> So far several rhodium hydride and rhodium alkyl complexes have been reported to undergo the CO<sub>2</sub> insertion. For instance, CO<sub>2</sub> reacts with RhPh(PR<sub>3</sub>)<sub>3</sub>, yielding Rh( $\eta^1$ -OC(O)Ph)(PR<sub>3</sub>)<sub>3</sub> and Rh( $\eta^2$ -O<sub>2</sub>CPh)(PH<sub>3</sub>)<sub>2</sub> (eq 5.1).<sup>5</sup> Similar insertion reactions of



$\text{CO}_2$  into Rh(I)-H and Rh(III)-H bonds are involved as key processes in catalytic hydrogenation of  $\text{CO}_2$  to formic acid (eq 5.2)<sup>6,7</sup> and catalytic reduction of  $\text{CO}_2$  to CO (eq 5.3)<sup>8</sup>

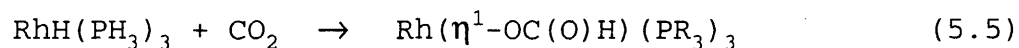


$\text{CO}_2$  into Rh(I)-H and Also, the reverse reaction of the  $\text{CO}_2$  insertion (eq 5.4) has been reported as a key process of the



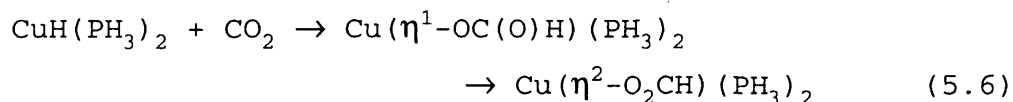
decomposition of formic acid.<sup>9</sup> From these reactions, we can expect that rhodium complexes serve as an efficient catalyst for the  $\text{CO}_2$  conversion into useful chemicals. Thus, there is a considerable need to investigate theoretically the  $\text{CO}_2$  insertion into the Rh-R bond.

In the present chapter, the insertion reaction of  $\text{CO}_2$  into the Rh(I)-H bond of  $\text{RhH}(\text{PH}_3)_3$  (eq 5.5) is investigated



with ab initio MO/MP4, SD-CI and coupled cluster methods. This reaction (eq 5.5) is selected here as a model of eqs 5.1 and 5.4. Purposes in this chapter are (1) to present detailed understanding of this insertion reaction, (2) to evaluate theoretically the activation energy and the energy of reaction, and (3) to compare this insertion reaction with

a similar insertion reaction of CO<sub>2</sub> into the Cu(I)-H bond (see, chapter 4).<sup>3</sup> Through this investigation, we hope to



clarify differences between Cu(I) and Rh(I) in the CO<sub>2</sub> insertion reaction.

## 5.2 Computational Details

Ab Initio MO/MP4SDQ, SD-CI and coupled cluster with double excitations (CCD) calculations were carried out by means of Gaussian 86<sup>10</sup> and 92<sup>11</sup> programs, using several kinds of basis sets (BS). In the BS I, core electrons (up to 4p) of Rh were replaced with Hay-Wadt's effective core potentials (ECP1), and valence orbitals (4d, 5s and 5p) were represented with a (3s 3p 4d)/[2s 2p 2d] set.<sup>12</sup> For C and O, MIDI-3 sets were adopted,<sup>13</sup> while STO-2G was used for PH<sub>3</sub>.<sup>14</sup> A (4s)/[2s] basis set<sup>15</sup> was employed for the active H atom that coordinated to Rh first and then reacted with CO<sub>2</sub>. In the BS II, valence orbitals of Rh were represented with almost the same basis set (3s 3p 4d)/[2s 2p 3d] as in the BS I, and the ECP1 was used for core electrons (up to 4p) of Rh.<sup>12</sup> MIDI-4<sup>13</sup> sets were used for C, O and P, and the (4s)/[2s] set<sup>15</sup> was employed for H. Only for the active H atom, a p-polarization function ( $\zeta = 1.0$ ) was added.<sup>15</sup> In the BS III, core electrons (up to 3d) were replaced with Hay-Wadt's effective core potentials (ECP2), and valence orbitals (4s, 4p, 4d, 5s and 5p) were represented with a (5s 5p 4d)/[3s 3p 3d] set.<sup>16</sup> For H, C, O and P, the same basis sets as those of the BS II were adopted. In the BS IV, not ECP but an all electron basis set (16s 12p 8d)/[6s 5

p 4d] was used for Rh,<sup>13</sup> where two p primitive functions<sup>13</sup> and one d primitive function ( $\zeta = 0.08$ )<sup>17</sup> were added to represent well valence 5p and 4d orbitals respectively. In the BS V, (9s 5p)/[3s 2p] sets were adopted for C and O,<sup>16</sup> while the same basis sets as those in the BS IV were used for the other atoms.

Geometries of reactants, transition state (TS) and products were optimized at the Hartree-Fock (HF) level with the energy gradient technique, using the BS I,<sup>18</sup> where the geometry of PH<sub>3</sub> was taken to be the same as the experimental structure of a free PH<sub>3</sub> molecule.<sup>19,20</sup> The TS was determined by evaluating the hessian matrix. MP2 ~ MP4SDQ, SD-CI and CCD calculations were carried out with all core orbitals excluded from an active space. In SD-CI calculations, contributions from higher order excited configurations were estimated, according to Davidson-Silver<sup>21</sup> and Pople et al.<sup>22</sup> In the CCD calculations, the contribution of single and triple excitations were evaluated through forth order using double excitation wave functions. Instability of HF wave functions<sup>23</sup> was not observed for all the reactants, TS, and product.<sup>24</sup> Because solvent effects were not considered here, the present computations are meaningful because CO<sub>2</sub> insertion into Rh(I)-H bond of RhH(PH<sub>3</sub>)<sub>3</sub> was carried out in non-polar solvent.<sup>5,8</sup>

In order to investigate bonding nature at the TS, we carried out energy decomposition analysis proposed by Morokuma et al.<sup>25</sup> In this analysis, the interaction energy (INT) is defined as the stabilization energy of the reaction system relative to reactants, CO<sub>2</sub> and RhH(PH<sub>3</sub>)<sub>3</sub>, taking the distorted structures like in the TS (see eq 5.7). The

deformation energy (DEF) is defined as the destabilization energy which is necessary to distort  $\text{CO}_2$  and  $\text{RhH}(\text{PH}_3)_3$  from their equilibrium structures to their distorted ones taken in the TS (see eq 5.8);

$$\text{INT} = E_t[\text{RhH}(\text{PH}_3)_3 \bullet \bullet \bullet \text{CO}_2]_{\text{TS}} - E_t[\text{RhH}(\text{PH}_3)_3]_{\text{dist}} - E_t(\text{CO}_2)_{\text{dist}} \quad (5.7)$$

$$\text{DEF} = E_t[\text{RhH}(\text{PH}_3)_3]_{\text{dist}} - E_t[\text{RhH}(\text{PH}_3)_3]_{\text{eq}} + E_t(\text{CO}_2)_{\text{dist}} - E_t(\text{CO}_2)_{\text{eq}} \quad (5.8)$$

The sum of INT and DEF corresponds to the activation energy ( $E_a$ ) relative to reactants (eq 5.9). INT is further divided into several chemically meaningful terms, as shown in eq

$$\begin{aligned} E_a &= \text{INT} + \text{DEF} \\ &= E_t[\text{RhH}(\text{PH}_3)_3 \bullet \bullet \bullet \text{CO}_2]_{\text{TS}} - E_t[\text{RhH}(\text{PH}_3)_3]_{\text{eq}} - E_t(\text{CO}_2)_{\text{eq}} \end{aligned} \quad (5.9)$$

$$\begin{aligned} \text{INT} &= \text{ES} + \text{EX} + \text{CTPLXA} (\text{RhH}(\text{PH}_3)_3 \rightarrow \text{CO}_2) \\ &\quad + \text{CTPLXB} (\text{CO}_2 \rightarrow \text{RhH}(\text{PH}_3)_3) + \text{R} \end{aligned} \quad (5.10)$$

5.10. ES is the electrostatic term arising from the coulombic interaction between  $\text{RhH}(\text{PH}_3)_3$  and  $\text{CO}_2$ . EX is the exchange repulsion due to Pauli exclusion principle. CTPLXA consists of the charge-transfer from  $\text{RhH}(\text{PH}_3)_3$  to  $\text{CO}_2$ , the polarization of  $\text{CO}_2$ , and their coupling terms. CTPLXB consists of the charge-transfer from  $\text{CO}_2$  to  $\text{RhH}(\text{PH}_3)_3$ , the polarization of  $\text{RhH}(\text{PH}_3)_3$  and their coupling terms. R is a higher order coupling term. From the definition, a negative value means stabilization in energy for all these terms. Although this analysis is based on the HF approximation,<sup>25</sup> bonding nature of the TS is expected to be successfully investigated with this analysis because the activation energy of this insertion reaction is not influenced very much by electron correlation, as will be described below.

The IMSPAC program was used for this analysis.<sup>26</sup>

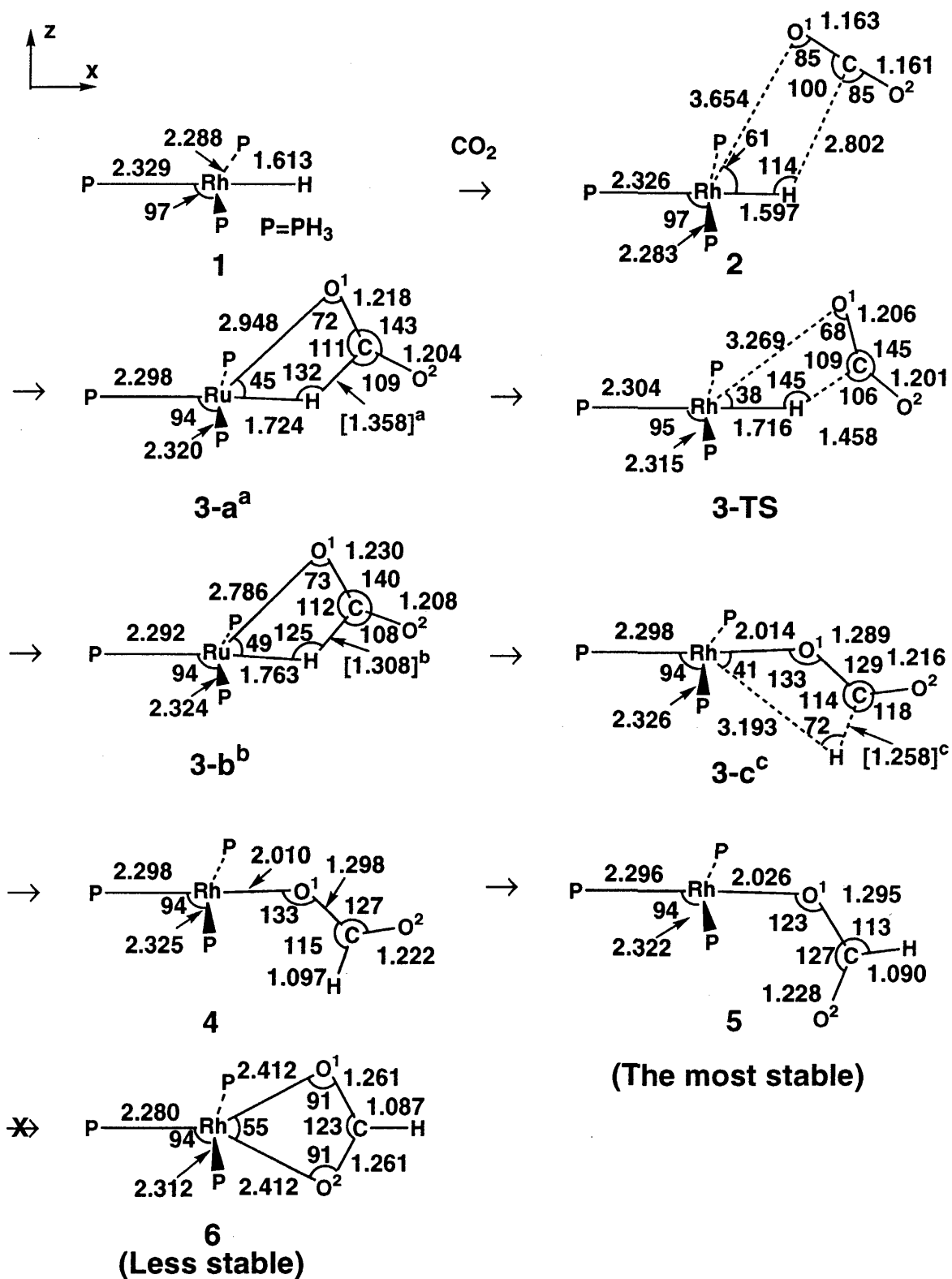
### 5.3 Results and Discussion

#### 5-3-1 Geometries of Precursor Complex, Transition State and Product

In many catalytic reactions by transition metal complexes, a substrate first coordinates to (or interacts with) a transition metal complex, to form a precursor complex before reaching the TS. We will mention the precursor complex, first. In the precursor complex (**2** in Figure 5.1), CO<sub>2</sub> is considerably distant from Rh, and both RhH(PH<sub>3</sub>)<sub>3</sub> and CO<sub>2</sub> parts little distort (compare **2** with **1**), suggesting that an interaction between Rh and CO<sub>2</sub> is very weak (vide infra). These features are also observed in the insertion reaction of CO<sub>2</sub> into the Cu(I)-H bond as described in chapter 4.<sup>27,28</sup> When a substrate strongly coordinates to Rh(I), the precursor complex is a d<sup>8</sup> five-coordinate system.

In such a case, there are many possible isomers including trigonal bipyramidal and square pyramidal structures, and the reaction course of the CO<sub>2</sub> insertion is much complicated in the trigonal bipyramidal structure, as has been theoretically investigated in the insertion reaction of ethene into the Rh(I)-H bond of RhH(CO)<sub>2</sub>(PH<sub>3</sub>)(C<sub>2</sub>H<sub>4</sub>).<sup>29</sup> In the present case, however, we do not need to consider a five-coordinate trigonal bipyramidal structure because the interaction between CO<sub>2</sub> and Rh(I) is very weak.

In the transition state (TS), the C-H distance between RhH(PH<sub>3</sub>)<sub>3</sub> and CO<sub>2</sub> is 1.46 Å, the Rh-H distance slightly lengthens by only 0.12 Å and the H ligand barely moves downward from the RhP<sub>3</sub> plane (see **3-TS** of Figure 5.1).<sup>30</sup>



**Figure 5.1** Geometry changes in the CO<sub>2</sub> insertion into a Rh(I)-H bond of RhH(PH<sub>3</sub>)<sub>3</sub>. Bond distance in Å and bond angle in degree. a), b), and c) The geometry was optimized under assumption that R(C-H) was 1.358, 1.308, and 1.258 Å for a), b), and c), respectively.



These geometrical features of the TS are common in both insertion reactions of CO<sub>2</sub> into Rh(I)-H and Cu(I)-H bonds.<sup>3b,27,31</sup> Interesting differences are, however, observed between them; the C-H distance (1.46 Å) between CO<sub>2</sub> and RhH(PH<sub>3</sub>)<sub>3</sub> is shorter than that (1.68 Å) of the Cu reaction system, indicating that the TS of the Rh reaction system is more product-like than that of the Cu reaction system. Nevertheless, the Rh(I)-O<sup>1</sup> distance (3.27 Å) is much longer than the Cu(I)-O<sup>1</sup> distance (2.50 Å), and the RhHC angle (145°) is much larger than the CuHC angle (105°). The C-O<sup>1</sup> distance (1.21 Å) is almost equal to the C-O<sup>2</sup> distance (1.20 Å) in the Rh reaction system, while the C-O<sup>1</sup> distance (1.21 Å) is longer than the C-O<sup>2</sup> distance (1.18 Å) in the Cu reaction system. These differences indicate that the Cu-O<sup>1</sup> bond is partially formed but the Rh-O<sup>1</sup> bond is not formed yet at the TS. It should be, therefore, reasonably concluded that a four-center type interaction is hardly involved in the TS of the Rh reaction system but involved in the TS of the Cu reaction system.<sup>3b</sup>

Geometry changes after the TS were examined, shortening the C-H distance between CO<sub>2</sub> and RhH(PH<sub>3</sub>)<sub>3</sub> to 1.358 Å, 1.308 Å and 1.258 Å. The reaction system is getting similar to the product **4**, as the C-H distance is getting shorter (see **3-a**, **3-b** and **3-c** in Figure 5.1). This geometry change suggests that although a four-center type interaction is not formed at the TS, the CO<sub>2</sub> insertion yields the Rh-(η<sup>1</sup>-OC(O)H) species as the product.

In the product, there are three possible structures, as shown in Figure 5.1. **4** and **5** include a monodentate η<sup>1</sup>-formate ligand and **6** a bidentate η<sup>2</sup>-formate ligand. Of

them, **5** is the most stable, as will be discussed below.

In a recent experiment,<sup>6</sup> CO<sub>2</sub> reacts with a five-coordinate rhodium(I)-hydride complex, [RhH(P-P)<sub>2</sub>] (P-P = Ph<sub>2</sub>(CH<sub>2</sub>)<sub>n</sub>PPh<sub>2</sub>, n = 2 or 3), in DMSO, affording not a Rh-(η<sup>1</sup>-OC(O)H) species but [Rh(P-P)<sub>2</sub>](HCO<sub>2</sub>) in which formate exists as a counter anion (eq 5.2). This experimental result is consistent with the geometrical feature of the TS presented here; because the Rh-O<sup>1</sup> bond is hardly formed at the TS, the insertion reaction of CO<sub>2</sub> into the Rh(I)-H bond would not always yield a Rh-(η<sup>1</sup>-OC(O)H) species but yield a free formate anion when coordinating species (coordinating solvent, four phosphine ligands per Rh etc.) exist in the reaction system.

**Table 5.1** Basis set effects on the activation energy (E<sub>a</sub>) and the exothermicity (E<sub>exo</sub>) at the HF level for the CO<sub>2</sub> insertion into the Rh(I)-H bond of RhH(PH<sub>3</sub>)<sub>3</sub> (kcal/mol)

	BS I	BS II	BS III	BS IV	BS V
E <sub>a</sub> <sup>a</sup>	9.3	14.3	13.3	12.2	11.2
E <sub>exo</sub> <sup>b</sup>	42.5	37.3	34.9	37.3	38.2

a) E<sub>a</sub> = E<sub>t</sub>(TS) - E<sub>t</sub>(precursor, **2**).

b) E<sub>exo</sub> = E<sub>t</sub>(**1** + CO<sub>2</sub>) - E<sub>t</sub>(**5**).

### 5-3-2 Activation Energy (E<sub>a</sub>) and Exothermicity (E<sub>exo</sub>)

Prior to detailed discussion of E<sub>a</sub> and E<sub>exo</sub>, basis set effects on E<sub>a</sub> and E<sub>exo</sub> will be mentioned here, where E<sub>a</sub> is defined as an energy difference between the TS and the precursor complex **2**, and E<sub>exo</sub> is an energy difference between the final product **5** and the sum of reactants, **1** + CO<sub>2</sub>. As shown in Table 5.1, the BS I yields a smaller E<sub>a</sub> value and a

larger  $E_{\text{exo}}$  value than the others. On the other hand, the BS II yields a larger  $E_a$  value than the others (note ECP1 was employed in both BS I and BS II). Recently, use of ECP2 has been recommended for calculating energy change.<sup>32,33</sup> Also in our calculations of the  $\text{CO}_2$  insertion into the  $\text{Cu(I)}-\text{R}$  bond,<sup>27</sup> the BS II yielded much different  $E_{\text{exo}}$  value from the value calculated with the BS III. Thus, it is necessary to use the BS III or a better one in investigating the  $\text{CO}_2$  insertion into the  $\text{Rh(I)}-\text{H}$  bond. In the present work, the BS IV was mainly used, except that the BS III was used in comparing several computational methods at the correlated level.

Then we will examine electron correlation effects on the  $E_a$  and the energy of reaction ( $\Delta E$ ). As clearly shown in Table 5.2, introduction of electron correlation somewhat increases the  $E_a$  value, but considerably decreases the exothermicity (the negative  $\Delta E$  means the exothermicity). Thus, introduction of electron correlation is indispensable for quantitative estimation of  $E_a$  and  $\Delta E$ . The other important result to be noted is that MP2 and MP3 methods are not reliable in investigating the  $\text{CO}_2$  insertion, because  $E_a$  and  $\Delta E$  significantly fluctuate at MP2 and MP3 levels. On the other hand, MP4DQ, MP4SDQ, and SD-CI calculations yield similar  $E_a$  values, while the  $\Delta E$  values at the SD-CI level are a little bit larger than the value at the MP4SDQ level. In Table 5.3, we can also see that SD-CI and CCD calculations yield almost the same  $E_a$  value and that the  $E_{\text{exo}}$  value calculated at the CCD level is intermediate between  $E_{\text{exo}}$  values at MP4SDQ and SD-CI levels. Thus, the method of higher quality than MP4 should be applied to the present

**Table 5.2** Electron correlation effects on energy changes<sup>a</sup> by the CO<sub>2</sub> insertion into a Rh(I)-H bond

compd		HF	MP2	MP3	MP4		SDCI(DS) <sup>b</sup>	SDCI(P) <sup>c</sup>
					DQ	SDQ		
RhH(PH <sub>3</sub> ) <sub>2</sub> + CO <sub>2</sub>	<b>1</b> <sup>d</sup>	0.0 <sup>e</sup>	0.0 <sup>f</sup>	0.0 <sup>g</sup>	0.0 <sup>h</sup>	0.0 <sup>i</sup>	0.0 <sup>j</sup>	0.0 <sup>k</sup>
Precursor complex	<b>2</b>	-1.6	-3.3	-3.3	-3.1	-3.2	-3.4	-3.3
TS	<b>3-TS</b>	11.7	14.8	9.8	13.5	12.4	12.8	12.8
		(13.3)	(18.1)	(13.1)	(16.6)	(15.6)	(16.2)	(16.1)
Rh(η <sup>1</sup> -OC(O)H)(PH <sub>3</sub> ) <sub>3</sub>	<b>4</b>	-29.0	-1.0	-20.1	-11.3	-9.7	-16.2	-16.5
	<b>5</b>	-34.9	-6.7	-25.9	-17.0	-15.3	-22.0	-22.4
Rh(η <sup>2</sup> -O <sub>2</sub> CH)(PH <sub>3</sub> ) <sub>3</sub>	<b>6</b>	-21.7	2.5	-15.4	-6.8	-6.3	-	-

a) BS-III was used. b) Correction by Davidson and Silver for higher order excitations.<sup>20</sup> c) Correction by Pople et al. for higher order excitations.<sup>21</sup>

d) See Figure 5.1 for these numbers.

e) E<sub>t</sub>(HF) = -1322.6328. f) E<sub>t</sub>(MP2) = -1323.3920. g) E<sub>t</sub>(MP3) = -1323.3619.

h) E<sub>t</sub>(MP4DQ) = -1323.4118. i) E<sub>t</sub>(MP4SDQ) = -1323.4400. j) E<sub>t</sub>(SDCI(DS)) =

-1323.4231. k) E<sub>t</sub>(SDCI(P)) = -1323.4118 (hartree unit for all these total energies. l) In parentheses; energy difference between **2** and **3-TS**, which corresponds to the activation energy.

