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## Testing Method for Determination of Microscopic Fracture Toughness for Rock Materials

### Reference

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### ABSTRACT

The fracture behavior of rocks is known to depend on the microstructures of the rocks: the distribution and orientation of the microcracks, and the type, size, and shape of mineral grains. To explain quantitatively the effect of the microstructures on the fracture of rocks, the determination of the fracture toughness of grain and grain boundaries, namely, the microscopic fracture toughness (MFT), is necessary. The authors developed a testing method for determination of MFT for rock materials. A micro-sized specimen of a cantilever beam type with dimensions of 10 by 10 by 50  $\mu\text{m}$  was used in this testing method, and we built a special testing machine for this specimen. Micro-sized specimens were made within grains of Iksan granite by Focused Ion Beam machining, and the MFT of its constituents—plagioclase, alkali feldspar, and quartz—was determined using this testing method at room temperature. The MFT varied widely and the results are discussed based on the mineralogical knowledge. This testing method will be helpful to more accurately interpret the fracture behavior.

### Keywords

rock mechanics, microscopic fracture toughness, granite, mineral grain, size effect

## Introduction

The utilization of underground resources has become diversified, enlarged, and complex, e.g., exploitation of energy resources (geothermal energy and shale gas, etc.), underground petroleum storage, carbon dioxide geological storage, and disposal of high-level nuclear waste. The excavation and drilling techniques that are used under higher temperature and pressure for construction of larger and deeper underground spaces, and empirical as well as theoretical estimation methodologies for estimation of the long-term stability of rock structures, must be developed and improved. Mechanisms of rock fracture and especially the linear elastic fracture mechanics (LEFM) have been used to explain rock engineering problems. In LEFM, a mechanical property known as the fracture toughness describing resistance to crack initiation is important for understanding of the fracture behavior of the materials.

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Several testing methods have been suggested by the International Society for Rock Mechanics (ISRM) for determining the Mode I (opening mode) fracture toughness of rock materials: the short rod test, chevron bend test, cracked chevron notched Brazilian disk test, and semicircular bend (SCB) test (Franklin et al. 1988; Fowell 1995; Kuruppu et al. 2014). The fracture toughness determined by the testing methods is known to depend on the microstructures of rocks; the distribution and orientation of microcracks; and the type, size, and shape of mineral grains (Nasseri and Mohanty 2008; Kataoka, Obara, and Kuruppu 2011,2015). Rock is an inhomogeneous material. Crystalline rock, such as granite, for instance, consists of a completely crystalline assemblage of minerals and microcracks as mechanical weaknesses are included within mineral grains. Kataoka, Obara, and Kuruppu (2011,2015) estimated the anisotropy of the Mode I fracture toughness of a crystalline rock (Rustenburg granodiorite) by the SCB tests and analyzed the fracture states using X-ray computed tomography images of the specimens after the test. It was reported that the observed fractures tended to go across grains with lower density and along grain boundaries, rather than across grains with higher density, and that the anisotropic characteristics of the fracture toughness were shown because of the orientation of mineral grains. It can be considered that the fracture toughness varied depending on the mineral type of grains and grain boundaries.

The fracture toughness of grains, including their boundaries, which is described as microscopic fracture toughness (MFT) in this article, is an important property in understanding the fracture behavior of rock materials. To estimate the microscopic mechanical properties (the elastic modulus, tensile strength, fracture toughness, and fatigue life) of the alloys used for Micro Electro Mechanical Systems or Micro System Technology devices, a mechanical testing machine for a micro-sized specimen was developed by Higo et al. (2000). Takashima and Higo (2005) and Halford et al. (2005) estimated the fracture toughness of amorphous and fully lamellar alloys using the micro-sized specimens and investigated the effects of the specimen size on fatigue and fracture. If this testing method can be introduced to the field of rock mechanics, it should be useful and effective in evaluating the MFT to explain quantitatively the effect of the microstructures on the fracture behavior and to clarify the fracture mechanisms of rocks.

