Analysis of Cooperativity in Metallic Glass Forming Liquids

Masaru Aniya^{1, a}, and Masahiro Ikeda^{2, b}

¹Department of Physics, Graduate School of Science and Technology, Kumamoto University, Kumamoto 860-8555, Japan

²Course of General Education, Natural Science, Applied Physics, Fukui National College of Technology, Geshi-cho, Sabae, Fukui 916-8507, Japan

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Abstract. The relation between fragility and cooperativity of atomic motion in bulk metallic glass forming liquids is studied based on the bond strength-coordination number fluctuation model. The model describes the temperature dependence of the viscosity in terms of the mean values of the bond strength, coordination number and their fluctuations of the structural units that form the melt. According to the model, the cooperativity increases with the increase of fragility. The model estimates that the magnitude of the cooperativity $N_{\rm B}$ extends approximately from 7 to 60 structural units, depending on the material. The temperature dependence of $N_{\rm B}$ for different metallic glass forming systems reveals that $N_{\rm B}$ increases with the decrease of temperature. The relation between $N_{\rm B}$ and diffusivity of atoms is discussed briefly.

Introduction

Recently, much attention has been devoted to understand the mechanism of glass transition and structural relaxation in supercooled liquids. By decreasing the temperature of the melt, the glass-formation process takes place, which is accompanied by a drastic increase of the viscosity and structural relaxation time. The process is also accompanied by a growth of the size of the heterogeneity that develops in the supercooled liquid. The temperature dependence of the viscosity or relaxation time can be characterized by using the concept of fragility, which quantifies the degree of deviation from the Arrhenius behavior. Concerning the relation between fragility, cooperativity of atomic motions and heterogeneity, some studies have been done [1-5]. In particular, the correlation length of the heterogeneity and the number of molecules involved on it has been evaluated using different approaches [6-8]. These studies indicate that no consensus exists regarding the relation between fragility and cooperativity. Some studies indicate that the cooperativity increases with the fragility in accord with our intuitive expectation. Others state that no clear correlation exists. These situations indicate the need of further studies from different points of views. Recently, we have started a study directed to elucidate the above relation [9]. The present paper is a continuation of such program.

Multicomponent bulk metallic glasses have unique properties such as extraordinary high strength, low ductility, high hardness, excellent corrosion resistance and high thermal stability of their supercooled liquids. To exploit the excellent properties of bulk metallic glasses, a good understanding on fundamental materials properties is indispensable. For instance, the problem of shear bands discussed widely in the processing of glassy metallic alloys [10-12] is intimately related with the subject of the present paper. In the following, the cooperativity and fragility of metallic glass forming supercooled liquids is investigated by the bond strength-coordination number fluctuation (BSCNF) model proposed and developed in our group [13-17].

The Bond Strength-Coordination Number Fluctuation Model

The BSCNF model was introduced based on the physical picture that the viscous flow of the melt occurs by breaking or twisting the bonds between the structural units [13]. According to this model, the temperature dependence of the viscosity is described in terms of the mean bond strength E_0 , the mean coordination number Z_0 , and their fluctuations, ΔE , ΔZ , of the structural units that form the melt.

$$\ln\left(\frac{\eta}{\eta_0}\right) = \frac{Cx + Cx^2 \left[\left\{\ln\left(\frac{\eta_{T_g}}{\eta_0}\right) + \frac{1}{2}\ln(1-B)\right\} + \frac{1}{2}\ln(1-B)\right\} + \frac{1}{2}\ln(1-B) + \frac{1}{2}\ln(1-B) + \frac{1}{2}\ln(1-Bx^2), \quad (1)$$

where $B = \frac{(\Delta E)^2 (\Delta Z)^2}{R^2 T_g^2}$, $C = \frac{E_0 Z_0}{R T_g}$ and $x = \frac{T_g}{T}$.

Here, T_g is the glass transition temperature and R is the gas constant. η_0 and η_{Tg} are the values of the viscosities at high temperature limit and at T_g , respectively. The fragility index m is obtained from Eq. (1) as

$$m = \left[\frac{\mathrm{dlog}\eta}{\mathrm{d}(T_g/T)}\right]_{T_g} = \frac{B - C + 2\left[\ln\left(\frac{\eta_{T_g}}{\eta_0}\right) + \frac{1}{2}\ln(1-B)\right]}{\ln(10)(1-B)} .$$

$$(2)$$

Applications of the above Eqs. (1) and (2) to various materials have revealed that highly interconnected network glass forming materials or strong systems such as SiO₂ are characterized by large value of *C* and small value of *B*. On the other hand, fragile systems such as ZrF_4 -BaF₂-LaF₃-AlF₃ (ZBLA) are characterized by small value of *C* and large value of *B* [14]. The values of *B* and *C* are obtained by fitting Eq. (1) to the experimental data of viscosity. It should be noted that the expressions of the viscosity and fragility given above are written in terms of the parameters *B* and *C* which have clear physical meanings as defined in Eq. (1). Theoretically, it has been shown that the parameters *B* and *C* are interrelated as [16].

$$C = \frac{2\gamma(1-B)}{2\gamma + \sqrt{B}(1+\gamma^2)} \left[\ln\left(\frac{\eta_{T_g}}{\eta_0}\right) + \frac{1}{2}\ln(1-B) \right],$$
(3)

where
$$\gamma = \frac{\left|\Delta E\right| / E_0}{\left|\Delta Z\right| / Z_0}$$
.

It is worth to note that in the case where the condition $|\Delta E|/E_0 = |\Delta Z|/Z_0$ is satisfied, that is when the ratio between the fluctuations of energy and coordination number becomes equal, Eq. (1) follows closely the behavior of the Vogel-Fulcher-Tammann (VFT) equation widely used in the literature [16, 17].