**Table 5.3** Stabilization energy of a precursor complex, BE, activation energy,  $E_a$ , and exothermicity,  $E_{exo}$ , of the  $\text{CO}_2$  insertion into  $\text{Rh(I)-H}$  and  $\text{Cu(I)-H}$  bonds (kcal/mol)<sup>a</sup>

	$\text{RhH}(\text{PH}_3)_3$			$\text{CuH}(\text{PH}_3)_2^{34}$		
	BE	$E_a^b$	$E_{exo}^b$	BE	$E_a^b$	$E_{exo}^b$
HF	1.5	12.2	-37.3	3.5	3.7	-51.4
MP4DQ	3.2	21.0	-17.8	4.5	5.9	-43.6
MP4SDQ	3.2	20.5	-15.6	4.4	7.1	-40.1
SDCI(DS)	3.5	15.7	-24.0	5.0	3.5	-39.4
SDCI(P)	3.5	15.6	-24.2	5.0	3.6	-39.7
CCD <sup>c</sup>	3.1	15.9	-18.7	---	---	---

a) The BS IV was used.  $E_t$  of  $\text{RhH}(\text{PH}_3)_2 + \text{CO}_2$  is -5896.1584 at HF, -5896.9380 at MP4DQ, -5896.9676 at MP4SDQ, -5896.9066 at SDCI(DS), -5896.8954 at SDCI(P), and -5898.9824 at CCD (hartree unit).  $E_t$  of  $\text{CuH}(\text{PH}_3)_2 + \text{CO}_2$  is -2509.2300 at HF, -2510.0240 at MP4DQ, -2510.0713 at MP4SDQ, -2510.0162 at SDCI(DS), and -2510.0057 at SDCI(P) (hartree unit).

b) See footnotes a) and b) of Table 1 for the definition.

c) The contribution of single and triple excited configurations is evaluated through double excited configurations.

study. The SD-CI method was mainly used in comparing the Rh reaction system with the Cu reaction system.

As given in Table 5.3, the stabilization energy (BE) of the precursor complex is very small at all computational levels adopted here. This small stabilization energy is consistent with the long Rh- $\text{CO}_2$  distance and the very small distortion of  $\text{RhH}(\text{PH}_3)_3$  and  $\text{CO}_2$  parts (vide supra). This is not surprising because a coordinate bond of  $\text{CO}_2$  with a transition metal is, in general, weak. The activation

energy was calculated to be ca. 12 kcal/mol at the HF level and ca. 16 kcal/mol at the SD-CI level (after correction of higher order excited configurations). This activation energy is considerably higher than that of the CO<sub>2</sub> insertion into the Cu(I)-H bond (3.5 kcal/mol).<sup>34</sup>

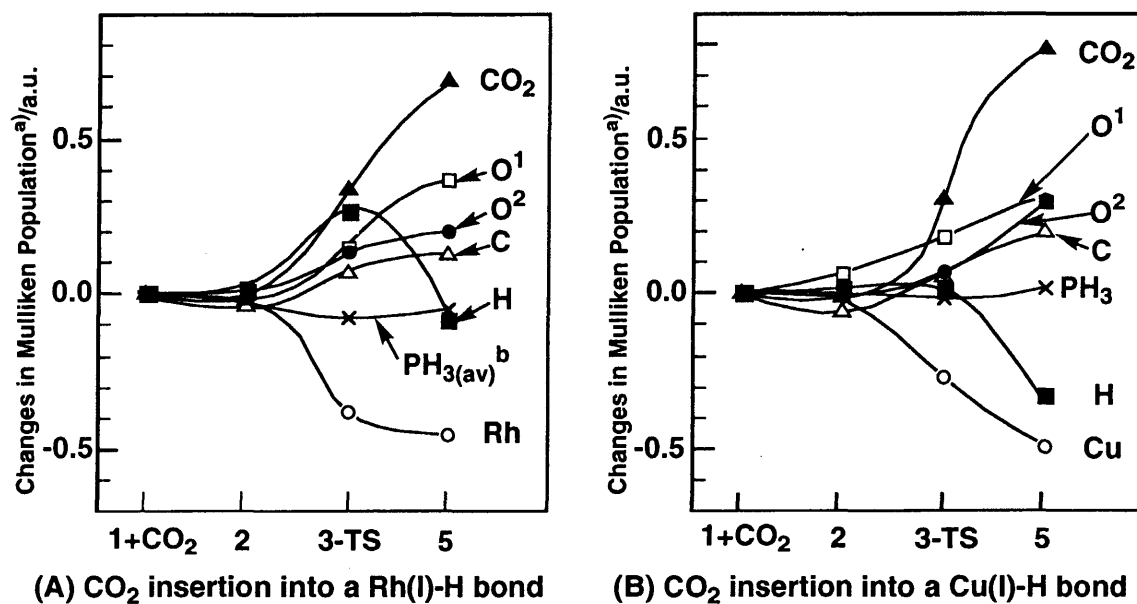
Before discussing the energy of reaction, we must examine the relative stabilities of the products. As shown in Table 5.2, **5** is the most stable, **4** is the next and **6** is the least stable at HF, MP2 - MP4SDQ and SD-CI levels. These relative stabilities differ from those of the products in the CO<sub>2</sub> insertion into the Cu(I)-H bond of CuH(PH<sub>3</sub>)<sub>2</sub>. This difference is easily interpreted in terms of the electron configurations of Rh(I) and Cu(I); Rh(I) prefers a four-coordinate square planar structure, **5**, to a five-coordinate pseudo-trigonal bipyramid structure, **6**, due to its d<sup>8</sup> electron configuration, whereas Cu(I) prefers a four-coordinate pseudo-tetrahedral structure due to its d<sup>10</sup> electron configuration. In a recent experiment of the CO<sub>2</sub> insertion into the Rh(I)-Ph bond of RhPh(PR<sub>3</sub>)<sub>3</sub>,<sup>5</sup> the η<sup>1</sup>-formate species is formed first and then it converts to the η<sup>2</sup>-formate species after one PR<sub>3</sub> ligand dissociates from Rh (eq 5.1). Our calculation is consistent with this experimental result.

For the Rh reaction system, the exothermicity is calculated to be 24 kcal/mol at the SD-CI level and 19 kcal/mol at the CCD level (Table 5.3). This value is much smaller than the exothermicity of the CO<sub>2</sub> insertion into the Cu(I)-H bond (ca. 40 kcal/mol).<sup>3b,34</sup> Comparing the E<sub>a</sub> and E<sub>exo</sub> values between Rh and Cu reaction systems, we can conclude that the CO<sub>2</sub> insertion into the Rh(I)-H bond occurs less

easily than the CO<sub>2</sub> insertion into the Cu(I)-H bond of CuH(PH<sub>3</sub>)<sub>2</sub>.

### 5-3-3 Electron Redistribution in the CO<sub>2</sub> Insertion and Bonding Interactions at the Transition State

Changes in Mulliken populations are shown in Figure 5.2, in which several interesting features are observed, as follows: (1) Electron population of CO<sub>2</sub> considerably increases, while Rh and Cu atomic populations remarkably decrease, indicating that the charge transfer from RhH(PH<sub>3</sub>)<sub>3</sub> to CO<sub>2</sub> is important in the CO<sub>2</sub> insertion. (2) The O<sup>1</sup> and O<sup>2</sup> atomic populations increase more than the C atomic population in both Rh and Cu reaction systems. This electron redistribution arises from the orbital mixing in which the  $\pi$  orbital of CO<sub>2</sub> mixes into the bonding overlap between the  $\pi^*$  orbital of CO<sub>2</sub> and HOMO of RhH(PH<sub>3</sub>)<sub>3</sub>. This kind of orbital mixing is in general observed in transition-metal CO<sub>2</sub> complexes and their reactions. Detailed explanation has been presented in our previous works<sup>3,35</sup> and is omitted here. (3) In the Rh reaction system, the H atomic population increases at the TS, unexpectedly. Because the electron population of CO<sub>2</sub> considerably increases at the TS, the increase in the H atomic population cannot be attributed to the charge-transfer from CO<sub>2</sub> to RhH(PH<sub>3</sub>)<sub>3</sub>. One plausible explanation is that the  $\delta^+$  charge on the C atom of CO<sub>2</sub> causes the polarization of RhH(PH<sub>3</sub>)<sub>3</sub> in which electrons are accumulated on the H ligand so as to strengthen the C <sup>$\delta^+$</sup> ...H <sup>$\delta^-$</sup>  coulombic interaction between CO<sub>2</sub> and RhH(PH<sub>3</sub>)<sub>3</sub>. In the Cu reaction system, on the other hand, the H atomic population



**Figure 5.2** Changes in Mulliken population<sup>a</sup> in the CO<sub>2</sub> insertion into a Rh(I)-H or Cu(I)-H bond.

a) A positive value means an increase in population. The infinite separation between CO<sub>2</sub> and RhH(PH<sub>3</sub>)<sub>3</sub> is taken to be the standard (change 0). The BS IV was used. b) The averaged value of three PH<sub>3</sub> ligands.

hardly increases at the TS (Figure 5.2B). This difference suggests that RhH(PH<sub>3</sub>)<sub>3</sub> is much more polarizable than CuH(PH<sub>3</sub>)<sub>2</sub>, which will be discussed below in more detail.

To inspect the bonding interaction at the TS, energy decomposition analysis was performed, as shown in Tables 5.4 and 5.5. The ES stabilization cannot overwhelm the EX repulsion, as is often found in the reactions of transition metal complexes.<sup>3b,36</sup> This means that the static interaction, which corresponds to the sum of ES and EX, is



**Table 5.4** Energy decomposition analysis of an interaction between CO<sub>2</sub> and MH(PH<sub>3</sub>)<sub>n</sub> (M = Cu or Rh, n = 2 or 3) at the transition state (TS) (kcal/mol)<sup>a</sup>

θ <sup>b</sup>	RhH(PH <sub>3</sub> ) <sub>3</sub> ···CO <sub>2</sub>		CuH(PH <sub>3</sub> ) <sub>2</sub> ···CO <sub>2</sub>	
	145°	106° <sup>c</sup>	145°	106° <sup>c</sup>
	(TS)		(TS)	
ΔE	10.6	23.1 (19.2) <sup>d</sup>	5.1	0.4
DET total	25.7	25.7 (25.7)	21.7	21.7
MH(PH <sub>3</sub> ) <sub>n</sub>	0.8	0.8 (0.8)	2.1	2.1
CO <sub>2</sub>	24.9	24.9 (24.9)	19.6	19.6
INT	-15.1	-2.6 (-6.5)	-16.6	-21.3
ES	-55.9	-103.6 (-63.0)	-47.5	-71.0
EX	106.5	189.3 (105.7)	70.5	101.7
CTPLXA				
(MH(PH <sub>3</sub> ) <sub>n</sub> →CO <sub>2</sub> )	-44.7	-59.3 (-35.2)	-28.6	-37.9
CTPLXB				
(CO <sub>2</sub> →MH(PH <sub>3</sub> ) <sub>n</sub> )	-13.8	-20.7 (-10.8)	-7.4	-8.9
R	-7.2	-8.4 (-3.2)	-3.6	-5.2

a) The BS IV was used. A positive value means destabilization in energy (vice versa). b) The MHC angle (see Figure 5.1).

c) The only θ angle (= the MHC angle) is changed with the geometry of the other part unchanged.

d) In parentheses; The C-H distance between CO<sub>2</sub> and RhH(PH<sub>3</sub>)<sub>3</sub> is lengthend to 1.678 Å which is the C-H distance in the TS of the Cu reaction system.

**Table 5.5** Partitioning of population changes<sup>a</sup> at the transition state

	RhH(PH <sub>3</sub> ) <sub>3</sub>				CuH(PH <sub>3</sub> ) <sub>2</sub>			
	Rh	H	PH <sub>3</sub> (av)	CO <sub>2</sub>	Cu	H	PH <sub>3</sub>	CO <sub>2</sub>
EX	0.013	-0.024	0.008	0.000	-0.014	0.013	0.001	0.000
CTPLXA	-0.152	-0.134	-0.014	0.329	-0.140	-0.163	0.000	0.303
CTPLXB	-0.425	0.476	-0.045	-0.023	-0.170	0.198	0.008	-0.038

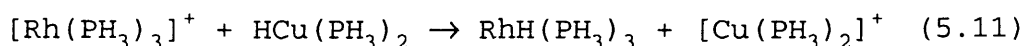
a) Difference from the population at the infinite separation between CO<sub>2</sub> and MH(PH<sub>3</sub>)<sub>n</sub> (M = Cu or Rh, n = 2 or 3). A positive value means an increase in the population (vice versa).

repulsive and the contribution from the CTPLXA and CTPLXB terms is necessary to stabilize the TS of the CO<sub>2</sub> insertion reaction. CTPLXA yields much greater stabilization than CTPLXB. This result is consistent with the electron redistribution discussed above, since the CTPLXA term includes the charge-transfer from RhH(PH<sub>3</sub>)<sub>3</sub> to CO<sub>2</sub> as a main contributor. Actually, the electron population of CO<sub>2</sub> increases but atomic populations of Rh and H decrease through this term (Table 5.5). Although the CTPLXB stabilization is small, its contribution cannot be neglected. The electron population of CO<sub>2</sub> is little decreased, the Rh atomic population is considerably decreased but the H atomic population is remarkably increased by this term (Table 5.5). These results indicate that the charge-transfer from CO<sub>2</sub> to RhH(PH<sub>3</sub>)<sub>3</sub> does not contribute to the CTPLXB term very much but the polarization of RhH(PH<sub>3</sub>)<sub>3</sub> considerably contributes to this term. In the Cu reaction system, the H atomic population increases

through this term to a much lesser extent than in the Rh reaction system (Table 5.5). This is because  $\text{CuH}(\text{PH}_3)_2$  is much less polarizable than  $\text{RhH}(\text{PH}_3)_3$ . The increase in the H atomic population through the CTPLXB term is almost compensated by its decrease through the CTPLXA term (Table 5.5). Thus, the H atomic population hardly changes at the TS of the Cu reaction system, as has been shown in Figure 5.2B.

#### 5-3-4 Differences Between $\text{RhH}(\text{PH}_3)_3$ and $\text{CuH}(\text{PH}_3)_2$ in the $\text{CO}_2$ Insertion Reaction

One of the great differences between these two reaction systems is that the  $\text{CO}_2$  insertion into the Rh(I)-H bond is much less exothermic than the insertion into the Cu(I)-H bond (Table 5.3). The exothermicity is mainly determined by bond energies. In the  $\text{CO}_2$  insertion into the M-H bond, the M-H bond is broken, while the M-OC(O)H and the H-C(O)OM bonds are formed. The formation of the H-C(O)OM bond is common in both insertion reactions of  $\text{CO}_2$  into the Rh(I)-H and Cu(I)-H bonds. Thus, the difference in exothermicity mainly arises from Rh(I)-H, Cu(I)-H, Rh(I)-( $\eta^1$ -OC(O)H) and Cu(I)-( $\eta^1$ -OC(O)H) bond energies. Considering the assumed



eq 5.10, we can estimate the difference between Rh(I)-H and Cu(I)-H bond energies, as shown in eq 5.11 where  $\Delta E_{r-1} =$

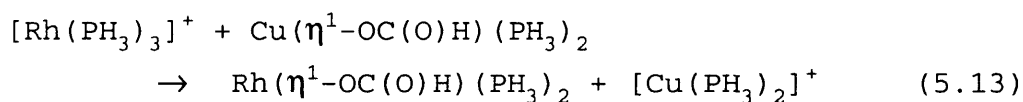
$$\Delta E_{r-1} = E(\text{Cu-H}) - E(\text{Rh-H}) \quad (5.12)$$

$E_t(\text{right hand side of eq 5.11}) - E_t(\text{left-hand side of eq 5.10})$ . Similarly, we can estimate the difference between Rh(I)-( $\eta^1$ -OC(O)H) and Cu(I)-( $\eta^1$ -OC(O)H) bond energies from the following assumed eq 5.11;

**Table 5.6** Differences in bond energies between Rh(I)-X and Cu(I)-X (X = H or  $\eta^1$ -OC(O)H) (kcal/mol)<sup>a</sup>

	E(Rh-H) -E(Cu-H)	E(Rh-OC(O)H) -E(Cu-OC(O)H)
MP2	37.2	9.2
MP3	29.6	8.1
MP4DQ	30.7	6.9
MP4SDQ	28.3	5.5

a) The BS IV was used.

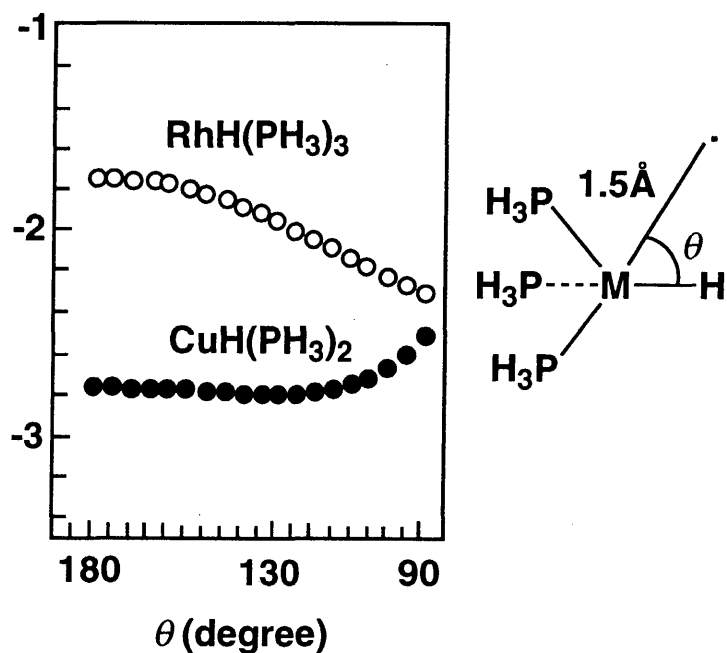


$$\Delta E_{r-1} = E(\text{Cu-OC(O)H}) - E(\text{Rh-OC(O)H}) \quad (5.14)$$

where geometries of  $[\text{Cu}(\text{PH}_3)_2]^+$  and  $[\text{Rh}(\text{PH}_3)_3]^+$  were optimized at the HF level, using the BS I. As shown in Table 5.6, E(Rh-H) is larger than E(Cu-H) by 28-31 kcal/mol at the MP4 level, while E(Rh-OC(O)H) is slightly larger than E(Cu-OC(O)H) by only 6-7 kcal/mol. In the Rh reaction system, therefore, the considerably stronger Rh(I)-H bond is broken but the only slightly stronger Rh(I)-( $\eta^1$ -OC(O)H) bond is formed than those in the Cu reaction system, which leads to the smaller exothermicity of the Rh reaction system than that of the Cu reaction system.

It should be also noted that the Rh reaction system requires the higher activation energy than the Cu reaction system. The interaction between  $\text{CO}_2$  and  $\text{MH}(\text{PH}_3)_n$  (M = Cu or Rh; n = 2 or 3) at the TS was investigated with energy

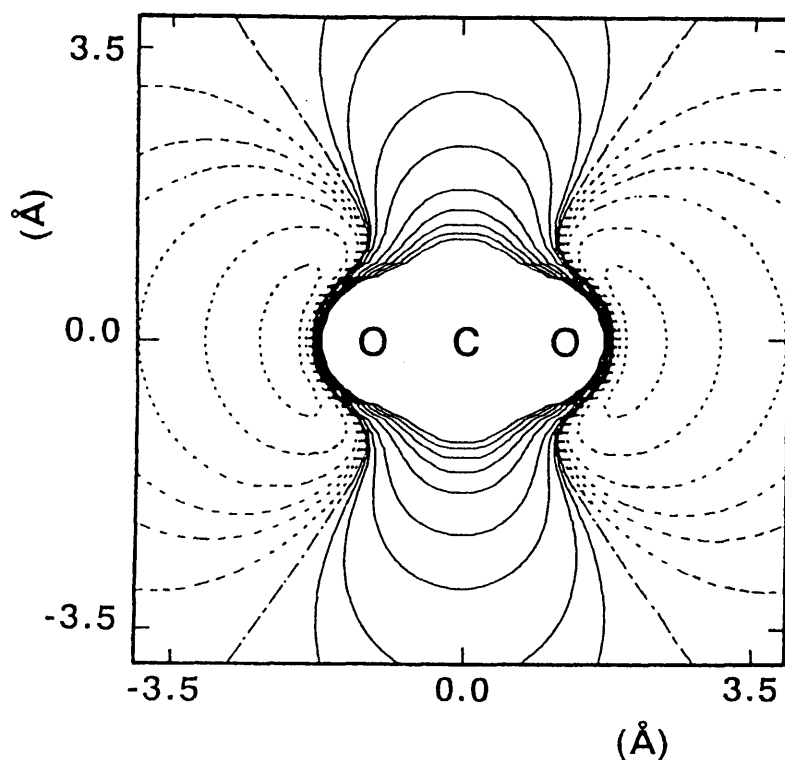
decomposition analysis (EDA), which was performed at  $\theta$  (the MHC angle) =  $145^\circ$  and  $105^\circ$ , one corresponding to the TS of the Rh reaction system and the other to the TS of the Cu reaction system. A clear reason for the higher activation energy of the Rh reaction system is not, however, found by comparing these two reaction systems at the same  $\theta$  value, because the Rh reaction system suffers greater destabilization from DEF and EX terms and greater stabilization from ES, CTPLXA and CTPLXB terms than the Cu reaction system (Table 5.4). To inspect the differences between two reaction systems, we carried out further EDA of the Rh reaction system in which the C-H distance and the RhHC angle were taken to be the same as those of the Cu reaction system (results are given in parentheses of Table 5.4). Comparing this assumed structure of the Rh reaction system with the TS of the Cu reaction system, the Rh reaction system suffers larger destabilization energies from the DEF and EX terms and receives a smaller stabilization energy from the ES term than the Cu reaction system. Thus, the higher activation energy of the former can be attributed to the larger DEF value, the smaller ES stabilization and the larger EX repulsion. The large DEF value is due to the large distortion of the CO<sub>2</sub> part (Table 5.4). In order to break the strong Rh(I)-H bond, CO<sub>2</sub> more strongly interacts with the H ligand in the TS of the Rh reaction system than in the TS of the Cu reaction system, which causes the larger distortion of the CO<sub>2</sub> part in the former than in the latter (Figure 5.1). Thus, the large DEF value of the Rh reaction system is related to the strong Rh(I)-H bond. The smaller ES stabilization is interpreted in terms of the



**Figure 5.3** Electrostatic potential of  $\text{RhH(PH}_3)_3$  and  $\text{CuH(PH}_3)_2$ .

a) A positive value means destabilization of positive charge. The BS IV set was used.