Recently, the authors proposed a testing method for determination of MFT for rock materials (Kataoka et al. 2014; Jeong, Obara, and Kataoka 2016; Jeong et al. 2017). However, only a few experiments were performed during the investigations, and the discussion of the size effect on the fracture toughness and the variation of the MFT given was not sufficient. In this article, this new testing method is introduced to measure the MFT of granite, and the test results (including new ones) are reported. Micro-sized specimens were prepared using Iksan granite with Focused Ion Beam (FIB) machining to be tested using the special

testing machine developed for this purpose. The MFT of plagioclase, alkali feldspar, and quartz within the granite was determined using this testing method at room temperature. The determined MFT was discussed based on the mineralogical knowledge. The size effect on the fracture toughness and the variation of the MFT were also investigated.

## Testing Method

### DETERMINATION OF FRACTURE TOUGHNESS

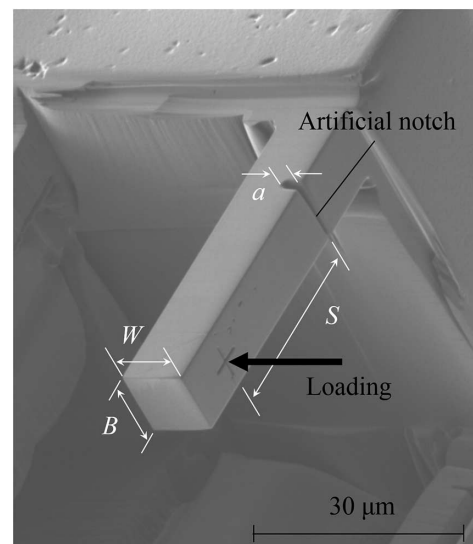
A micro-sized specimen used for the fracture toughness test is a cantilever beam type with an artificial notch as a crack and is shown in Fig. 1. The dimensions of the beam are approximately 10  $\mu\text{m}$  thick and wide and 50  $\mu\text{m}$  in length. The artificial notch with a depth of approximately 3  $\mu\text{m}$  is located near the fixed end of the cantilever beam. Load is applied at a point on the side surface at a distance of 30  $\mu\text{m}$  from the notch by a diamond chip with a curvature of 5  $\mu\text{m}$ . The Mode I fracture toughness,  $K_{IC}$ , as a critical value of the stress intensity factor, is estimated from maximum load  $P_{\max}$  using the following equation for the stress intensity factor for a single edge notched cantilever beam (Murakami 1987):

$$K_{IC} = \frac{6P_{\max}S}{W^2B} \sqrt{\pi a} Y(a/W) \quad (1)$$

where:

- $a$  = depth of the artificial notch,
- $W$  = thickness of the cantilever beam,
- $B$  = width of the cantilever beam,

**FIG. 1** SIM image of a micro-sized specimen, which is made using quartz (No. Q-3 in Table 2) from Iksan granite (after Jeong, Obara, and Kataoka 2016).



$S$  = distance between the loading point and the notch, and  
 $Y$  = function of dimensionless notch length  $a/W$ , as follows:

$$Y(a/W) = 1.122 - 1.40(a/W) + 7.33(a/W)^2 - 13.08(a/W)^3 + 14.0(a/W)^4 \quad (2)$$

### SPECIMEN

Iksan granite was used as the test material. This rock was produced in Iksan, North-Jeolla Province (Jeollabuk-do), Korea. The uniaxial compression test and Brazilian disk tensile test of this rock were performed using a few centimeters of specimens (Kataoka, Obara, and Kuruppu 2015). The elastic wave velocity of this rock was also measured (Kataoka and Obara 2013; Kataoka, Obara, and Kuruppu 2015), and the results are listed in Table 1. A thin section was observed using a polarization microscope to investigate the composite minerals and the microstructures. The mineral types of quartz, plagioclase, alkali feldspar, biotite, etc. were found, as shown in Fig. 2, and the average grain size was estimated as 0.6–0.8 mm (Kataoka and Obara 2013; Kataoka, Obara, and Kuruppu 2015).