A quantity defined as $N_{\rm B} = E_{\eta}/(E_0Z_0)$, where E_{η} is the activation energy for viscous flow has been introduced in the framework of the BSCNF model [14]. This quantity has been interpreted to give the number of structural units involved in the viscous flow. In other words, this quantity describes the cooperativity of molecular motions involved in the structural relaxation. In terms of the parameters *B* and *C*, $N_{\rm B}$ is written as

$$N_{B} = \frac{B - C + 2\left[\ln\left(\frac{\eta_{T_{g}}}{\eta_{0}}\right) + \frac{1}{2}\ln(1 - B)\right]}{(1 - B)C} \quad .$$
(4)

By comparing Eq. (2) and Eq. (4), we note that the cooperativity is related with the fragility.

Relation between fragility and cooperativity

Many studies were devoted to understand the relation between fragility and cooperativity [6, 18]. Fig. 1 shows the relation between N_B and m for different materials evaluated based on the BSCNF model. The numbers of correlated units evaluated by other approaches such as those based on the Donth formula, N_{α} [6], the four-point correlation functions, $N_{\text{corr},4}$ [7], and the thermodynamic cooperativity discussed by Wang, N_c^T [8] are shown for comparison. The lines (L₁-L₃) describe the curves calculated with different values of γ and $a_T = \ln(\eta_{Tg}/\eta_0)$. It is noted that a large number of data points follow the line L₁. Fig. 1 indicates that N_B increases with m. The values of N_B extend from few to about 60 structural units, depending on the value of m. It seems that the estimations N_{α} and N_c^T follows a different trend. According to the last estimation, the cooperativity does not depend or depends only weakly on m.



Fig. 1. Relation between $N_{\rm B}$ at $T=T_{\rm g}$ and the fragility index *m*. The numbers of correlated units evaluated by other approaches, N_{α} [6], $N_{\rm corr,4}$ [7], and $N_{\rm c}^{\rm T}$ [8] are also shown. The lines (L₁-L₃) describe the curves calculated with different values of γ and $a_{\rm T} = \ln(\eta_{Tg}/\eta_0)$.

To the best of our knowledge, information concerning the number of atoms or size of the regions that move cooperatively in the viscous flow in metallic systems is limited. From this point of view, the BSCNF model is useful, because, once having the values of *B* and *C*, we can estimate easily the values of *m* and $N_{\rm B}$. An example is shown in Fig. 2.



Fig. 2. Relation between N_B and m at $T = T_g$ in metallic glass forming systems. In the table, the values of B and C for each compound are given. The parameters for the compounds No. 10–14 were obtained from the analysis of relaxation time. Experimental data are taken from [19-22].

Temperature dependence of the cooperativity

The results shown in Fig. 2 were obtained at $T = T_g$. The temperature evolution of N_B is a topic of considerable interest, because it reflects the development of interconnection of structural units in the glass formation process. In Fig. 3, the $N_B(T)$ in metallic glass forming systems is shown. The temperature dependence were obtained from $N_B(T) = E_{\eta}(T)/(E_0Z_0)$, that is, from the temperature dependence of the activation energy of the viscous flow. As expected intuitively, we note that $N_B(T)$ increases with the decrease of temperature. In some systems such as Ni_{59.5}Nb_{40.5}, a large change of $N_B(T)$ is discernible.



Fig. 3. Temperature dependence of the cooperativity $N_{\rm B}$ in metallic glass forming systems. The compounds are the same to those given in Fig. 2.

Cooperativity and fractional Stokes-Einstein relation

The results shown in the previous section indicate that considerable number of atoms move cooperatively in the structural relaxation process. This observation prompts us to investigate how the diffusion is involved in the collective motion. The subject relates with the Stokes-Einstein (SE) relation. Recent studies have revealed that the SE relation is violated, particularly, in the proximity of the glass transition temperature [23-25]. In these cases, the fractional Stokes-Einstein (FSE) relation given by

$$D \propto \left(\frac{T}{\eta}\right)^p, \quad (0$$

has been invoked. Here, *p* describes the deviation from the original SE law, p = 1. In other words, it gives a measure on the degree of coupling between diffusion and viscous flow. In a recent study, the relation between diffusivity and cooperativity of different supercooled liquids near T_g have been analyzed in the framework of the BSCNF model [26, 27]. As shown in Fig. 4, for the case of Pd₄₃Cu₂₇Ni₁₀P₂₀, the value of *p* is p = 0.74, which is in accordance with the literature value [28]. This value is also close to the values of *p* reported for other systems such as *o*-terphenyl (p = 0.74) and Na₂O-2SiO₂ (p = 0.71). The analysis revealed also that log*D* and log(T/η) vary linearly with log(N_B^{-1}) [27].



Fig. 4. Relation between $\ln D$ and $\ln(T/\eta)$ in Pd₄₃Cu₂₇Ni₁₀P₂₀.

Conclusion

The BSCNF model describes the temperature dependence of the viscosity of many kinds of glass forming liquids in terms of the mean values of the bond strength, coordination number and their fluctuations of the structural units that form the melt. In the present paper, the relation between fragility and cooperativity of atomic motion in bulk metallic glass forming liquids has been studied based on the BSCNF model. The result indicates that the cooperativity increases with the increase of fragility. The model estimates that the magnitude of the cooperativity $N_{\rm B}$ of metallic systems extends approximately from 7 to 60 structural units. Furthermore, the BSCNF model predicts that by lowering

temperature, the values of $N_{\rm B}$ increases. The sensitivity to the variation of temperature depends on the specific material. The relation of $N_{\rm B}$ with the atomic transport properties was also briefly discussed.

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