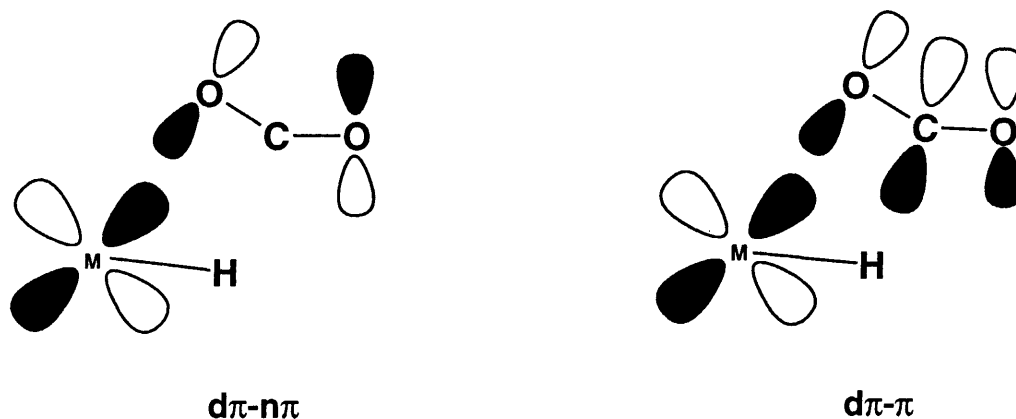
electrostatic potential. The electrostatic potentials of  $\text{RhH(PH}_3)_3$  and  $\text{CuH(PH}_3)_2$  are compared at the position  $1.5 \text{ \AA}$  distant from the H ligand (Figure 5.3). At both  $\theta = 105^\circ$  and  $145^\circ$ , the electrostatic potential of  $\text{CuH(PH}_3)_2$  is more negative than that of  $\text{RhH(PH}_3)_3$ , probably because the H ligand is more negatively charged in  $\text{CuH(PH}_3)_2$  ( $-0.161 e$ ) than in  $\text{RhH(PH}_3)_3$  ( $-0.043 e$ ). Because  $\text{CO}_2$  exhibits positive electrostatic potential toward the H ligand (Figure 5.4), the Cu reaction system can receive the larger ES stabilization than the Rh reaction system. The greater EX



**Figure 5.4** Map of electrostatic potential of CO<sub>2</sub>

a) The BS IV set was used. Contour values (eV unit) are 0.0,  $\pm 0.05$ ,  $\pm 0.10$ ,  $\pm 0.15$ ,  $\pm 0.25$ ,  $\pm 1.0$ ,  $\pm 1.5$ ,  $\pm 2.0$ ,  $\pm 2.5$ , and  $\pm 3.0$ . The solid lines indicate positive values, the dotted lines indicate negative values, and the --- lines indicate the values of 0.0.

repulsion of the Rh reaction system can be understood, considering the occupied  $4d_{xz}$  orbital of Rh. In general, the  $4d$  orbital expands to a greater extent than the  $3d$  orbital, and furthermore, the Cu atom possesses the least expanding  $3d$  orbital in the elements of the first transition series. Thus, the Rh  $4d_{xz}$  orbital gives rise to larger EX repulsion with the  $\pi$  and  $n\pi$  orbitals of CO<sub>2</sub> than the Cu  $3d_{xz}$  orbital



### Scheme 5.1

(Scheme 5.1). These results reasonably lead to a conclusion that the higher activation energy of the Rh reaction system arises from the stronger Rh(I)-H bond, the smaller electrostatic potential of  $\text{RhH}(\text{PH}_3)_3$ , and the more largely expanding  $4d_{xz}$  orbital of Rh than those of the  $\text{CuH}(\text{PH}_3)_2$ .

There are outstanding differences in the TS structure between two reaction systems. The first is that the C-H distance between  $\text{CO}_2$  and the H ligand is much shorter in the TS of the Rh reaction system than in the TS of the Cu reaction system (Figure 5.1). This is because  $\text{CO}_2$  must interact strongly with the H ligand at the TS of the Rh reaction system, to break the strong Rh(I)-H bond (vide supra). The next is that the RhHC angle is much larger than the CuHC angle (vide supra). As clearly shown in Table 5.4, both destabilization from the EX term and stabilization from the ES and CTPLXA terms increase, as the  $\theta$  angle becomes small. The increase of the EX repulsion energy cannot be



overwhelmed by the increases of ES and CTPLXA stabilization energies in the Rh reaction system but can be in the Cu reaction system. This difference is easily explained, as follows. The decrease in  $\theta$  enlarges the overlap of the Rh  $4d_{xz}$  orbital with the  $\pi$  and  $n\pi$  orbitals of  $\text{CO}_2$  (Scheme I), which increases the EX repulsion between them. Because of the smaller expanse of the Cu 3d orbital (vide supra), the EX repulsion is intrinsically weak in the Cu reaction system. Thus, the decrease in  $\theta$  strengthens the exchange repulsion of the Cu reaction system to a lesser extent than that of the Rh reaction system. Accordingly, the  $\theta$  angle is large at the TS of the Rh reaction system but small at the TS of the Cu reaction system. Although the dependence of ES and CTPLXA terms on the  $\theta$  angle can be explained in terms of the electrostatic potential and the expanse of  $d_{xz}$  orbital, we leave the explanation here, because their dependence is not the point in main discussion.

#### 5.4 Conclusions

The  $\text{CO}_2$  insertion into the Rh(I)-H bond easily occurs with an activation barrier of ca. 16 kcal/mol and exothermicity of ca. 24 kcal/mol (at the SD-CI level), yielding  $\text{Rh}(\eta^1\text{-OC(O)H})(\text{PH}_3)_3$ . This activation barrier is higher and the exothermicity is lower than those of the similar  $\text{CO}_2$  insertion into the Cu(I)-H bond of  $\text{CuH}(\text{PH}_3)_2$  ( $E_a = 3.5$  kcal/mol and  $E_{\text{exo}} = \text{ca. } 40$  kcal/mol at the SD-CI level). The higher activation energy of the Rh reaction system results from the facts that the Rh(I)-H bond is stronger than the Cu(I)-H bond, the negative electrostatic potential of  $\text{RhH}(\text{PH}_3)_3$  is smaller than that of  $\text{CuH}(\text{PH}_3)_2$ , and

the EX repulsion between  $\text{CO}_2$  and  $\text{RhH}(\text{PH}_3)_3$  is greater than that between  $\text{CO}_2$  and  $\text{CuH}(\text{PH}_3)_2$ . The lower exothermicity is due to the stronger  $\text{Rh}(\text{I})\text{-H}$  bond. The TS of the Rh reaction system has a shorter C-H distance between  $\text{CO}_2$  and the H ligand than the TS of the Cu reaction system. The strong  $\text{Rh}(\text{I})\text{-H}$  bond is the reason for the short C-H distance; in the TS of the Rh reaction system,  $\text{CO}_2$  must approach the H ligand to a greater extent than in the TS of the Cu reaction system, so as to break the strong  $\text{Rh}(\text{I})\text{-H}$  bond. The  $\theta$  angle at the TS is much different between two reaction systems; this angle is  $145^\circ$  in the Rh reaction system but only  $105^\circ$  in the Cu reaction system. The larger RhHC angle of the Rh reaction system arises from the strong EX repulsion between the  $4d_{xz}$  orbital of Rh and the  $\pi$  and  $n\pi$  orbitals of  $\text{CO}_2$ . The Rh  $4d_{xz}$  orbital more expands than the Cu  $3d_{xz}$  orbital, which gives rise to the stronger EX repulsion in the Rh reaction system. From these results, we can predict that the  $\text{CO}_2$  insertion into the M-H bond easily occurs when the M-H bond is weak, the electrostatic potential of the metal hydride complex is negatively large, and the expanse of the  $d_\pi$  orbital is small.

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- (17) This value was determined, according to an even-tempered criterion.
- (18) (a) The HF optimization with BS I offers reasonable geometries; For  $\text{Rh}(\text{CO})(\text{PH}_3)_2(\eta^1\text{-OCO}_2\text{H})$ ,  $R(\text{Rh-O}) = 2.009$  (2.075),  $R(\text{Ph-P}) = 2.338$  (2.333),  $R(\text{Rh-CO}) = 1.826$  (1.798), and for  $\text{RhH}_2(\text{PH}_3)_2(\eta^2\text{-O}_2\text{COH})$ ,  $R(\text{Rh-O})$

- = 2.237, 2.239, 2.279, 2.306), R(Rh-P) = 2.306(2.302), R(Rh-H) = 1.512 and 1.513 (1.41 and 1.47), where values are in Å unit, and in parentheses are experimental values for Rh(CO)(PPh<sub>3</sub>)<sub>2</sub>(η<sup>1</sup>-OCO<sub>2</sub>H)<sup>18b</sup> and RhH<sub>2</sub>(PPr<sup>i</sup><sub>3</sub>)<sub>2</sub>(η<sup>2</sup>-O<sub>2</sub>COH)<sup>18c</sup>
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- (27) S. Sakaki and Y. Musashi, submitted for Inorg. Chem.
- (28) In the precursor complex,  $\text{CuH}(\text{PH}_3)_2 \cdots \text{CO}_2$ , the  $\text{Cu}-\text{O}^1$  distance is 3.28 Å, the C-H distance is 2.66 Å, the  $\text{C}-\text{O}^1$  and  $\text{C}-\text{O}^2$  distances are 1.168 and 1.159 Å, the OCO angle is  $172^\circ$ , and the Cu-H distance lengthens by 0.06 Å.<sup>27</sup>
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value, while the HF-optimization provides slightly more reactant-like TS than the optimization at the correlated level.

- (31) The TS structure was roughly determined in our previous work<sup>3b</sup> and correctly optimized at the HF level with the energy gradient technique in our recent work.<sup>27</sup> The basis sets used for ligand atoms were the same as the BS I, and the basis set and ECPs used for Cu were of the same quality as those used for Rh in the BS I (see ref. 3). The C-H distance is 1.68 Å, the Cu-O<sup>1</sup> distance is 2.50 Å, the CuHC angle is 105°, the OCO angle is 149°, the C-O<sup>1</sup> and C-O<sup>2</sup> distances are 1.21 and 1.18 Å respectively, and the Cu-H distance is 1.68 Å (about 0.15 Å longer than in CuH(PH<sub>3</sub>)<sub>2</sub>).
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## CO<sub>2</sub> Insertion Into a Rh(III)-H Bond

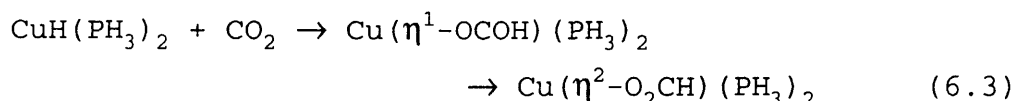
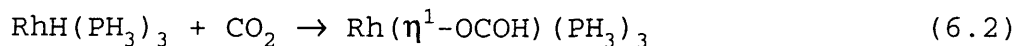
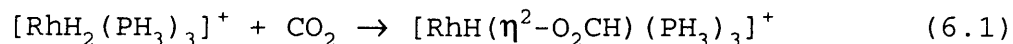
### 6-1 Introduction

Insertion reactions of alkenes and alkynes into metal-hydride and metal-alkyl bonds are involved as a key process in many catalytic reactions by transition metal complexes. In this regard, many theoretical works have been reported on those insertion reactions.<sup>1</sup> Considering the importance of the insertion reactions in catalytic cycles,<sup>2</sup> we can expect that the CO<sub>2</sub> insertion into the metal-hydride and metal-alkyl bonds would be utilized to construct a good catalytic system for CO<sub>2</sub> fixation. In fact, several interesting catalytic systems for the CO<sub>2</sub> fixation involve the CO<sub>2</sub> insertion into the metal-hydride bond, as have been reported so far.<sup>3-5</sup> However, only a few of theoretically works have been carried out on the CO<sub>2</sub> insertion reactions,<sup>6,7</sup> whereas the theoretical knowledge is indispensable to finding a good catalytic system for the CO<sub>2</sub> fixation. Furthermore, the CO<sub>2</sub> insertion reaction is worthwhile investigating from the point of view of theoretical chemistry because CO<sub>2</sub> has different frontier orbitals from those of alkene and alkyne; the HOMO of CO<sub>2</sub> is non-bonding  $\pi$  ( $n\pi$ ) orbital and the LUMO of CO<sub>2</sub> is the polarized  $\pi^*$  orbital which expands more at the C atom than at the O atoms.

In this chapter, the CO<sub>2</sub> insertion into the Rh(III)-H (Rh<sup>III</sup>-H) bond (eq 6.1) is investigated with ab initio MO/MP4, SD-CI and CCD methods, and compared with the similar



CO<sub>2</sub> insertion into the Rh<sup>I</sup>-H and Cu(I)-H (Cu<sup>I</sup>-H) bonds (eqs 6.2 and 6.3).



Similar CO<sub>2</sub> insertion reactions have been experimentally reported for Cu<sup>I</sup>-CH<sub>3</sub>,<sup>8</sup> Cu<sup>I</sup>-H,<sup>9</sup> Rh<sup>I</sup>-H,<sup>10</sup> and Rh<sup>III</sup>-H complexes.<sup>4</sup> Purposes of this chapter are (1) to examine basis set effects and electron correlation effects on these reactions, (2) to compare the reactivities of CuH(PH<sub>3</sub>)<sub>2</sub>, RhH(PH<sub>3</sub>)<sub>3</sub>, and [RhH<sub>2</sub>(PH<sub>3</sub>)<sub>3</sub>]<sup>+</sup> in the CO<sub>2</sub> insertion reaction, and (3) to clarify what factors determine the ease of CO<sub>2</sub> insertion reaction.

## 6-2 Computational Details

Geometries of reactants, transition states (TS), and products were optimized at the Hartree-Fock (HF) level with the energy gradient technique, and then MP2 to MP4SDQ, SD-CI and coupled cluster with double substitution (CCD) calculations were carried out on those optimized geometries, where core orbitals were excluded from the active space. In SD-CI calculations, the contributions of higher-order excited configurations were estimated, according to Davidson,<sup>11</sup> Davidson-Silver,<sup>12</sup> and Pople's methods.<sup>13</sup> In CCD calculations, the contributions of single and triple substitutions were evaluated through forth-order with CCD wave functions.<sup>14</sup> Gaussian 86<sup>15</sup> and 92<sup>16</sup> programs were used for these calculations.

Several kinds of basis sets were used in these

**Table 6.1** Basis sets used in this work

	BS-I	BS-II	BS-III	BS-IV
Cu	ECP(~3p) +(21/21/31) <sup>a</sup>	ECP(~3p) +(21/21/211) <sup>a</sup>	ECP(~2p) +(311/311/311) <sup>d</sup>	ECP(~2p) +(311/311/311) <sup>d</sup>
Rh	ECP(~4p) +(21/21/31) <sup>a</sup>	ECP(~4p) +(21/21/211) <sup>a</sup>	ECP(~3d) +(311/311/211) <sup>d</sup>	ECP(~3d) +(311/311/211) <sup>d</sup>
PH <sub>3</sub>	STO-2G	MIDI-4 <sup>b</sup>	MIDI-4 <sup>b</sup>	MIDI-4 <sup>b</sup>
CO <sub>2</sub>	MIDI-3 <sup>b</sup>	MIDI-4 <sup>4</sup>	MIDI-4 <sup>4</sup>	MIDI-4 <sup>4</sup>
H <sub>(hydride)</sub>	(31/1) <sup>c</sup>	(31/1) <sup>c</sup>	(31/1) <sup>c</sup>	(31/1) <sup>c</sup>

	BS-V	BS-VI	BS-VII
Cu	ECP(~2p) +(311/311/311) <sup>d</sup>	(43321/4311 /311) <sup>e</sup>	(43321/4311 /311) <sup>e</sup>
Rh	ECP(~3d) +(311/311/211) <sup>d</sup>	(433321/43311 /4211) <sup>e</sup>	(433321/43311 /4211) <sup>e</sup>
PH <sub>3</sub>	MIDI-4 <sup>b</sup>	MIDI-4 <sup>b</sup>	MIDI-4 <sup>b</sup>
CO <sub>2</sub>	(621/41/1) <sup>c</sup>	MIDI-4 <sup>4</sup>	MIDI-4 <sup>*b</sup>
H <sub>(hydride)</sub>	(31/1) <sup>c</sup>	(31/1) <sup>c</sup>	(31/1) <sup>c</sup>

a) Ref. 13. b) Ref. 14 c) Ref. 15. d) Ref. 16. e) The (43333/43/4)<sup>14</sup> for Cu and (43333/433/43)<sup>14</sup> for Rh basis sets were augmented with a diffuse function,  $\zeta = 0.141$  and  $\zeta = 0.08$ , respectively.

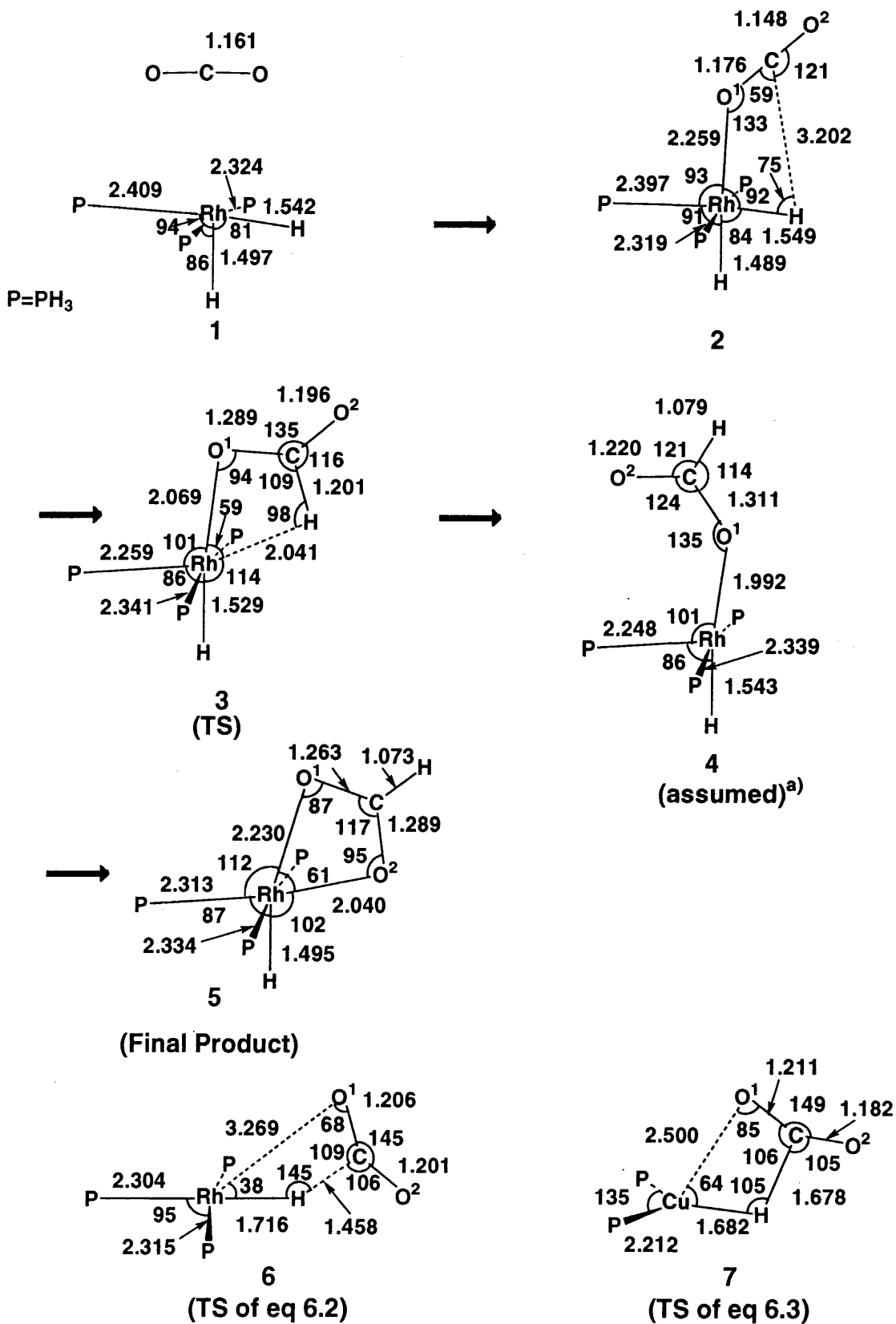
calculations. As summarized in Table 6.1, the quality becomes higher going to BS-VII from BS-I. The BS-I was employed for geometry optimization, and the other better basis sets were used for correlated calculations. The reliability of effective core potentials was investigated by

comparing BS-II, BS-III, BS-IV, BS-VI, and BS-VII, where BS-II involves a large ECP (up to 4p electron of Rh), BS-III and BS-IV involve a small ECP (up to 3d electron of Rh), BS-VI and BS-VII involve an all electron basis set for Rh. Effects of polarization functions are also examined by comparing BS-III and BS-VI with BS-IV and BS-VII respectively, where polarization functions were added to CO<sub>2</sub> in the latter two basis sets.