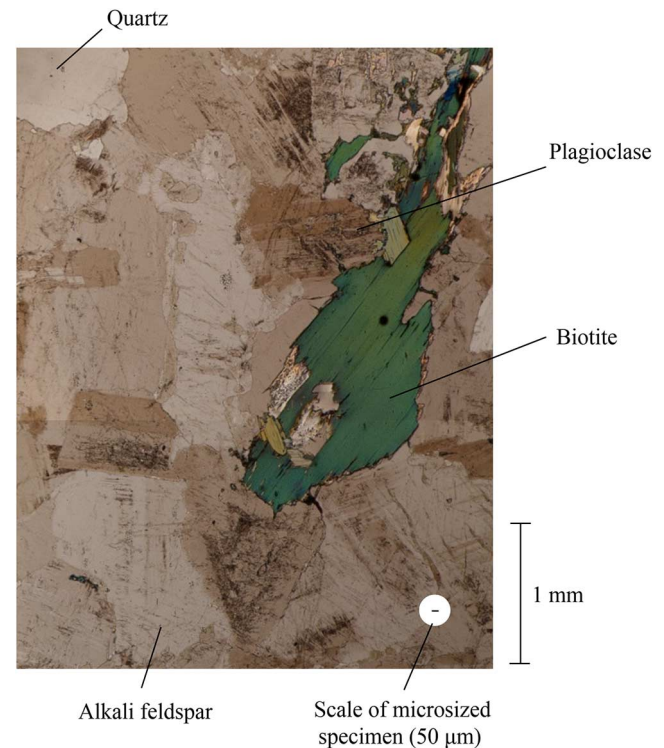
To prepare the micro-sized specimen, a rock block was cut into a rectangular parallelepiped with dimensions of 3 by 5 by 7 mm, as shown in Fig. 3a. The surfaces of the rectangular parallelepiped were polished smoothly and the micro-sized specimen was prepared along a side that was 7 mm in length. To determine the MFT of a single mineral grain, the micro-sized specimen was prepared within grain-avoiding flaws (such as microcracks). An Electron Probe Microanalyzer (EPMA) was used to specify the mineral types of a grain.

Micro-sized specimens were made by a FIB instrument (Quanta 3D 200i, Fei Company, Hillsboro, OR). Prior to the start of the preparation, the surfaces of the rectangular parallelepiped were coated with gold by sputter deposition. The rectangular parallelepiped was then fixed into a holder to allow FIB micromachining. The FIB instrument uses a gallium ion source and operates at an accelerating voltage of 30 kV with a working distance of 30 mm. Fig. 3b–d shows the preparation process of the micro-sized specimen. FIB hits gray areas on the rectangular parallelepiped surfaces shown in Fig. 3b and c at a current of 20 or 7 nA. The materials in these areas are removed by micromachining with FIB sputtering. The shape of a cantilever beam was made

**TABLE 1** Material properties of Iksan granite (after Kataoka et al. 2013,2015).

Properties	Values
Uniaxial compressive strength	167–170 MPa
Young's modulus	19.0–19.2 GPa
Tensile strength	10.3–11.4 MPa
Elastic wave velocity	4.0–4.2 km/s

**FIG. 2** Mineral grains of Iksan granite as shown in a thin section. The scale of the micro-sized specimen is indicated (Kataoka et al. 2014; Jeong et al. 2016,2017).