### 6-3 Results and Discussion

#### 6-3-1 Geometries of Reactants, Transition States, and Products

The CO<sub>2</sub> insertion into the Rh<sup>III</sup>-H bond proceeds via the precursor complex **2** and the transition state (TS) **3**, finally affording the  $\eta^2$ -O<sub>2</sub>CH complex **5**, as shown in Figure 6.1. In **2**, both CO<sub>2</sub> and RhH<sub>2</sub>(PH<sub>3</sub>)<sub>3</sub> parts little distort, which suggests that the interaction between CO<sub>2</sub> and Rh<sup>III</sup> is very weak. These geometrical features of precursor complex are common to the CO<sub>2</sub> insertion into CuH(PH<sub>3</sub>)<sub>2</sub> and RhH(PH<sub>3</sub>)<sub>3</sub>.<sup>21</sup> This is not surprising because the coordinate bond of CO<sub>2</sub> to transition metal is in general weak. The geometry of TS **3** is, however, much different from TS of the CO<sub>2</sub> insertion into Cu<sup>I</sup>-H and Rh(I)-H (Rh<sup>I</sup>-H) bonds (see **6** and **7** in Figure 6.1). In **3**, the Rh-O<sup>1</sup> and C-H distances are shorter, and the OCO angle is more closed than those in **6** and **7**. This Rh-O<sup>1</sup> distance seems to be almost the same as the usual coordinate bond distance, and surprisingly, it is much shorter than in the product. These features indicate that **3** is product-like, while **6** and **7** are rather reactant-like. There is the other difference to be noted; CO<sub>2</sub> little



**Figure 6.1** Geometry changes in the CO<sub>2</sub> insertion into the Rh<sup>III</sup>-H bond of [RhH<sub>2</sub>(PH<sub>3</sub>)<sub>3</sub>]<sup>+</sup>.

Bond distance in Å and bond angle in degree.

changes its coordination site but the hydride ligand attacks CO<sub>2</sub> in **3**, whereas CO<sub>2</sub> moves toward the hydride ligand and inserts into the M-H bond in **6** and **7**.

Geometries of products are also discussed briefly here. The CO<sub>2</sub> insertion reaction with [RhH<sub>2</sub>(PH<sub>3</sub>)<sub>3</sub>]<sup>+</sup> affords the η<sup>2</sup>-formate complex [RhH(PH<sub>3</sub>)<sub>3</sub>(η<sup>2</sup>-O<sub>2</sub>CH)]<sup>+</sup> **5**. This is because the Rh<sup>III</sup> complex is a d<sup>6</sup> system and tends to form a six-coordinate system. The similar η<sup>2</sup>-formate complex Cu(PH<sub>3</sub>)<sub>2</sub>(η<sup>2</sup>-O<sub>2</sub>CH) is the product of the CO<sub>2</sub> insertion reaction with CuH(PH<sub>3</sub>)<sub>2</sub>,<sup>6b</sup> because Cu<sup>I</sup> has a d<sup>10</sup> electron configuration and tends to take a tetrahedral-like four-coordinate complex. On the other hand, the CO<sub>2</sub> insertion reaction with RhH(PH<sub>3</sub>)<sub>3</sub> yields the η<sup>1</sup>-formate complex Rh(η<sup>1</sup>-OCOH)(PH<sub>3</sub>)<sub>3</sub> as a product, where the η<sup>2</sup>-formate complex Rh(η<sup>2</sup>-O<sub>2</sub>CH)(PH<sub>3</sub>)<sub>3</sub> is less stable than the η<sup>1</sup>-formate complex. The reason for this result is that Rh<sup>I</sup> takes a d<sup>8</sup> electron configuration and tends to form a planar four-coordinate complex unlike Cu<sup>I</sup> and Rh<sup>III</sup>.

### **6-3-2 Electron Correlation and Basis set Effects on Activation Energy and Reaction Energy**

The activation energy (E<sub>a</sub>) is defined as an energy difference between the precursor complex and the TS, the reaction energy (ΔE) is an energy difference between sum of reactants, MHL<sub>n</sub> and CO<sub>2</sub>, and the final product, and the binding energy (BE) is a stabilization energy of the precursor complex relative to reactants. A negative ΔE value means exothermicity. First, correlation effects on BE, E<sub>a</sub>, and ΔE of the CO<sub>2</sub> insertion into the Rh<sup>III</sup>-H bond will be examined, using BS-VI. As shown in Table 6.2, BE hardly

**Table 6.2** Electron correlation effects<sup>a</sup> on stabilization energy (BE) of precursor complex,<sup>b</sup> activation energy ( $E_a$ )<sup>c</sup> and reaction energy ( $\Delta E$ ).<sup>d</sup>

	HF	MP2	MP3	MP4DQ	MP4SDQ	SD-CI (D)
$[\text{RhH}_2(\text{PH}_3)_3]^+ + \text{CO}_2 \rightarrow [\text{Rh}(\eta^2\text{-O}_2\text{CH})\text{H}(\text{PH}_3)_3]^+$						
BE	6.8	13.1	11.0	12.3	13.2	11.6
$E_a$	44.2	52.9	44.2	48.8	46.8	45.5
$\Delta E$	-14.2	-3.3	-13.9	-8.8	-10.5	-13.6
$\text{RhH}(\text{PH}_3)_3 + \text{CO}_2 \rightarrow \text{Rh}(\eta^1\text{-OCOH})\text{H}(\text{PH}_3)_3$						
BE	1.5	3.4	3.6	3.2	3.2	3.3
$E_a$	12.2	24.6	15.1	21.0	20.5	15.7
$\Delta E$	-37.3	-7.7	-27.9	-17.8	-15.6	-26.2

	SD-CI (DS)	SD-CI (P)	CCD (ST)
$[\text{RhH}_2(\text{PH}_3)_3]^+ + \text{CO}_2 \rightarrow [\text{Rh}(\eta^2\text{-O}_2\text{CH})\text{H}(\text{PH}_3)_3]^+$			
BE	6.8	11.0	12.3
$E_a$	44.2	44.2	48.8
$\Delta E$	-14.2	-13.9	-8.8
$\text{RhH}(\text{PH}_3)_3 + \text{CO}_2 \rightarrow \text{Rh}(\eta^1\text{-OCOH})\text{H}(\text{PH}_3)_3$			
BE	1.5	3.6	3.2
$E_a$	12.2	15.1	21.0
$\Delta E$	-37.3	-27.9	-17.8

a) BS VI was used. b) The energy difference between sum of reactants and the precursor complex. c) The energy difference between the precursor complex and the TS. d) The energy difference between the sum of reactants and the most stable product. A negative value means the exothermicity.

**Table 6.3** Eigenvalues of instability matrix at the TS of CO<sub>2</sub> insertion reactions

	[RhH <sub>2</sub> (PH <sub>3</sub> ) <sub>3</sub> ] <sup>+</sup>	RhH(PH <sub>3</sub> ) <sub>3</sub>	CuH(PH <sub>3</sub> ) <sub>2</sub>
Internal RHF	0.122	0.089	0.215
RRHF → CRHF	0.094	0.058	0.201
RRHF → RUHF	0.056	0.018	0.099

depends on the computational method except for the HF level. E<sub>a</sub> and ΔE somewhat fluctuate upon going from HF to MP4DQ but only a little upon going from MP4SDQ to CCD. In the CO<sub>2</sub> insertion into the Rh<sup>I</sup>-H bond of RhH(PH<sub>3</sub>)<sub>3</sub>, E<sub>a</sub> and ΔE somewhat change upon going to SD-CI and CCD from MP4SDQ. However, it should be noted that CCD calculations provide intermediate BE, E<sub>a</sub>, and ΔE values between MP4SDQ and SD-CI calculations. This suggests that single-reference wave function can be used for these reaction systems. Consistent with this suggestion, no instability of HF wave functions was observed for TS of these three CO<sub>2</sub> insertion reactions; as shown in Table 6.3, the minimum eigenvalue of the instability matrix is not large but apparently positive.

Then, basis set effects were examined at the MP4SDQ level, because MP4SDQ calculations yield similar E<sub>a</sub> and ΔE values to CCD calculations with only one exception that E<sub>a</sub> of the CO<sub>2</sub> insertion into the Rh<sup>I</sup>-H bond is slightly different between CCD and MP4SDQ methods (vide supra). As shown in Table 6.4, several significant effects are observed; (1) Addition of d-polarization functions to CO<sub>2</sub>

**Table 6.4** Basis set effects on BE,  $E_a$  and  $\Delta E^a$ 

		BS-II	BS-III	BS-IV	BS-V	BS-VI	BS-VII
(a) $\text{RhH}(\text{PH}_3)_3 + \text{CO}_2 \rightarrow \text{Rh}(\eta^1\text{-OCOH})\text{H}(\text{PH}_3)_3$							
BE	HF	1.9	1.6	1.3	0.5	1.5	0.8
	MP4SDQ	3.3	3.2	7.5	2.8	3.2	2.8
$E_a$	HF	13.8	13.8	20.2	18.5	12.2	21.0
	MP4SDQ	14.7	15.6	19.5	18.0	20.5	24.6
$\Delta E$	HF	-39.4	-34.9	-10.2	-13.6	-37.3	-12.2
	MP4SDQ	-22.1	-15.3	-5.2	-4.1	-15.6	-0.4
(b) $[\text{RhH}_2(\text{PH}_3)_3]^+ + \text{CO}_2 \rightarrow [\text{Rh}(\eta^2\text{-O}_2\text{CH})\text{H}(\text{PH}_3)_3]^+$							
BE	HF	11.6	6.8	4.3	2.9	6.8	4.1
	MP4SDQ	15.8	12.5	14.8	10.3	13.2	10.9
$E_a$	HF	42.2	46.5	58.0	54.7	44.2	56.8
	MP4SDQ	45.1	48.2	53.0	50.9	46.8	52.3
$\Delta E$	HF	-23.5	-12.2	7.5	5.3	-14.2	6.6
	MP4SDQ	-17.7	-8.3	-2.5	-0.3	-10.5	0.8

BS VII was used (kcal/mol). a) See footnote b)~d) of Table 2.

decreases exothermicity and enlarges the  $E_a$  value (compare BS-III and BS-VI with BS-IV and BS-VII respectively). Effects of polarization functions are significantly larger at the HF level than at the correlated level. (2) Use of all electron basis set for Rh instead of ECP does not cause significant change on  $E_a$  and  $\Delta E$ , whereas the  $E_a$  value of the



CO<sub>2</sub> reaction with RhH(PH<sub>3</sub>)<sub>3</sub> slightly increases by 4 kcal/mol upon going to all electron basis set from ECP (compare BS-III with BS-VI). The same result is observed in comparing BS-IV with BS-VII. (3) Improvement of the basis set for s and p orbitals of CO<sub>2</sub> little changes the E<sub>a</sub> and ΔE values (compare BS-IV with BS-V). (4) Introduction of electron correlation decreases the exothermicity independently on the presence of the polarization functions on C and O atoms, slightly increases E<sub>a</sub> in the absence of the polarization functions but little changes E<sub>a</sub> in the presence of the polarization functions. The above results are summarized as follows; the addition of d-polarization functions on CO<sub>2</sub> considerably changes E<sub>a</sub> and ΔE, and electron correlation effects on E<sub>a</sub> and ΔE are not significant when the polarization functions are added on CO<sub>2</sub>. This indicates that the d-polarization functions should be added on C and O atoms to estimate quantitatively E<sub>a</sub> and ΔE.

### **6-3-3 Comparison of Exothermicity in the Rh<sup>III</sup>, Rh<sup>I</sup>, and Cu<sup>I</sup> Reaction Systems**

The CO<sub>2</sub> reaction with [RhH<sub>2</sub>(PH<sub>3</sub>)<sub>3</sub>]<sup>+</sup> requires the highest E<sub>a</sub> value and yields the smallest exothermicity (see Table 6.5). First, we will compare the exothermicity between three insertion reactions. Because a comparison between CuH(PH<sub>3</sub>)<sub>2</sub> and RhH(PH<sub>3</sub>)<sub>3</sub> has been made in chapter 5 and ref. 21, its comparison is briefly repeated here. The difference between Cu<sup>I</sup>-H and Rh<sup>I</sup>-H bond energies and that between Cu<sup>I</sup>-(η<sup>2</sup>-O<sub>2</sub>CH) and Rh<sup>I</sup>-(η<sup>2</sup>-O<sub>2</sub>CH) bond energies were estimated, according to the following assumed eqs 6.8 and 6.10 respectively:

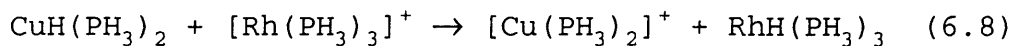
**Table 6.5**  $E_a^a$  and  $\Delta E^a$  of the  $\text{CO}_2$  insertion reactions with  $\text{RhH}(\text{PH}_3)_3$ ,  $[\text{RhH}_2(\text{PH}_3)_3]^+$ , and  $\text{CuH}(\text{PH}_3)_2$

	$\text{CuH}(\text{PH}_3)_2$			$\text{RhH}(\text{PH}_3)_3$		
	HF	MP4SDQ	SDCI (DS)	HF	MP4SDQ	SDCI (DS)
$E_a$	10.3	7.1	6.5	21.0	24.6	21.2
$\Delta E$	-31.7	-32.1	-33.5	-12.2	-0.4	-7.0

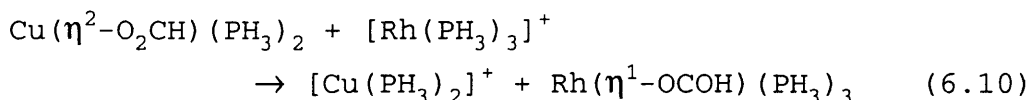
  

	$[\text{RhH}_2(\text{PH}_3)_3]^+$		
	HF	MP4SDQ	SDCI (DS)
$E_a$	56.8	52.3	51.3
$\Delta E$	6.6	0.8	-1.1

BS-VII was used (kcal/mol unit). a) See footnote c) and d) of Table 2.



$$\Delta E_{r-1} = D(\text{Cu}^{\text{I}}-\text{H}) - D(\text{Rh}^{\text{I}}-\text{H}) \quad (6.9)$$

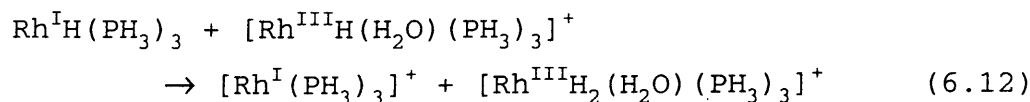


$$\Delta E_{r-1} = D(\text{Cu}^{\text{I}}-(\eta^2\text{-O}_2\text{CH})) - D(\text{Rh}^{\text{I}}-(\eta^1\text{-OCOH})) \quad (6.11)$$

where  $D(\text{X}-\text{Y})$  = the  $\text{X}-\text{Y}$  bond energy and  $\Delta E_{r-1} = E_t$  (the right hand side of the eq) -  $E_t$  (the left hand side of the eq).

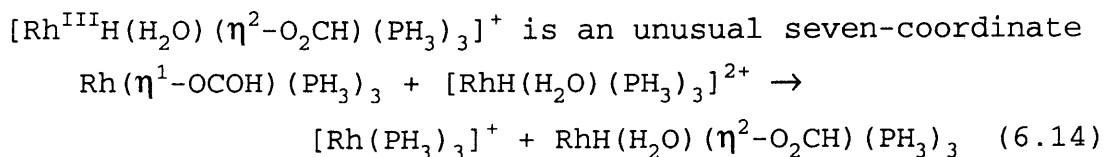
These energy differences were calculated at the MP4SDQ level because MP4SDQ calculations provide similar  $E_a$  and  $\Delta E$  values to those of CCD calculations (vide supra). As shown in Table 6.6, the  $\text{Rh}^{\text{I}}-\text{H}$  bond is considerably stronger than the  $\text{Cu}^{\text{I}}-\text{H}$  bond, whereas the  $\text{Rh}^{\text{I}}-(\eta^1\text{-OCOH})$  is slightly stronger

than the  $\text{Cu}^{\text{I}}-(\eta^2\text{-O}_2\text{CH})$  bond. Thus, the stronger  $\text{Rh}^{\text{I}}\text{-H}$  bond than the  $\text{Cu}^{\text{I}}\text{-H}$  bond is the main reason that the  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{I}}\text{-H}$  bond is much less exothermic than that into the  $\text{Cu}^{\text{I}}\text{-H}$  bond. Then, the similar comparison is made between  $\text{RhH}(\text{PH}_3)_3$  and  $[\text{RhH}_2(\text{PH}_3)_3]^+$ . The difference between the  $\text{Rh}^{\text{I}}\text{-H}$  and  $\text{Rh}^{\text{III}}\text{-H}$  bond energies was estimated, considering the following assumed eq 6.12.

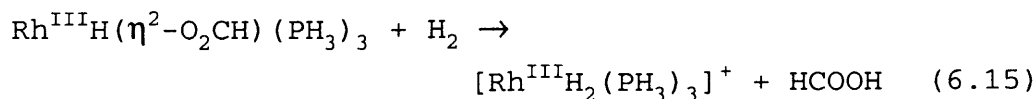


$$\Delta E_{r-1} = D(\text{Rh}^{\text{I}}\text{-H}) - D(\text{Rh}^{\text{III}}\text{-H}) \quad (6.13)$$

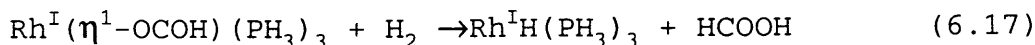
where  $\text{H}_2\text{O}$  was coordinated to  $[\text{Rh}^{\text{III}}\text{H}(\text{PH}_3)_3]^{2+}$  to stabilize the four coordinate  $d^6$  system because the four coordinate  $d^6$  system such as  $[\text{Rh}^{\text{III}}\text{H}(\text{PH}_3)_3]^{2+}$  was unstable. The term of  $D(\text{Rh}^{\text{III}}\text{-H}) - D(\text{Rh}^{\text{I}}\text{-H})$  is 117 kcal/mol at the MP4SDQ level, indicating that the  $\text{Rh}^{\text{III}}\text{-H}$  bond is much stronger than the  $\text{Rh}^{\text{I}}\text{-H}$  bond. The similar eq 6.14, however, could not be employed for estimating the difference between the  $\text{Rh}^{\text{I}}-(\eta^1\text{-OCOH})$  and  $\text{Rh}^{\text{III}}-(\eta^2\text{-O}_2\text{CH})$  bond energies because



So, we estimated the difference, considering the following two eqs 6.15 and 6.17.



$$\Delta E_{r-1}(\text{eq 6.15}) = D(\text{Rh}^{\text{III}}-(\eta^2\text{-O}_2\text{CH})) + D(\text{H-H}) - D(\text{Rh}^{\text{III}}\text{-H}) - D(\text{C-H}) \quad (6.16)$$



$$\Delta E_{r-1}(\text{eq 6.17}) = D(\text{Rh}^{\text{I}}-(\eta^1\text{-OCOH})) + D(\text{H-H}) - D(\text{Rh}^{\text{I}}\text{-H}) - D(\text{C-H}) \quad (6.18)$$

From eqs 6.16 and 6.18, the following eq 6.19 is obtained;

$$\begin{aligned} \Delta E_{r-1}(\text{eq 6.15}) - \Delta E_{r-1}(\text{eq 17}) &= D(\text{Rh}^{\text{III}}-(\eta^2\text{-O}_2\text{CH})) \\ &- D(\text{Rh}^{\text{I}}-(\eta^1\text{-OOCH})) + D(\text{Rh}^{\text{I}}\text{-H}) - D(\text{Rh}^{\text{III}}\text{-H}) \quad (6.19) \end{aligned}$$

Because the term of  $D(\text{Rh}^{\text{I}}\text{-H}) - D(\text{Rh}^{\text{III}}\text{-H})$  has been estimated above, the term of  $D(\text{Rh}^{\text{III}}-(\eta^2\text{-O}_2\text{CH})) - D(\text{Rh}^{\text{I}}-(\eta^1\text{-OOCH}))$  can

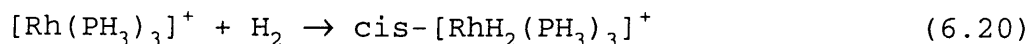
**Table 6.6** Difference in bond energy calculated with MP2~MP4SDQ/BS-VII method (kcal/mol)

	MP2	MP3	MP4DQ	MP4SDQ
$D(\text{Rh}^{\text{III}}-(\eta^2\text{-O}_2\text{CH})) - D(\text{Rh}^{\text{I}}-(\eta^1\text{-OOCH}))^a$	109	131	119	111
$D(\text{Rh}^{\text{III}}\text{-H}) - D(\text{Rh}^{\text{I}}\text{-H})^a$	109	121	114	109
$D(\text{Rh}^{\text{I}}-(\eta^1\text{-OOCH})) - D(\text{Cu}^{\text{I}}-(\eta^1\text{-OOCH}))^a$	9	8	6	5
$D(\text{Rh}^{\text{I}}\text{-H}) - D(\text{Cu}^{\text{I}}\text{-H})^a$	37	30	31	28
$D(\text{Rh}^{\text{III}}\text{-H})$	64	60	64	63

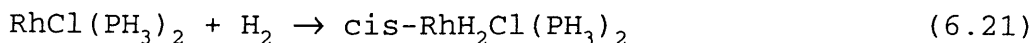
a) For heterolytic bond breaking. b) For homolytic bond breaking.

be estimated from eq 6.19. As given in Table 6.6, the  $\text{Rh}^{\text{III}}-(\eta^2\text{-O}_2\text{CH})$  and  $\text{Rh}^{\text{III}}\text{-H}$  bonds are much stronger than the  $\text{Rh}^{\text{I}}-(\eta^1\text{-OOCH})$  and  $\text{Rh}^{\text{I}}\text{-H}$  bonds respectively. However, the difference between  $\text{Rh}^{\text{III}}\text{-H}$  and  $\text{Rh}^{\text{I}}\text{-H}$  bond energies is slightly smaller than the difference between  $\text{Rh}^{\text{I}}-(\eta^1\text{-OOCH})$  and  $\text{Rh}^{\text{III}}-(\eta^2\text{-O}_2\text{CH})$  bond energies. Thus, the  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{III}}\text{-H}$  bond is slightly less exothermic than the  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{I}}\text{-H}$  bond.

At the end of this section, it is necessary to mention the meaning of the bond energy given in Table 6.6. The  $D(\text{Rh}^{\text{III}}\text{-H})$  bond energy was estimated to be about 63 kcal/mol at the MP4SDQ level, considering the following eq 6.20.



The similar value was reported by Koga et al. from eq 6.23.<sup>22</sup>

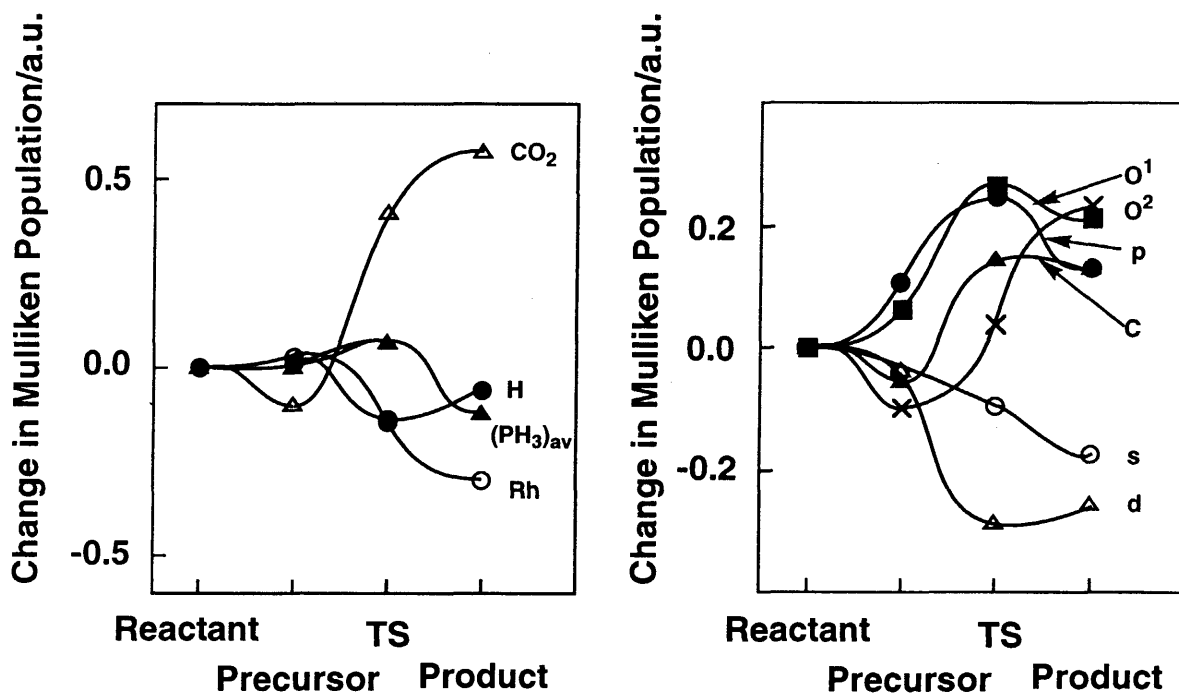


This  $D(\text{Rh}^{\text{III}}\text{-H})$  value and the value of  $D(\text{Rh}^{\text{III}}\text{-H}) - D(\text{Rh}^{\text{I}}\text{-H})$  in Table 6.6 lead to a negative  $D(\text{Rh}^{\text{I}}\text{-H})$  value. This is strange apparently, if we do not pay attention to the fact that the meaning of the bond energy is different between eqs 6.13 and 6.20. The  $\text{Rh}^{\text{III}}\text{-H}$  bond energy from eqs 6.20 and 6.21 was estimated from the homolytic bond fission, while  $\text{Rh}^{\text{III}}\text{-H}$  and  $\text{Rh}^{\text{I}}\text{-H}$  bond energies in eq 6.13 were from the heterolytic bond fission. Thus, the term of  $D(\text{Rh}^{\text{III}}\text{-H}) - D(\text{Rh}^{\text{I}}\text{-H})$  in eq 6.13 cannot be related to the  $D(\text{Rh}^{\text{III}}\text{-H})$  value estimated from eq 6.20. This is the reason that the term of  $D(\text{Rh}^{\text{III}}\text{-H}) - D(\text{Rh}^{\text{I}}\text{-H})$  seems too large. Also, we must comment here that the exothermicity of the  $\text{CO}_2$  insertion is reasonably discussed in terms of the bond energies based on the heterolytic bond fission because the H ligand moves toward  $\text{CO}_2$  as a hydride, as will be described below.

#### **6-3-4 Bonding Nature of the Transition State and the Activation Energy**

As shown in Table 6.6, the  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{III}}\text{-H}$  bond requires the much higher activation energy than the  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{I}}\text{-H}$  and  $\text{Cu}^{\text{I}}\text{-H}$  bonds. This high activation energy would be related to the geometry and the bonding nature at the TS **3** (Figure 6.1).

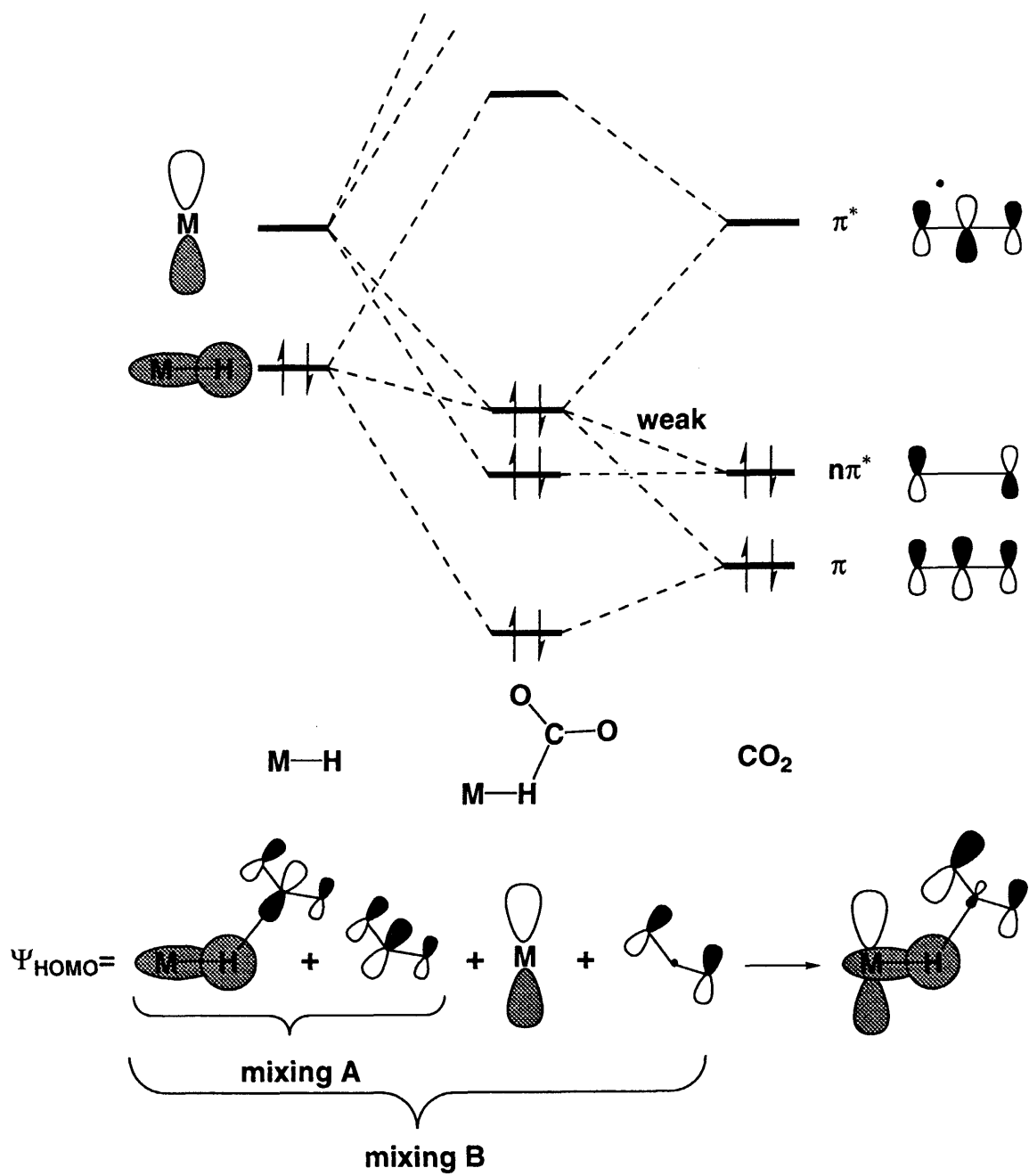
First, let us see the electron redistribution by the  $\text{CO}_2$  insertion to shed some light on the bonding nature. Several interesting features are observed in Mulliken population changes. As shown in Figure 6.2, the electron



**Figure 6.2** Changes in Mulliken population<sup>a</sup> in the CO<sub>2</sub> insertion into the Rh<sup>III</sup>-H bond of [RhH<sub>2</sub>(PH<sub>3</sub>)<sub>3</sub>]<sup>+</sup>.

a) A positive value represents the increase in population and vice versa. The standard (change zero) is taken for the sum of reactants, [RhH<sub>2</sub>(PH<sub>3</sub>)<sub>3</sub>]<sup>+</sup> + CO<sub>2</sub>.

population of CO<sub>2</sub> significantly increases as the CO<sub>2</sub> insertion proceeds. In CO<sub>2</sub>, the O<sup>1</sup> and O<sup>2</sup> atomic populations remarkably increase but the C atomic population increases less than the O atomic population. These features are common in the CO<sub>2</sub> insertion. They are explained in terms of orbital mixing **A** shown in Scheme 6.1. The charge transfer from the occupied orbitals of [Rh<sup>III</sup>H<sub>2</sub>(PH<sub>3</sub>)<sub>3</sub>]<sup>+</sup> to the π\* orbital of CO<sub>2</sub> occurs in the CO<sub>2</sub> insertion, and at the same time, the π orbital of CO<sub>2</sub> mixes into the charge-transfer



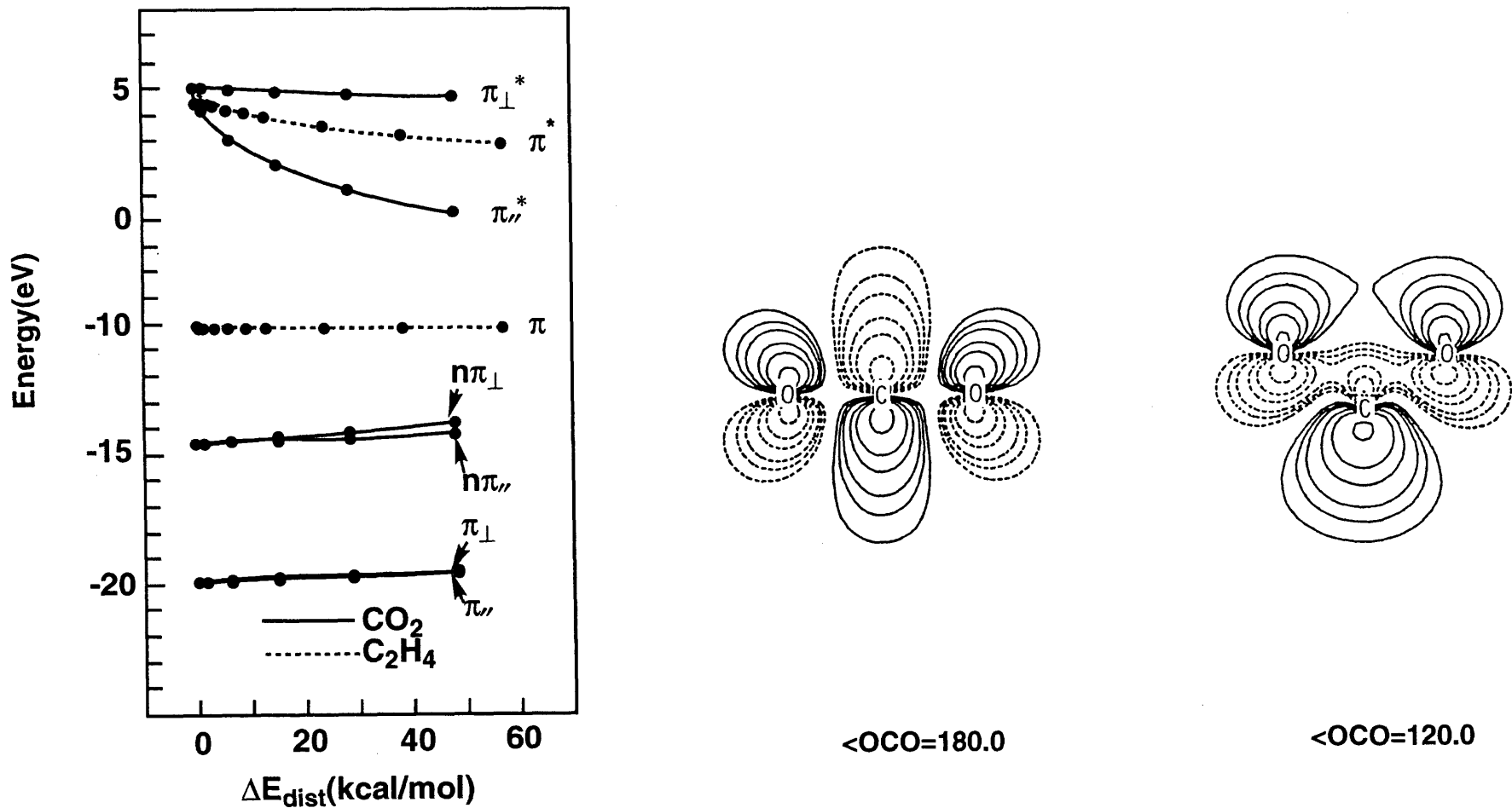
Scheme 6.1

interaction in an anti-bonding way with the occupied orbital of  $[\text{Rh}^{\text{III}}\text{H}_2(\text{PH}_3)_2]^{2+}$ . This mixing enhances the  $p_\pi$  orbitals of O but weakens the  $p_\pi$  orbital of C, which increases the O atomic population much more than the C atomic population, as we have seen in Figure 6.2. These features also suggest that the bonding interaction between  $\text{CO}_2$  and the H ligand is produced by the charge transfer from HOMO of  $[\text{Rh}^{\text{III}}\text{H}_2(\text{PH}_3)_3]^+$  to the  $\pi^*$  orbital of  $\text{CO}_2$ . The HOMO includes the significant contribution of the H 1s orbital. Thus, the  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{III}}\text{-H}$  bond is characterized as a nucleophilic attack of the H ligand to  $\text{CO}_2$ , in other word, the H ligand moves toward  $\text{CO}_2$  as a hydride.

It is necessary to discuss here the origin of the strong charge-transfer interaction from the metal-hydride to  $\text{CO}_2$ .  $\text{CO}_2$  causes the bending distortion, as the  $\text{CO}_2$  insertion proceeds. Although the  $\pi^*$  orbital of the undistorted  $\text{CO}_2$  lies at a relatively high energy level like  $\text{C}_2\text{H}_4$ , it considerably lowers in energy upon bending of  $\text{CO}_2$ , as shown in Figure 6.3A. Comparing  $\text{CO}_2$  with  $\text{C}_2\text{H}_4$  at the same distortion energy, the  $\pi^*$  orbital of  $\text{CO}_2$  lies at a much lower energy than that of  $\text{C}_2\text{H}_4$ . This is because the bonding overlap between two O atoms emerges in the  $\pi^*$  orbital when  $\text{CO}_2$  causes the bending distortion (see contour map in Figure 6.3B). Such bonding overlap dose not emerge at all in the  $\pi^*$  orbital of  $\text{C}_2\text{H}_4$  even if  $\text{C}_2\text{H}_4$  causes the distortion. Thus, it is reasonably concluded that the strong charge-transfer interaction is one of the characteristic features of the  $\text{CO}_2$  insertion reaction.

Although qualitatively the same electron redistribution is observed in the other  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{I}}\text{-H}$  and





(A)  $\pi$ ,  $n\pi$ , and  $\pi^*$  orbital energies vs. distortion energy.<sup>a)</sup>

(B) Contour map of the  $\text{CO}_2 \pi^*$  orbital.<sup>b)</sup>

**Figure 6.3** The frontier orbital energy levels vs. the distortion energy,<sup>a</sup> and the contour map of the  $\text{CO}_2 \pi^*$  orbital.

a) MP4SDQ/MIDI-4.  $n\pi$  means non-bonding  $\pi$  orbital.  $\pi_{//}$ , etc. represents the  $\pi$  orbital in the molecular

**Table 6.7** Comparison of Mulliken populaitons

	$[\text{RhH}_2(\text{PH}_3)_3]^+$			$\text{RhH}(\text{PH}_3)_3$	
	Reactant	(TS) <sup>a</sup>	TS	Reactant	TS
H	0.937	1.089	1.005	1.039	1.268
CO <sub>2</sub>	22.000	22.176	22.414	22.000	22.320

$\text{CuH}(\text{PH}_3)_2$	
Reactant	TS
H	1.174
CO <sub>2</sub>	22.000

a) R(C-H) was taken to be the same as it in the TS of the CO<sub>2</sub> insertion into the Rh<sup>I</sup>-H bond.

Cu<sup>I</sup>-H bonds, important differences between them are found in Table 6.7. The CO<sub>2</sub> electron population at the TS is the greatest in the CO<sub>2</sub> insertion into the Rh<sup>III</sup>-H bond. However, the greatest electron population of CO<sub>2</sub> would arise from the short C-H distance between CO<sub>2</sub> and the H ligand at the TS of this insertion reaction. In this insertion, the CO<sub>2</sub> electron population increases least, when the C-H distance between CO<sub>2</sub> and the H ligand is taken to be the same as it in the TS of the CO<sub>2</sub> insertion into the Rh<sup>I</sup>-H bond. This means that the charge-transfer from the H ligand to CO<sub>2</sub> occurs least in the CO<sub>2</sub> insertion into the Rh<sup>III</sup>-H bond. The most weak charge-transfer from  $[\text{RhH}_2(\text{PH}_3)_3]^+$  to CO<sub>2</sub> would be related to the smallest H atomic population in the

reactant,  $[\text{RhH}_2(\text{PH}_3)_3]^+$  (see Table 6.7). This is one of the reasons for the considerably high  $E_a$  of this insertion reaction.

Now, let us start to discuss the TS geometry in terms of the bonding nature and the electron distribution at the TS. The TS of the  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{III}}\text{-H}$  bond is much product-like, as has been described above. This product-like TS can be explained by considering that the  $\text{Rh}^{\text{III}}\text{-H}$  bond is much stronger than the  $\text{Rh}^{\text{I}}\text{-H}$  and  $\text{Cu}^{\text{I}}\text{-H}$  bonds (vide supra). To break the strong  $\text{Rh}^{\text{III}}\text{-H}$  bond and to form the C-H bond between  $\text{CO}_2$  and the H ligand,  $\text{CO}_2$  must closely approach the H ligand, which leads to the short C-H distance and causes the highly bending distortion of the  $\text{CO}_2$  part. Corresponding to this geometry, the strong charge-transfer occurs from  $[\text{Rh}^{\text{III}}\text{H}_2(\text{PH}_3)_3]^+$  to  $\text{CO}_2$ , which accumulates considerable electron density on the  $\text{O}^1$  atom through the orbital mixing **A** of Scheme 6.1. As a result,  $\text{CO}_2$  can strongly interact with the unoccupied orbital of  $\text{Rh}^{\text{III}}$ , as shown in the orbital mixing **B** in Scheme 6.1. In fact, the  $\text{Rh}\text{-O}^1$  distance is very short the in TS like the usual coordinate bond, which suggests that the coordinate bond of formate is mostly formed at the TS. This situation of the TS would be considerably affected by the trans-influence of the co-existing ligand. It is well-known that the H ligand exhibits the strong trans-influence. To investigate the trans-influence of the  $\eta^1$ -formate ligand, we optimized the assumed structure **4** (see Figure 6.1) in which the  $\text{PRhO}^1$  angle was taken to be the same as it in TS. In **4**, the  $\text{Rh}\text{-O}^1$  distance is significantly short and the  $\text{Rh}\text{-H}$  distance is much longer than it in the reactant **1** and the product **5**.

This geometrical feature strongly suggests that the  $\eta^1$ -formate ligand exhibits the strong trans-influence. The geometry of TS is, therefore, much unfavorable because formate is going to be mostly formed at the trans-position of the H ligand. On the other hand, the unfavorable situation of this kind does not emerge in the  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{I}}\text{-H}$  and  $\text{Cu}^{\text{I}}\text{-H}$  bonds, as clearly shown in Figure 6.1 (see **6** and **7**). This is, therefore, one of the reasons for the considerably high  $E_a$  value of  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{III}}\text{-H}$  bond. This is also a reason that the  $\text{Rh-H}$  and  $\text{Rh-O}^1$  distances are longer in the TS **3** than in the product **5**; in **5**, formate can coordinate to  $\text{Rh}^{\text{III}}$  as a bidentate ligand and does not need to strongly coordinate to Rh through the  $\text{O}^1$  atom because  $\eta^2$ -formate can interact with Rh via the other  $\text{O}^2$  atom.

#### **6-4 Conclusion**

Basis set effects were examined in the  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{I}}\text{-H}$  and  $\text{Rh}^{\text{III}}\text{-H}$  bonds. Although use of ECP instead of all electron basis set for Rh causes little effects on the activation energy ( $E_a$ ) and the reaction energy ( $\Delta E$ ), introduction of polarization functions on  $\text{CO}_2$  considerably increases  $E_a$  and remarkably decreases the exothermicity. Electron correlation effects were investigated by using such methods as MP2 - MP4SDQ, SD-CI, and CCD. Although  $E_a$  and  $\Delta E$  somewhat fluctuate at MP2 and MP3, similar values of  $E_a$  and  $\Delta E$  are calculated with MP4, SD-CI, and CCD methods, and CCD values are intermediate between MP4SDQ and SD-CI values. When polarization functions were added on  $\text{CO}_2$ , introduction of electron

correlation changes  $E_a$  and  $\Delta E$  only a little. Consistent with these results, no instability of the HF wave-function was observed at the TS. This is not surprising because the H ligand moves toward  $\text{CO}_2$  as a hydride ligand, in other words, the C-H bond between  $\text{CO}_2$  and H ligand is formed not in a homolytic way but in a heterolytic way accompanied with the strong charge transfer from the H ligand to  $\text{CO}_2$ .

The  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{III}}\text{-H}$  bond reaches TS much more late than the other  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{I}}\text{-H}$  and  $\text{Cu}^{\text{I}}\text{-H}$  bonds, whereas the former is only slightly less exothermic than the  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{I}}\text{-H}$  bond. This is because the charge-transfer from  $[\text{RhH}_2(\text{PH}_3)_3]^+$  to  $\text{CO}_2$  is weak and  $\text{CO}_2$  must approach closely the H ligand to break the strong  $\text{Rh}^{\text{III}}\text{-H}$  bond. In the TS, therefore, formate is mostly formed and strongly interacts with Rh in a  $\eta^1$ -coordinating way at the trans-position of the H ligand. This geometrical feature is unfavorable because of the strong trans-influence of the H ligand. Thus, the  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{III}}\text{-H}$  bond requires the highest activation energy. In the other  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{I}}\text{-H}$  and  $\text{Cu}^{\text{I}}\text{-H}$  bonds, such situation does not emerge, and therefore, the activation energy of these insertion reactions is much lower than the  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{III}}\text{-H}$  bond.

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**Oxidative Addition of The Si-X  $\sigma$ -Bond to (X = H, C, or Si) Palladium (0) and Platinum (0) Complexes**

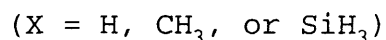
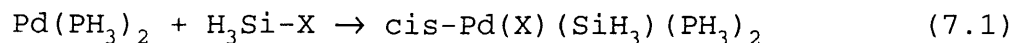
**7.1 Introduction**

Oxidative addition of the Si-X  $\sigma$ -bond (X = H, CH<sub>3</sub>, SiH<sub>3</sub> etc.) to transition metal complexes is of central significance in syntheses of various organosilicon compounds.<sup>1</sup> For instance, the oxidative addition of the Si-Si  $\sigma$ -bond is considered to be involved as a key process in platinum- and palladium-catalyzed bis-silylation of carbon-carbon,<sup>2-9</sup> carbon-nitrogen,<sup>10</sup> and carbon-oxygen<sup>11</sup> multiple bonds. In this context, interesting experimental works have been reported on stoichiometric oxidative addition of the Si-X  $\sigma$ -bond to transition metals.<sup>1,12-19</sup>

Although palladium(0) complexes have often been used as catalysts in the above-mentioned bis-silylation,<sup>1a,3-7,8c,d,9-11</sup> a previous theoretical work revealed that the palladium(0) complex was unfavorable for the oxidative addition of H-H, C-H, and C-C bonds.<sup>20</sup> Thus, knowledge of the Si-X oxidative addition to the palladium(0) complex is necessary to understanding well palladium-catalyzed syntheses of organosilicon compounds. Experimentally, bis(silyl)palladium complexes have been investigated well and several interesting results have been presented on their reductive elimination (i.e., the reverse reaction of the oxidative addition).<sup>21,22</sup> Besides the experimental work, the theoretical work is also expected to offer valid information on the Si-X oxidative addition to palladium(0) complexes.



In this chapter, oxidative addition of the Si-X  $\sigma$ -bond to Pd(PH<sub>3</sub>)<sub>2</sub> (eq 7.1) is theoretically investigated with the



ab initio MO/MP4 method, and compared with the same reaction of Pt(PH<sub>3</sub>)<sub>2</sub>.<sup>23</sup> Aims of this chapter are (1) to estimate the activation energy ( $E_a$ ) and the energy of reaction ( $\Delta E$ ) of eq 7.1, (2) to show similarities and differences between Pd(PH<sub>3</sub>)<sub>2</sub> and the Pt analogue, Pt(PH<sub>3</sub>)<sub>2</sub>, in the Si-X oxidative addition, and (3) to clarify the factors determining the reactivity of Pd(PH<sub>3</sub>)<sub>2</sub> in this oxidative addition.

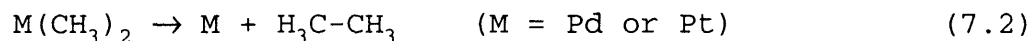
## 7.2 Computational Details

Ab initio MO/MP4 calculations were carried out with the Gaussian 86<sup>24a</sup> and 92<sup>24b</sup> programs. MP2 ~ MP4(SDQ) calculations were carried out with all the core orbitals excluded from the active space. Two kinds of basis sets, BS-I and BS-II, were mainly employed in this work; the BS-I was used for geometry optimization and the BS-II was used for MP2 ~ MP4(SDQ) calculations. In the BS-I, the 4s, 4p, 4d, 5s, and 5p orbitals of Pd were represented by a (5s 5p 4d)/[3s 3p 2d] set, where inner core electrons (up to 3d) were replaced with relativistic effective core potentials (ECPs).<sup>25</sup> MIDI-3 sets<sup>26</sup> were used for ligand atoms, except for MINI-1 set employed for PH<sub>3</sub>.<sup>26,27a</sup> In the BS-II, the 4s, 4p, 4d, 5s, and 5p orbitals of Pd were represented with a (5s 5p 3d)/[3s 3p 3d] set, where inner core electrons (up to 3d) were replaced with the same ECPs as those in the BS-I.<sup>25</sup> MIDI-4 sets<sup>26</sup> were used for Si, P, and C, and a (4s)/[2s] set was employed for H.<sup>27b</sup> In both BS-I and BS-II, the basis set

of Si was augmented with a d-polarization function.<sup>28</sup> In the BS-II, a p-polarization function<sup>27b</sup> was added to the basis set of H, when it directly coordinates to Pd.<sup>29</sup>

In the Si-Si, Si-C, and C-C oxidative additions, geometries of reactants, transition states (TS), and products were optimized with the energy gradient technique at Hartree-Fock (HF) level, where the geometry of PH<sub>3</sub> was taken from the experimental structure of the free PH<sub>3</sub> molecule<sup>30</sup> and the TS was determined by calculating the Hessian matrix. In the Si-H oxidative addition, however, geometries of reactants and product were optimized at the MP2 level, using the BS-I, because optimization of cis-Pd(H)(SiH<sub>3</sub>)(PH<sub>3</sub>)<sub>2</sub> at the HF level was failed (it led to the precursor complex, Pd(PH<sub>3</sub>)<sub>2</sub>(SiH<sub>4</sub>)). Geometry changes during this oxidative addition were optimized at the HF level, taking the Pd-Si distance as the reaction coordinate in the early stage of the reaction, the Si-H distance in the middle stage of the reaction, and the HPdSi angle in the late stage of the reaction. The TS was roughly determined from MP4(SDQ)/BS-II calculations performed for HF-optimized geometries (see below and Figure 7.3 for details).

In order to ascertain the reliability of the computational method employed here, the reductive elimination (eq 7.2) of a model complex, M(CH<sub>3</sub>)<sub>2</sub> (M = Pd or Pt), was examined because this reaction has been investigated well with theoretical methods of high



quality.<sup>20,31</sup> Geometries of M(CH<sub>3</sub>)<sub>2</sub> and the TS of eq 7.2 were optimized with the energy gradient technique at the HF level, using the BS-I. MP2 ~ MP4(SDQ), SD-CI, and coupled

cluster calculations were carried out with BS-II and BS-III; in the latter, Huzinaga-Dunning (9s 5p)/[3s 2p] set<sup>27b</sup> was used for C, but the same basis sets and ECPs as those in the BS-II were adopted for Pd and H. For Pt, a (5s 5p 3d)/[3s 3p 3d] set was employed with ECPs used for core electrons (up to 4f).<sup>25</sup>

### 7.3 Results and Discussion

#### 7-3-1 Reliability of Our Computational Method

Prior to discussion of the Si-X oxidative addition to  $\text{Pd}(\text{PH}_3)_2$ , we will compare our results on the reductive elimination of  $\text{M}(\text{CH}_3)_2$  (eq 7.2) with the results reported by Low and Goddard (LG)<sup>20</sup> and Siegbahn and Blomberg (SB),<sup>31</sup> in order to examine the reliability of our computational method employed here. In both the equilibrium structure of  $\text{M}(\text{CH}_3)_2$  and the TS structure of eq 7.2, the M-CH<sub>3</sub> distance optimized here is similar to that reported by SB, and the optimized bond angle is almost the same as those reported by LG and SB, whereas the M-CH<sub>3</sub> distance optimized by LG slightly differs from that of SB and ours (Table 7.1). The activation energy ( $E_a$ ) of the reductive elimination little depends on the basis sets (BS-II and BS-III) and the computational methods such as MP2 ~ MP4(SDQ), SD-CI, and CCD(ST4) methods (Table 7.2; see its footnote (d) for CCD(ST4)). Our  $E_a$  value for M = Pd agrees well with the  $E_a$  value of SB, but is larger than the  $E_a$  value of LG by ca. 10 kcal/mol. In the case of M = Pt, our  $E_a$  value is about 5 kcal/mol larger than the  $E_a$  value reported by LG. For the purpose of comparing the Pd reaction system with the Pt system, a difference in  $E_a$  between M = Pd and M = Pt should

**Table 7.1** Optimized Geometrical Parameters of  $M(\text{CH}_3)_2$  and the TS of Reductive Elimination ( $M = \text{Pd}$  or  $\text{Pt}$ )

		M = Pd			M = Pt	
		This Work	LG <sup>a</sup>	SB <sup>b</sup>	This Work	LG <sup>a</sup>
M(CH <sub>3</sub> ) <sub>2</sub>	R(M-CH <sub>3</sub> )	2.046	1.96	2.03	2.030	1.97
	∠CMC	88	92	89.9	98	98
TS	R(M-CH <sub>3</sub> )	2.185	2.34	2.17	2.258	2.34
	∠CMC	58	56	58.3	50	50
	R(C-C)	2.133	2.14	2.114	1.969	2.14

Bond length in Å and bond angle in degree.

a) Low and Goddard (Ref. 20). Pd; Basis sets and ECPs of Hay et al,<sup>32</sup> C; Dunning double- $\zeta$  contraction of Huzinaga's (9s 5p) primitive set,<sup>27b</sup> H; double- $\zeta$  contraction of Huzinaga's (4s) primitive set.<sup>27b</sup>

b) Siegbahn and Blomberg (Ref. 31). Pd; (17s 13p 9d 3f)/[7s 6p 4d 1f],<sup>33</sup> C; (9s 5p)/[3s 2p],<sup>27b</sup> H; (5s 1p)/[3s 1p].<sup>27c</sup>

be correctly calculated. This difference (36.6 kcal/mol) calculated here does not differ very much from that (40.8 kcal/mol) reported by LG. All these results suggest that the MP4(SDQ)/BS-II//HF/BS-I calculation (the MP4(SDQ)/BS-II calculation of the HF/BS-I optimized structure) is reliable at least in a semi-quantitative sense and in comparing the Si-X oxidative addition to  $\text{Pd}(\text{PH}_3)_2$  with the same reaction to  $\text{Pt}(\text{PH}_3)_2$ .

**Table 7.2** Activation Energy of the Reductive Elimination of  $M(\text{CH}_3)_2$  (kcal/mol unit)

		M = Pd		M = Pt	
		BS-II	BS-III	BS-II	BS-III
This	HF	20.0	19.9	57.4	57.3
Work	MP2	20.5	20.5	57.5	56.9
	MP3	23.6	23.7	60.1	59.9
	MP4DQ	22.5	22.5	59.0	58.7
	MP4SDQ	20.5	20.4	57.1	57.0
	SDCI (D) <sup>a</sup>	22.3	22.4	58.9	58.6
	SDCI (DS) <sup>b</sup>	22.9	22.9	58.9	58.8
	SDCI (P) <sup>c</sup>	22.7	22.7	59.1	58.7
	CCD (ST4) <sup>d</sup>	22.8	--	59.1	--
	-----				
LG	GVB-CI <sup>e</sup>	12.6 <sup>f</sup>		53.4	
SB	CCSD(T) <sup>g</sup>	23.3 <sup>h</sup>		--	

a) Davidson's correction for quadratic excitations. S. R. Langhoff and E. R. Davidson, *Int. J. Quant. Chem.*, **8**, 61 (1974).

b) Davidson and Silver's correction for quadratic excitations.<sup>40e</sup>

c) Pople's correction for quadratic excitations. J. A. Pople, R. Seeger, and R. Krishnan, *Int. J. Quant. Chem., Quant. Chem.*, **11**, 149 (1977).

d) Coupled Cluster (doubles) calculation with evaluation of contribution of single and triple excitations through fourth order using the CCD wavefunctions.

e) Low and Goddard (Ref. 20).

f) See footnote a) of Table 1 for the basis sets used.

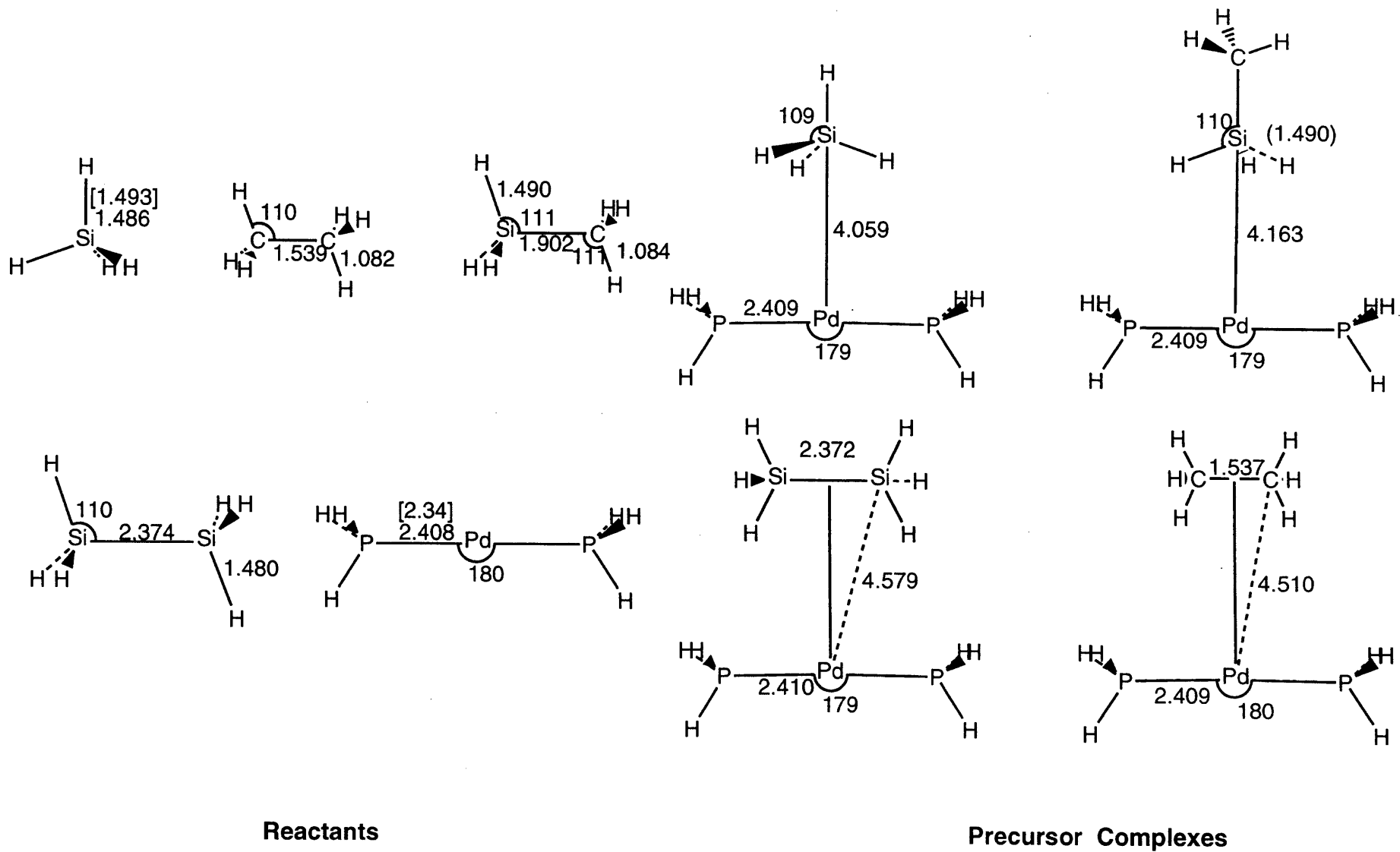
g) Siegbahn and Blomberg (Ref. 31).

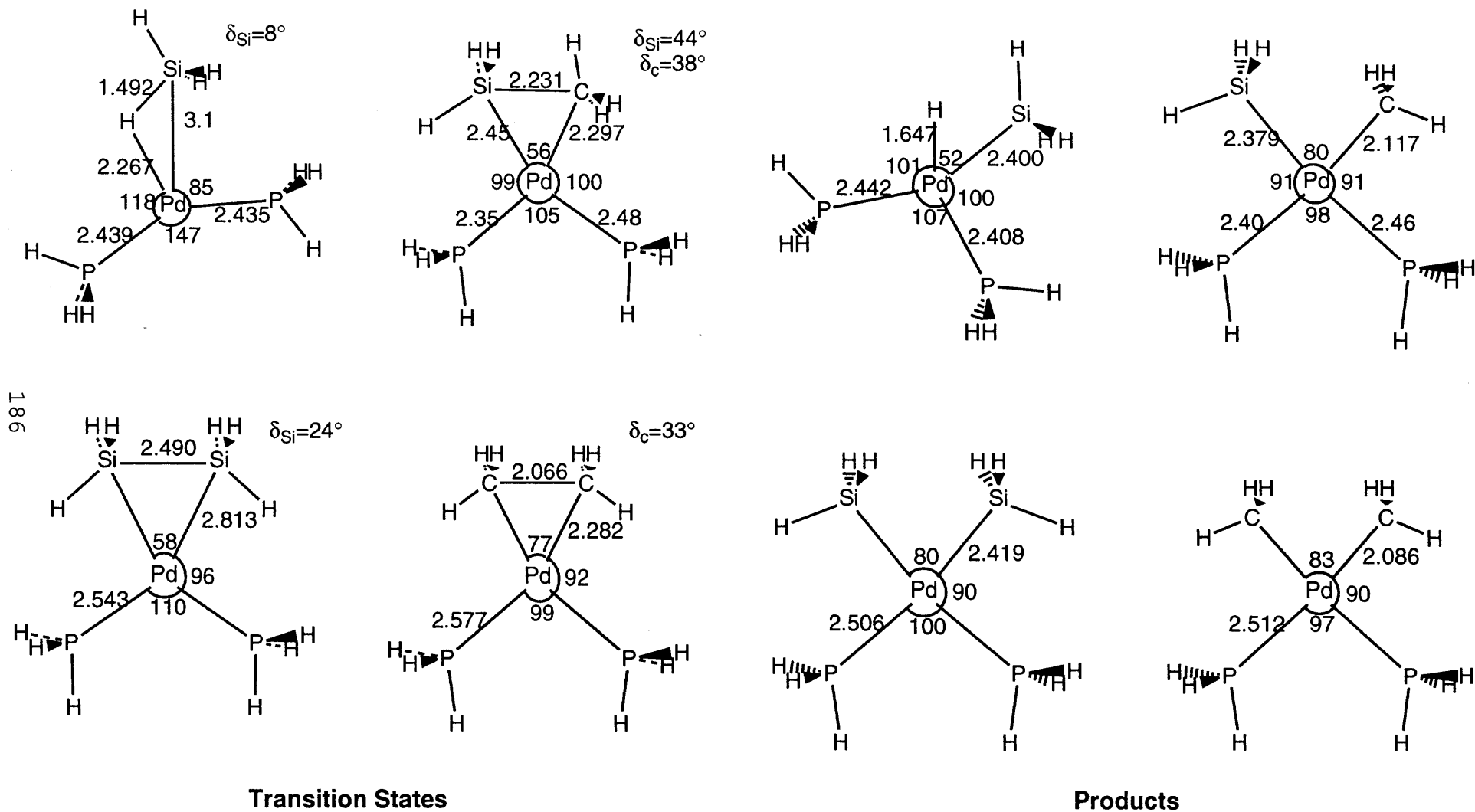
h) See footnote b) of Table 1 for the basis sets used.

### 7-3-2 Changes in Geometry and Energy in the Si-X Oxidative Addition

Now, we will start to consider the Si-X oxidative addition. It is often considered in this kind of oxidative addition that a substrate forms a precursor complex with a transition metal before reaching the TS.<sup>23,34</sup> Optimized geometries of reactants and precursor complexes are shown in Figure 7.1. In a precursor complex,  $\text{Pd}(\text{PH}_3)_2(\text{Si}_2\text{H}_6)$ , having a  $\text{C}_{2v}$ -like structure,<sup>35a,36</sup> the Pd-Si distance is very long (4.58 Å) and both  $\text{Pd}(\text{PH}_3)_2$  and  $\text{Si}_2\text{H}_6$  parts little distort ( $\angle\text{PPdP}=180^\circ$ ,  $R(\text{Si-Si})=2.37$  Å) like the precursor complex of the Pt analogue,  $\text{Pt}(\text{PH}_3)_2(\text{Si}_2\text{H}_6)$ .<sup>23</sup> The similar features are observed in the other precursor complexes,  $\text{Pd}(\text{PH}_3)_2(\text{C}_2\text{H}_6)$ ,<sup>36</sup>  $\text{Pd}(\text{PH}_3)_2(\text{SiH}_4)$ ,<sup>35b,36</sup> and  $\text{Pd}(\text{PH}_3)_2(\text{SiH}_3\text{CH}_3)$ .<sup>36</sup> Consistent with these geometrical features, all the precursor complexes yield very small stabilization energies like the Pt analogues<sup>23</sup> (Table 7.3): for instance, the stabilization energy of  $\text{Pd}(\text{PH}_3)_2(\text{Si}_2\text{H}_6)$  is only 3 kcal/mol (MP4(SDQ)) without the correction of basis set super position error (BSSE) and 1.6 kcal/mol with BSSE correction.<sup>37</sup> These values are too small for the usual coordinate bond, indicating that these complexes can be considered as a van der Waals complex.

At the TS of the Si-Si oxidative addition (Figure 7.2), the Si-Si distance (2.490 Å) is 0.12 Å longer than it in the free  $\text{Si}_2\text{H}_6$  (Figure 7.1), the  $\text{SiH}_3$  group is changing its direction toward Pd, and the Pd-SiH<sub>3</sub> distance is still 0.4 Å longer than it in the product, while the PPdP angle (110°) is very close to that in the product. At the TS of the Si-C oxidative addition,<sup>38</sup> the  $\text{Pd}(\text{PH}_3)_2$  part remarkably distorts





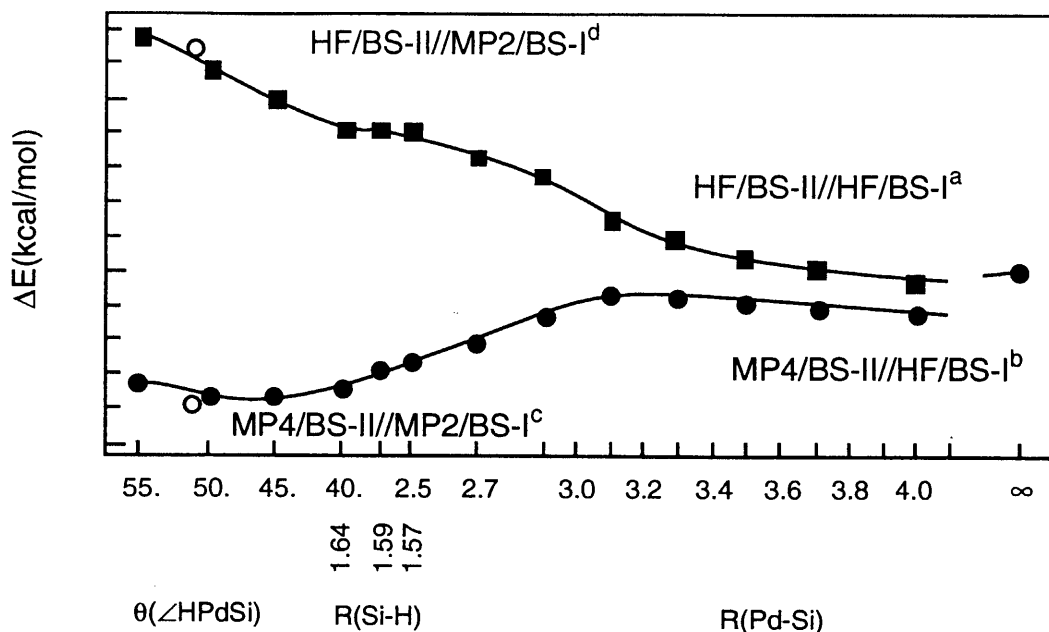
**Figure 7.2** Optimized geometries of transition states and products of the Si-X oxidative addition to  $\text{Pd}(\text{PH}_3)_2$  (Bond length in Å and bond angle in degree)



( $\angle \text{PPdP} = 105^\circ$ ), the Si-C distance lengthens by 0.33 Å, and the Pd-Si (2.450 Å) and Pd-C (2.297 Å) distances are longer than those in the product by only 0.07 and 0.18 Å respectively, suggesting that this TS is more product-like than the TS of the Si-Si oxidative addition. In the TS of the C-C oxidative addition, the PPdP angle is very small ( $99^\circ$ ) and the C-C distance is considerably long (2.066 Å), about 0.53 Å longer than it in the free  $\text{C}_2\text{H}_6$ , indicating that this TS is further product-like compared to the TS of the Si-C oxidative addition. It is noted that the PPdP angles in these TSs are much smaller than those in the TSs of the Pt reaction systems; for instance, the PPdP angle is  $110^\circ$  and PPtP angle is  $132^\circ$  for the Si-Si oxidative addition, the PPdP angle is  $95^\circ$  and the PPtP angle is  $110^\circ$  for the C-C oxidative addition, whereas  $\text{Si}_2\text{H}_6$  and  $\text{C}_2\text{H}_6$  parts in the TSs of Pd reaction systems are distorted to a similar extent to those in the TSs of Pt reaction systems. This interesting feature relates to the Pd d orbital energy, as will be discussed below.

As shown in Figure 7.3, the Si-H oxidative addition occurs with a very small barrier at the MP4(SDQ) level. Apparently, the HF optimization of  $\text{cis-Pd(H)(SiH}_3\text{)(PH}_3\text{)}_2$  leads to a precursor complex,  $\text{Pd(PH}_3\text{)}_2\text{(SiH}_4\text{)}$ , and therefore, we abandoned HF optimization of the TS. From the MP4(SDQ)/BS-II//HF/BS-I calculations of Figure 7.3, the TS is roughly determined at around  $R(\text{Pd-Si}) = 3.1 \text{ \AA}$ . In its geometry (Figure 7.2), the PPdP angle is  $147^\circ$ , much smaller than it in the reactant, whereas the  $\text{SiH}_4$  part little distorts and the Si-H distance little lengthens.

The activation barrier ( $E_a$ ) and the energy of reaction



**Figure 7.3** Energy changes<sup>a</sup> during the Si-H oxidative addition to  $\text{Pd}(\text{PH}_3)_2$ .  $R(\text{Pd-Si})$  and  $R(\text{Si-H})$  in Å and  $\theta$  in degree.

- HF/BS-II calculation for the geometry optimized by HF/BS-I calculation.
- MP4SDQ/BS-II calculation for the geometry optimized by HF/BS-I calculation.
- MP4SDQ/BS-II calculation for the geometry optimized by MP2/BS-I calculation.
- HF/BS-II calculation for the geometry optimized by MP2/BS-I calculation.

( $\Delta E$ ) of these reactions are compared in Table 7.3. The C-C oxidative addition to  $\text{Pd}(\text{PH}_3)_2$  occurs with a considerably high activation energy and a remarkably high endothermicity, as expected. The Si-Si oxidative addition, however, proceeds with a rather small activation energy and a considerable exothermicity, indicating that although the C-C oxidative addition to  $\text{Pd}(\text{PH}_3)_2$  is difficult very much, the

**Table 7.3** Energy Change in Oxidative Additions<sup>a</sup> (kcal/mol unit)

	M = Pd					M = Pt
	HF	MP2	MP3	MP4DQ	MP4SDQ	MP4SDQ
(A) C-C Oxidative Addition						
Reactants <sup>c</sup>	-889.0641	-889.5403	-889.5659	-889.5938	-889.6042	-881.9800
Precursor	-0.2(0.4)	-1.3(-1.1)	-1.2(-0.36)	-1.2(-0.6)	-1.4(-0.8)	-1.1(-0.8)
TS	82.8(85.3)	56.9(59.3)	63.5(65.9)	61.0(63.5)	56.8(59.3)	66.0(68.5)
Product	50.9	27.9	29.5	30.7	30.5	5.2
(B) Si-Si Oxidative Addition						
Reactants <sup>c</sup>	-1390.6068	-1391.0659	-1391.0976	-1391.1259	-1391.1380	-1383.5124
Precursor	-0.6(0.8)	-2.9(-1.4)	-2.7(-1.3)	-2.7(-1.2)	-3.0(-1.6)	-3.7(-2.6)
TS	21.2(24.8)	9.8(13.4)	11.9(15.5)	11.1(14.7)	8.2(11.9)	13.7(17.0)
Product	9.0	-21.1	-13.3	-16.7	-18.1	-46.4
(C) Si-C Oxidative Addition						
Reactants <sup>c</sup>	-1139.8416	-1140.3050	-1140.3346	-1140.3625	-1140.3740	-1132.7497
Precursor	-0.6(0.5)	-2.3(-1.2)	-2.1(-1.0)	-2.2(-1.1)	-2.5(-1.4)	-2.3(-1.4)
TS	42.9(46.6)	-15.1(18.9)	22.2(25.9)	19.2(22.9)	16.3(20.1)	24.9(28.1)
Product	34.0	5.9	9.9	8.7	8.1	-14.1

(Continued to be the next page)

(D) Si-Si Oxidative Addition

Reactants <sup>c</sup>	-1100.8494	-1101.2327	-1101.2542	-1101.2809	-1101.2920	-1093.6616 <sup>e</sup>
Precursor	-2.2(-1.2)	-1.8(-0.8)	-2.5(-1.5)	-2.1(-1.1)	-2.4(-1.4)	-6.1(-5.8)
TS	2.6(4.4)	-0.3(1.5)	-0.4(1.5)	-0.3(1.6)	-1.3(0.5)	-6.3(-4.0)
Product	12.5	-9.5	-4.1	-6.6	-8.1	-31.1

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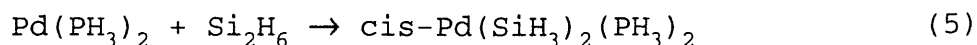
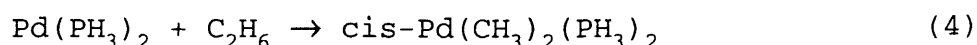
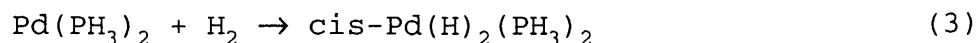
a) In parenthesis; basis set superposition error (BSSE) was corrected with the counter-poise method.<sup>37</sup>

b) ref. 23. c) Sum of the total energies of reactants (hartree unit). d) Pd(PH<sub>3</sub>)<sub>2</sub> and SiH<sub>4</sub> were optimized at the MP<sub>2</sub> level, using the BS-I. (e) Values differ from those of ref. 23, because a p-polarization function was added to H coordinating to Pt.

Si-Si oxidative addition to Pd(PH<sub>3</sub>)<sub>2</sub> can proceed easily. The Si-C oxidative addition is endothermic, and the activation energy of this reaction is much lower than that of the C-C oxidative addition but considerably higher than that of the Si-Si oxidative addition. The Si-H oxidative addition can proceed with a very small barrier (ca. 2 kcal/mol at MP4(SDQ)/BS-II) and a moderate exothermicity (8 kcal/mol at MP4(SDQ)/BS-II). In summary, the activation energy of oxidative addition to Pd(PH<sub>3</sub>)<sub>2</sub> increases in the order Si-H < Si-Si < Si-C << C-C, and the exothermicity increases in the order C-C < Si-C < Si-H < Si-Si. These orders are the same as those in the oxidative addition to Pt(PH<sub>3</sub>)<sub>2</sub>, and the reasons have been discussed previously.<sup>23</sup>

### 7-3-3 A Comparison of Reactivity between Pd(PH<sub>3</sub>)<sub>2</sub> and Pt(PH<sub>3</sub>)<sub>2</sub>

First, let us examine the C-C oxidative addition. A significant difference between Pd(PH<sub>3</sub>)<sub>2</sub> and Pt(PH<sub>3</sub>)<sub>2</sub> is observed in this reaction; the C-C oxidative addition to Pd(PH<sub>3</sub>)<sub>2</sub> is significantly endothermic in contrast to the same reaction to Pt(PH<sub>3</sub>)<sub>2</sub> which is only slightly endothermic (Table 7.3). The other Si-X oxidative addition to Pd(PH<sub>3</sub>)<sub>2</sub> is also much less exothermic (or much more endothermic) than the corresponding reaction to Pt(PH<sub>3</sub>)<sub>2</sub>. This difference between Pt(PH<sub>3</sub>)<sub>2</sub> and Pd(PH<sub>3</sub>)<sub>2</sub> is easily interpreted in terms of bond energies. Bond energies are estimated at the MP2 ~ MP4(SDQ) levels, considering the following reactions;



**Table 7.4** Estimated Pd-X and Pt-X (X = H, CH<sub>3</sub>, or SiH<sub>3</sub>) Bond Energies (kcal/mol unit)

	Pd-H	Pd-CH <sub>3</sub>	Pd-SiH <sub>3</sub>	Pt-H	Pt-CH <sub>3</sub>	Pt-SiH <sub>3</sub>
MP2	47.0	29.5	47.0	59.9	42.2	64.4
MP3	49.1	27.7	43.3	62.2	40.2	60.3
MP4DQ	49.5	26.9	44.6	62.1	39.4	59.4
MP4SDQ	48.9	27.1	45.4	61.7	39.7	61.5

a) Values differ from those of ref. 23, because a p-polarization was added to H coordinating to Pt

Apparently shown in Table 7.4, the Pd-X bond energy is smaller than the corresponding Pt-X bond energy. Thus, the oxidative additions of the Si-Si, Si-C, Si-H, and C-C bonds to Pd(PH<sub>3</sub>)<sub>2</sub> are much less exothermic (or much more endothermic) than the corresponding reaction with Pt(PH<sub>3</sub>)<sub>2</sub>.

Interestingly, the activation energy (E<sub>a</sub>) of the Si-X oxidative addition to Pd(PH<sub>3</sub>)<sub>2</sub> is slightly lower than (or similar to) that of the corresponding reaction with Pt(PH<sub>3</sub>)<sub>2</sub>, whereas the former is much less exothermic (or much more endothermic) than the latter. If the bond energy was an only determining factor for the E<sub>a</sub> value, the oxidative addition to Pd(PH<sub>3</sub>)<sub>2</sub> would always require a considerably higher E<sub>a</sub> value than the corresponding oxidative addition to Pt(PH<sub>3</sub>)<sub>2</sub>. Thus, the rather low E<sub>a</sub> value indicates that the other factor is important in determining the activation barrier. At the TS, the charge-transfer from the d<sub>xz</sub> orbital of Pd(PH<sub>3</sub>)<sub>2</sub> to the σ\*-orbital of the Si-X bond is necessary

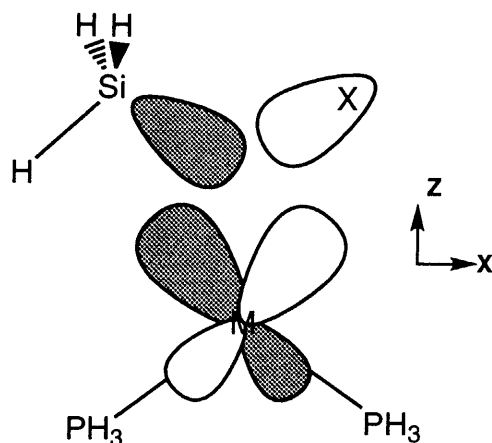
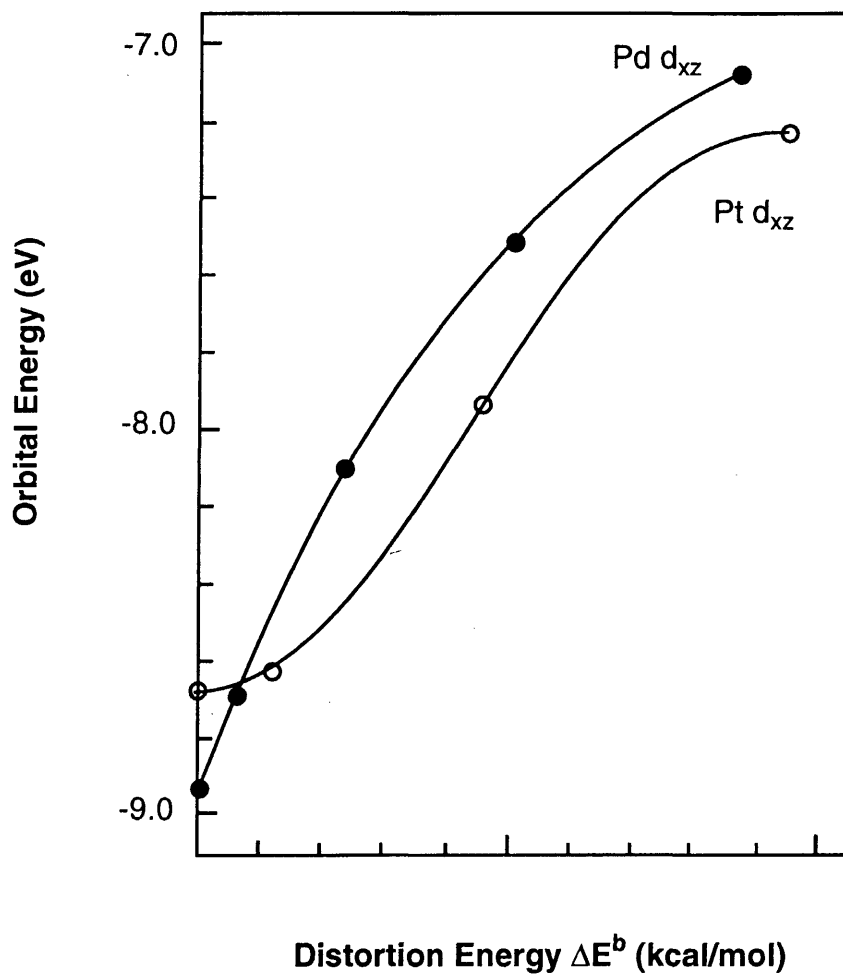


Chart 7.1

to break the Si-X  $\sigma$ -bond (see Chart 7.1 for  $d_{xz}$  and  $\sigma^*$ ), as well known.<sup>34,39</sup> This charge-transfer interaction is, in general, considered to be weaker in the Pd atom than in the Pt atom because Pd takes a  $d^{10}$  electron configuration as its ground state but Pt takes a  $d^9s^1$  configuration.<sup>20</sup> The situation, however, changes upon going to  $M(\text{PH}_3)_2$  from the bare M atom (M = Pd or Pt). The  $d^{10}$  state of  $\text{Pt}(\text{PH}_3)_2$  was calculated at the SD-CI level<sup>40</sup> to be 62 kcal/mol more stable than the  $^1B_1(d^9s^1)$  state, where the BS-II was used and the geometry of  $\text{Pt}(\text{PH}_3)_2$  as taken to be the same as in the TS of the Si-Si oxidative addition.<sup>23</sup> This result suggests that the situation of d orbital is similar in  $\text{Pd}(\text{PH}_3)_2$  and  $\text{Pt}(\text{PH}_3)_2$ . Furthermore,  $\text{Pd}(\text{PH}_3)_2$  is more flexible for the PPdP bending and needs smaller distortion energy ( $E_{\text{dist}}$ ) to cause the bending than  $\text{Pt}(\text{PH}_3)_2$  (note that  $\text{Pd}(\text{PH}_3)_2$  is linear at the equilibrium structure but takes a bending structure at the TS, as shown in Figures 7.1 and 7.2); when the PMP



**Figure 7.4** Relation between the  $d_{xz}$  orbital energy and the bending of  $M(\text{PH}_3)_2$  ( $M = \text{Pd}$  or  $\text{Pt}$ )<sup>a</sup>

a) Only the PMP angle was changed with the M-P distance fixed to that of the equilibrium structure.

b)  $E_{\text{dist}}$  was calculated at the MP4SDQ level.



**Table 7.5** Distortion Energy ( $E_{\text{dist}}$ ),  $d_{xz}$  orbital energy ( $\epsilon(d_{xz})$ ), and Ionization Potential ( $I_p(d_{xz})$ ).

	Pd(PH <sub>3</sub> ) <sub>2</sub>	Pt(PH <sub>3</sub> ) <sub>2</sub>
$E_{\text{dist}}^{\text{a}}$	47.0	29.5
$\epsilon(d_{xz})^{\text{b}}$	49.1	27.7
$I_p(d_{xz})$	49.5	26.9

a)  $E_t(\text{M}(\text{PH}_3)_2)_{\text{at TS}} - E_t(\text{M}(\text{PH}_3)_2)_{\text{eq}}$  at the MP4SDQ level. b) HS/BS-II calculation. c) SD-CI/BS-II. See ref. 40 and 41 for details of calculation.

angle ( $M = \text{Pd}$  or  $\text{Pt}$ ) is taken to be  $120^\circ$ ,  $E_{\text{dist}} = 19.1$  kcal/mol for  $\text{Pt}(\text{PH}_3)_2$  and 10.2 kcal/mol for  $\text{Pd}(\text{PH}_3)_2$  (at the MP4(SDQ) level). This bending of  $\text{M}(\text{PH}_3)_2$  pushes up the  $d_{xz}$  orbital energy. As shown by a relation between  $E_{\text{dist}}$  and the  $d_{xz}$  orbital energy (Figure 7.4), the  $d_{xz}$  orbital in  $\text{Pd}(\text{PH}_3)_2$  rises in energy to a greater extent than it in  $\text{Pt}(\text{PH}_3)_2$ , and the former lies higher in energy than the latter at the same distortion energy. The  $d_{xz}$  orbital energy ( $\epsilon(d_{xz})$ ), the ionization potential from the  $d_{xz}$  orbital ( $I_p(d_{xz})$ ),<sup>41</sup> and the  $E_{\text{dist}}$  value are compared between  $\text{Pd}(\text{PH}_3)_2$  and  $\text{Pt}(\text{PH}_3)_2$  in Table 7.5, where geometries of  $\text{Pd}(\text{PH}_3)_2$  and  $\text{Pt}(\text{PH}_3)_2$  were taken to be the same as the distorted structures in the TS of the Si-Si oxidative addition. It is noted that although the bending ( $\langle \text{PPdP} = 110^\circ$ ) of  $\text{Pd}(\text{PH}_3)_2$  is much greater than that ( $\langle \text{PPtP} = 132^\circ$ ) of  $\text{Pt}(\text{PH}_3)_2$ , the  $E_{\text{dist}}$  value of the former is slightly larger than that of the latter by only 1.7 kcal/mol (MP4(SDQ)). Furthermore, the  $d_{xz}$  orbital in

$\text{Pd}(\text{PH}_3)_2$  lies at a slightly higher energy than it in  $\text{Pt}(\text{PH}_3)_2$ , and the  $I_p(d_{xz})$  is almost the same in both  $\text{Pd}(\text{PH}_3)_2$  and  $\text{Pt}(\text{PH}_3)_2$ . All these results indicate that  $\text{Pd}(\text{PH}_3)_2$  can easily distort with the smaller distortion energy than  $\text{Pt}(\text{PH}_3)_2$ , and the  $d_{xz}$  orbital of  $\text{Pd}(\text{PH}_3)_2$  taking the distorted structure like in the TS lies at a relatively high energy level, similar to it in  $\text{Pt}(\text{PH}_3)_2$ . Accordingly, the charge-transfer interaction is easily formed between the  $d_{xz}$  orbital of  $\text{Pd}(\text{PH}_3)_2$  and the Si-X  $\sigma^*$  orbital. Thus, the Si-X oxidative addition to  $\text{Pd}(\text{PH}_3)_2$ , as well as the oxidative addition to  $\text{Pt}(\text{PH}_3)_2$ , easily occurs in spite of the low exothermicity of the former.

#### 7.4 Conclusions

Finally, let us mention here the reductive elimination of  $\text{cis-M}(\text{SiH}_3)_2(\text{PH}_3)_2$ . The activation barrier of the reductive elimination is estimated at the MP4(SDQ) level to be 31.3 kcal/mol for  $M = \text{Pd}$  and 60.0 kcal/mol for  $M = \text{Pt}$ ,<sup>23</sup> suggesting that the reductive elimination is much difficult in  $\text{cis-Pt}(\text{SiH}_3)_2(\text{PH}_3)_2$  but rather easy in  $\text{cis-Pd}(\text{SiH}_3)_2(\text{PH}_3)_2$ . The activation barrier of the Si-C reductive elimination from  $\text{cis-Pd}(\text{SiH}_3)(\text{CH}_3)(\text{PH}_3)_2$  is also estimated to be 8.2 kcal/mol at the MP4(SDQ) level, showing that this reductive elimination proceeds much more easily than the Si-C reductive elimination from  $\text{cis-Pt}(\text{SiH}_3)(\text{CH}_3)(\text{PH}_3)_2$  ( $E_a=42.2$  kcal/mol). Thus, we can expect that the palladium(0) complex is more useful as a catalyst for the reaction including both oxidative addition and reductive elimination of Si compounds than the platinum(0) complex; for instance, if the insertion of alkene and alkyne into the Pd-SiH<sub>3</sub> bond

easily occurs, the palladium(0) complex is more appropriate for the bis-silylation of alkenes, alkynes, dienes, etc. than the platinum(0) complex.

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- (36) The structure shown in Figure 7.1 corresponds to the most stable structure of the Pt's precursor complex.<sup>23</sup> The other structures were not calculated. Even if the other structure was more stable than that in Figure 7.1, the energy stabilization would be absolutely small, and therefore, E<sub>a</sub> would be little influenced, like in the Pt analogues.<sup>23</sup>
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### General Conclusion

In part I of this thesis, coenzyme functions of thiamin diphosphate and biotin are investigated theoretically. Thiamin diphosphate participates in enzymic decarboxylation of pyruvic acid and biotin performs carboxylation of organic substrate by utilizing bicarbonate and ATP.

In chapter 2, the decarboxylation reaction of lactylthiazolium was investigated with AM1 and ab initio MO/MP2 methods, where 2-lactylthiazolium was adopted here as a model of thiamin diphosphate. The decarboxylation step is much difficult to investigate experimentally, probably owing to high reactivity of 2-lactylthiazolium. Theoretical method is useful and expected to offer detailed knowledge on the reaction. The results and new findings obtained are summarized as follows.

- (1) In the decarboxylation of 2-lactylthiazolium, the activation barrier ( $E_a$ ) is estimated to be very small and the calculated exothermicity ( $E_{exo}$ ) is considerably large;  $E_a = 1.5$  kcal/mol (AM1), 3.9 kcal/mol (MP2/MIDI-4), 4.4 kcal/mol (MP2/6-31G), and  $E_{exo} = 23.8$  kcal/mol (AM1). Thus, decarboxylation of lactylthiazolium smoothly occurs.
- (2) Two water molecules increase the activation barrier to 5.6 kcal/mol and decrease the exothermicity to 14.7 kcal/mol (AM1). An additional water molecule interacting with the thiazolium ring further increases the activation barrier to 19.0 kcal/mol and significantly decreases the exothermicity to -2.1

kcal/mol (i.e., the reaction becomes endothermic). This result agrees well with Lienhard's experiment, and clearly indicates that the main role of thiamin is desolvation.

- (3) As the decarboxylation proceeds, the  $C^2-C^{2\alpha}$  and  $C^2-N$  bonds are changing to the corresponding double and single bonds respectively, and the product takes the typical enamine structure. This result, as well as Jordan's experiments, clearly supports that the enamine intermediate is indeed on the reaction pathway.
- (4) Decarboxylation reactions of 2-lactyloxazolium and 2-lactylimidazolium are theoretically investigated with the AM1 method, to compare their reactivities with that of 2-lactylthiazolium. Products of their decarboxylations also take the enamine structure. In their decarboxylations, the activation barrier is slightly higher than that of 2-lactylthiazolium; 2.8 kcal/mol for 2-lactyloxazolium and 6.4 kcal/mol for 2-lactylimidazolium, but the exothermicity is somewhat smaller in 2-lactyloxazolium and significantly smaller in 2-lactylimidazolium (3.9 kcal/mol) than in 2-lactylthiazolium. Thus, the decarboxylation reactivity decreases in the order thiazolium > oxazolium > imidazolium. This decreasing order is interpreted in terms of the  $\pi^*$  orbital of the azolium ring. Since the energy level of its  $\pi^*$  orbital lowers in the order imidazolium > oxazolium > thiazolium, HOMO of 2-hydroxyethylazolium lowers in the same order, which results in the most weak  $C^{2\alpha}-CO_2$  binding of 2-lactylthiazolium. Accordingly, the decarboxylation of 2-lactylthiazolium proceeds most easily. The  $\pi^*$  orbital

of the azolium ring would be stabilized in energy by highly polarizable and diffuse orbitals of the S atom.

In chapter 3, structure and bonding nature of carboxyimidazolidone were theoretically investigated as a model of carboxybiotin with ab initio MO/MP4, SD-CI, and CCD methods. Three isomers, N-carboxyimidazolidone **1**, O-carboxyimidazolidone **2**, and the  $\eta^2$ -side-on carboxyimidazolidone **3** were examined here. The important results are summarized as follows:

- (1) Imidazolidone can be adopted as a reasonable model of biotin because imidazolidone and methylbiotin have very similar geometry, electron distribution, and  $\pi$  and  $\pi^*$  orbital energies. However, more simple compounds such as  $\text{CH}_3\text{NH}_2$  and  $\text{CH}_3\text{NH}(\text{CHO})$  cannot be considered as a good model of biotin unlike imidazolidone.  $\text{CH}_3\text{NH}(\text{CONH}_2)$  seems reasonable as a model of biotin, because the  $\text{CO}_2$  binding energy to  $\text{CH}_3\text{NH}(\text{CONH}_2)$  is almost the same as that of carboxyimidazolidone. These results suggest that the urea structure is important in the  $\text{CO}_2$  binding with biotin.
- (2) In **1** and **2**,  $\text{CO}_2$  lies on the molecular plane. The perpendicular structure is less stable than the planar one by ca. 6 kcal/mol for **1** and 10 kcal/mol for **2** at the MP4SDQ/6-31G level. The binding energy of  $\text{CO}_2$  in **1** is much greater than that of **2** by ca. 12 kcal/mol, indicating that **1** is more stable than **2**. This is in accord with the experimental result that N-carboxybiotin is isolated in the biotin-dependent enzymic reactions. It is noted that geometries, electron distribution, and frontier orbitals of **1** and **2** resemble well those of  $\eta^1$ -C

coordinated CO<sub>2</sub> complexes of transition metal. The CO<sub>2</sub> binding energy of  $\eta^2$ -side-on carboxyimidazolidone **3** is much smaller than those of **1** and **2**, and geometry optimization of **3** led to **1**. Thus, the  $\eta^2$ -side-on CO<sub>2</sub> adduct would not exist in the reaction of biotin. The CO<sub>2</sub> part in **1** is considerably activated for an electrophile like it in the transition metal complex. Considering that the several  $\eta^1$ -C coordinated CO<sub>2</sub> complexes of transition metal serve as a key intermediate in electrochemical reduction of CO<sub>2</sub>, we can expect that biotin, imidazolidone, and their analogues would be useful as an organic catalyst for electrochemical reduction of CO<sub>2</sub>.

- (3) In carboxyimidazolidone, the charge-transfer from deprotonated imidazolidone to CO<sub>2</sub> strongly occurs. The electron population of CO<sub>2</sub> increases in the order **3** < **2** < **1**. The O<sup>1</sup> and O<sup>2</sup> atomic populations increase but the C atomic population decreases upon formation of carboxyimidazolidone, **1** and **2**. This electron distribution can be interpreted in terms of the bonding interaction between the donor orbital ( $\phi_{\text{donor}}$ ) of deprotonated imidazolidone and the CO<sub>2</sub>  $\pi^*$  orbital into which the  $\pi$  orbital of CO<sub>2</sub> mixes in an anti-bonding way with  $\phi_{\text{donor}}$ .
- (4) Energy decomposition analysis of the interaction between deprotonated imidazolidone and CO<sub>2</sub> also shows that the charge-transfer from deprotonated imidazolidone to CO<sub>2</sub> (the CTPLXA term) largely contributes to the CO<sub>2</sub> binding energy. The difference in stability between **1** and **2** mainly arises from this term. This is because  $\phi_{\text{donor}}$  of deprotonated imidazolidone expands more largely

on the N atom than on the O atom. Consequently, **1** can receive greater stabilization energy from the CTPLXA term than **2**.

- (5) The electron distribution and frontier orbitals indicate the possibility that the electrophile and cationic species interact with the O atom of CO<sub>2</sub> to activate it for the carboxyl-transfer reaction.

In Part II, several elementary reactions involved in transition-metal catalytic cycles are theoretically investigated. The first is the CO<sub>2</sub> insertion into the M-H and M-R (R = alkyl) bonds, the next is the C<sub>2</sub>H<sub>4</sub> insertion into the Cu(I)-R bond, and the last is the oxidative addition of the Si-X  $\sigma$ -bond to the palladium (0) complex.

In chapter 4, ab initio MO/MP4, SD-CI, and CCD (coupled cluster with double substitution calculations were carried out on the CO<sub>2</sub> insertion into the Cu(I)-R bond (R = H, CH<sub>3</sub>, or OH) and the C<sub>2</sub>H<sub>4</sub> insertion into the Cu(I)-R (R = H and CH<sub>3</sub>). Many important findings are reported, as follows;

- (1) The activation energy ( $E_a$ ) is calculated to be very low (ca. 4 - 5 kcal/mol) for the CO<sub>2</sub> insertion into the Cu-H bond, relatively high (9 - 10 kcal/mol) for the C<sub>2</sub>H<sub>4</sub> insertion into the Cu-H bond, and very high (23 - 30 kcal/mol) for the C<sub>2</sub>H<sub>4</sub> insertion into the Cu-CH<sub>3</sub> bond. These results suggest that the C<sub>2</sub>H<sub>4</sub> insertion into the Cu-R bond is much more difficult than the CO<sub>2</sub> insertion into the Cu-R bond.
- (2) The difference of  $E_a$  between CO<sub>2</sub> and C<sub>2</sub>H<sub>4</sub> insertion reactions can be interpreted in terms of  $\pi$  and  $\pi^*$  orbitals of CO<sub>2</sub> and C<sub>2</sub>H<sub>4</sub>; because the  $\pi$  orbital of C<sub>2</sub>H<sub>4</sub> lies higher in energy than that of CO<sub>2</sub>, the exchange

repulsion between  $C_2H_4$  and R is much larger than that between  $CO_2$  and R, leading to the higher  $E_a$  value of the  $C_2H_4$  insertion. Since the  $\pi^*$  orbital of  $CO_2$  becomes more stable than that of  $C_2H_4$  with increasing distortion, the charge-transfer from the metal part to  $CO_2$  is greater than the charge-transfer from the metal part to  $C_2H_4$ .

- (3) The exothermicity of the  $CO_2$  insertion is much greater than that of the  $C_2H_4$  insertion. The main reason for the greater exothermicity of the  $CO_2$  insertion is that the Cu-OC(O)H bond energy is larger than the Cu- $C_2H_5$  and Cu- $CH_3$  bond energy by ca. 50 kcal/mol.  $CO_2$  is inserted into the Cu-OH bond with no barrier. This is because the HOMO of  $Cu(OH)(PH_3)_2$  mainly consists of the lone-pair type orbital of  $OH^-$  and the bonding interaction between  $CO_2$  and OH can be formed without weakening of the Cu-OH bond. However, the exothermicity of this insertion is smaller than that of the other  $CO_2$  insertion, since the Cu-OC(O)OH bond energy is about 29 kcal/mol larger than the Cu-OH bond energy (remember that Cu-OC(O)R bond energy is about 50 kcal/mol larger than the Cu- $CH_3$  bond energy).
- (4) From the above result (3), one can predict that a primarily important factor for the  $CO_2$  insertion is the presence of a lone-pair type orbital of R which is not used for coordination to Cu. When the R ligand possesses such a lone-pair type orbital, the bonding interaction between this lone-pair type orbital and the LUMO of  $CO_2$  can be formed without weakening of the Cu-R bond. This situation facilitates the  $CO_2$  insertion into the Cu-R bond.



In chapter 5, the CO<sub>2</sub> insertion into the Rh(I)-H bond of RhH(PH<sub>3</sub>)<sub>3</sub> was theoretically investigated by ab initio MO/MP4, SD-CI and coupled cluster (CCD) calculations. Results to be noted are summarized as follows:

- (1) The CO<sub>2</sub> insertion into the Rh(I)-H bond easily occurs with an activation barrier of ca. 16 kcal/mol and exothermicity of ca. 24 kcal/mol at the SD-CI level, yielding Rh(η<sup>1</sup>-OC(O)H)(PH<sub>3</sub>)<sub>3</sub>. This activation barrier is higher and the exothermicity is lower than those of the similar CO<sub>2</sub> insertion into the Cu(I)-H bond of CuH(PH<sub>3</sub>)<sub>2</sub> in which activation barrier is 3.5 kcal/mol and the exothermicity is ca. 40 kcal/mol at the SD-CI level.
- (2) The higher activation energy of the Rh reaction system results from the facts that the Rh(I)-H bond is stronger than the Cu(I)-H bond by ca. 28 kcal/mol at the MP4SDQ level, the negative electrostatic potential of RhH(PH<sub>3</sub>)<sub>3</sub> is smaller than that of CuH(PH<sub>3</sub>)<sub>2</sub>, and the EX repulsion between CO<sub>2</sub> and RhH(PH<sub>3</sub>)<sub>3</sub> is greater than that between CO<sub>2</sub> and CuH(PH<sub>3</sub>)<sub>2</sub>. The lower exothermicity of CO<sub>2</sub> insertion into the Rh(I)-H bond is also due to the stronger Rh(I)-H bond than the Cu(I)-H bond, because the difference between Rh(I)-OC(O)H and Cu(I)-OC(O)H bonds is considerably small.
- (3) The transition state of the Rh reaction system has a shorter C-H distance between CO<sub>2</sub> and the H ligand than it in the transition state of the Cu reaction system. The reason of the short C-H distance is the strong Rh(I)-H bond; in the transition state of the Rh reaction system, CO<sub>2</sub> must approach the H ligand to a greater extent than in the transition state of the Cu reaction system, so as to break the strong Rh(I)-H bond. The

RhHC angle at the transition state is much different between two reaction systems; this angle is  $145^\circ$  in the Rh reaction system but only  $105^\circ$  in the Cu reaction system. The larger RhHC angle arises from the strong EX repulsion between the occupied  $4d_{xz}$  orbital of Rh and the occupied  $\pi$  and  $n\pi$  orbitals of  $\text{CO}_2$ . The Rh  $4d_{xz}$  orbital more expands than the Cu  $3d_{xz}$  orbital, which gives rise to the stronger EX repulsion with  $\text{CO}_2$  in the Rh reaction system.

- (4) From these results, one can predict that the  $\text{CO}_2$  insertion into the M-H bond easily occurs, when the M-H bond is weak, the electrostatic potential of the metal hydride complex is negatively large, and the expanse of the  $d_\pi$  orbital is small.

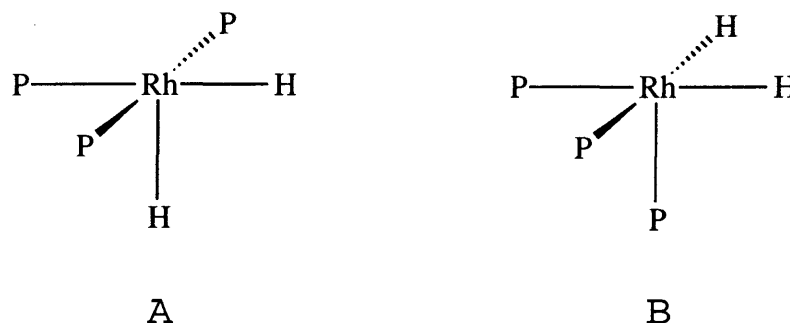
In chapter 6, the  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{III}}\text{-H}$  bond was theoretically investigated with ab initio MO/MP4, SD-CI and CCD methods. Electron correlation effects and basis set effects on the activation energy ( $E_a$ ) and the reaction energy ( $\Delta E$ ) are also examined. The  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{III}}\text{-H}$  bond are compared with the similar  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{I}}\text{-H}$  and  $\text{Cu}^{\text{I}}\text{-H}$  bonds investigated in chapters 4 and 5.

- (1) Electron correlation effects were investigated by using such methods as MP2 - MP4SDQ, SD-CI, and CCD. Although  $E_a$  and  $\Delta E$  somewhat fluctuate at MP2 and MP3, similar values of  $E_a$  and  $\Delta E$  are calculated with MP4, SD-CI, and CCD methods. This result clearly shows that discussion of the  $E_a$  and  $\Delta E$  of  $\text{CO}_2$  insertion into the M-H bond should be based on calculations including electron correlation effects, at least, at the MP4SDQ level.
- (2) Basis set effects were examined in the  $\text{CO}_2$  insertion

into the  $\text{Rh}^{\text{I}}\text{-H}$  and  $\text{Rh}^{\text{III}}\text{-H}$  bonds. Although use of the effective core potential (ECP) instead of all electron basis set for Rh causes little effects on the  $E_a$  and  $\Delta E$ , introduction of polarization functions on  $\text{CO}_2$  considerably increases  $E_a$  and remarkably decreases the exothermicity. These results indicate that the polarization function is very important and indispensable to estimate the activation energy and the reaction energy.

- (3) When polarization functions were added on  $\text{CO}_2$ , introduction of electron correlation changes the activation energy and the reaction energy only a little. Consistent with these results, no instability of the HF wave-function was observed at the transition state. This is because the H ligand moves toward  $\text{CO}_2$  as a hydride ligand, in other words, the C-H bond between  $\text{CO}_2$  and H ligand is formed not in a homolytic way but in a heterolytic way accompanied with the strong charge transfer from the H ligand to  $\text{CO}_2$ .
- (4) The  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{III}}\text{-H}$  bond reaches the transition state much more late than the other  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{I}}\text{-H}$  and  $\text{Cu}^{\text{I}}\text{-H}$  bonds, whereas the former is only slightly less exothermic than the  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{I}}\text{-H}$  bond. This is because the charge-transfer from  $[\text{RhH}_2(\text{PH}_3)_3]^+$  to  $\text{CO}_2$  is weak and  $\text{CO}_2$  must closely approach the H ligand to break the strong  $\text{Rh}^{\text{III}}\text{-H}$  bond. In the transition state, therefore, formate is mostly formed and strongly interacts with Rh in a  $\eta^1$ -coordinating way at the trans-position of the H ligand. This geometrical feature is unfavorable because of the strong trans-influence of the H ligand. Thus,

the  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{III}}\text{-H}$  bond requires the highest activation energy. In the other  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{I}}\text{-H}$  and  $\text{Cu}^{\text{I}}\text{-H}$  bonds, such situation does not emerge, and therefore, the activation energy of these insertion reactions is much lower than the  $\text{CO}_2$  insertion into the  $\text{Rh}^{\text{III}}\text{-H}$  bond. From this result, we can predict that the structure B of  $\text{RhH}_2(\text{PH}_3)_3$  shown in Scheme 8.1 is more favorable for the  $\text{CO}_2$  insertion, because the formate is formed at the *trans* position of not the H ligand but the  $\text{PH}_3$  ligand.



Scheme 8.1

In chapter 7, *ab initio* MO/MP4 studies were carried out on the oxidative addition of the  $\text{Si-X}$   $\sigma$ -bond ( $\text{X} = \text{H}, \text{C},$  or  $\text{Si}$ ) to  $\text{Pd}(\text{PH}_3)_2$ . This reaction is involved in several catalytic reactions such as hydrosilation and bis-silation of alkenes and alkynes as an important elementary process. The results obtained are compared with several previous works, and detailed insight into this kind of reaction is presented, as follows:

- (1) The  $\text{Si-X}$  oxidative addition to  $\text{Pd}(\text{PH}_3)_2$  proceeds with lower activation energy but lower exothermicity than it to  $\text{Pt}(\text{PH}_3)_2$ . The lower exothermicity arises from the fact that the  $\text{Pd-X}$  bond is weaker than the  $\text{Pt-X}$  bond, as

expectedly. Unexpected result of the lower activation energy is attributed to the lower distortion energy and the relatively high  $d_{\pi}$  orbital energy of  $\text{Pd}(\text{PH}_3)_2$  at the transition state.

(2) An interesting prediction is also possible for the reductive elimination which is the reverse reaction of the oxidative addition. For instance, the reductive elimination of  $\text{Pd}(\text{SiH}_3)(\text{CH}_3)(\text{PH}_3)_2$  is calculated to proceed with only 8 kcal/mol of the activation energy while that of  $\text{Pt}(\text{SiH}_3)(\text{CH}_3)(\text{PH}_3)_2$  is calculated to require the 39 kcal/mol of the activation energy. This result suggests that the reductive elimination is much more difficult in *cis*- $\text{Pt}(\text{SiH}_3)(\text{PH}_3)_2$  but rather easy in the Pd-analogue.

(3) From these results, we can expect that the palladium(0) complex is more useful as a catalyst for the reaction including both oxidative addition and reductive elimination of Si compounds than the platinum(0) complex; for instance, if the insertion of alkene and alkyne into the Pd-SiH<sub>3</sub> bond easily occurs, the palladium(0) complex is more useful for the bis-silylation of olefin, acetylene, butadiene, etc. than the platinum(0) complex.

In this thesis, theoretical studies with the *ab initio* MO method were carried out on several elementary reaction steps involved in catalytic reactions by enzymes and transition-metal complexes. We obtained detailed theoretical informations, such as geometries, electronic structures, and bonding natures of the intermediates and transition states, activation energies and reaction energies

in the examined reaction steps. These informations are very useful to understand well the catalytic reactions. Thus, the ab initio MO method is considered to be powerful means in investigating catalytic reactions, and in designing a good catalyst.