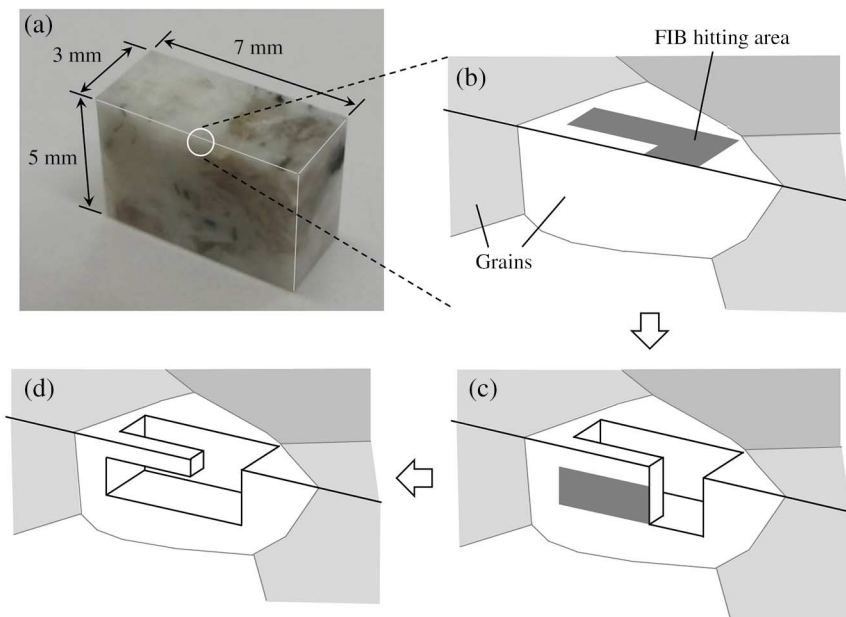


roughly at such a high current. After this process, the surfaces of the cantilever beam were made smooth by FIB using a lower current of 3 nA, making the beam size, as shown in Fig. 1. The dimensions of the beam were measured by a Scanning Ion Microscope (SIM) with an image resolution of 0.1  $\mu\text{m}$ . Then, the artificial notch and the alignment markings of the loading point were prepared by FIB machining. To make the depth of the artificial notch approximately 3  $\mu\text{m}$ , a thin FIB at a current of 0.1 nA was emitted in the direction of the beam width, and the curvature of its tip was made to 0.25  $\mu\text{m}$ . This preparation process does not need a special FIB operation skill because of the simple shape of the specimen. Moreover, the effect of mineral types on the machining speed and accuracy showed little difference.

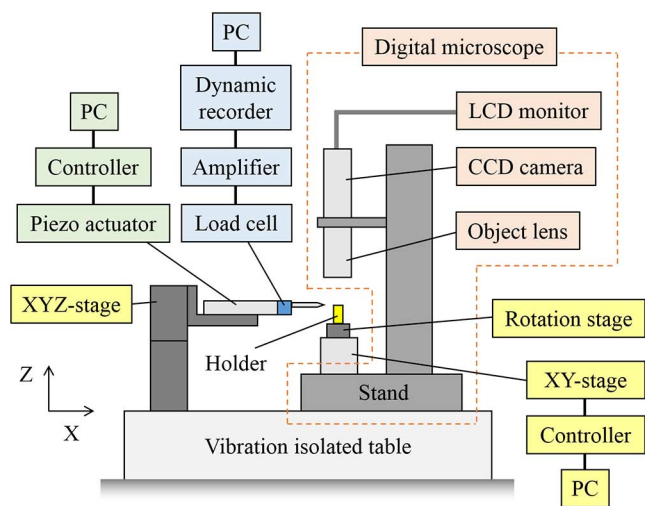
### TESTING MACHINE

The authors built a testing machine for the fracture toughness test using the micro-sized specimens. A block diagram of this testing system and the view of the specimen are shown in Figs. 4 and 5, respectively. The advantage of this testing machine is that a position alignment and the loading of the micro-sized specimen are provided by using six accurate stages, a piezo actuator, and a high-powered digital microscope. This testing machine was fixed on a vibration isolated table. The micro-sized specimen within the rectangular parallelepiped is put on a loading holder fixed on a

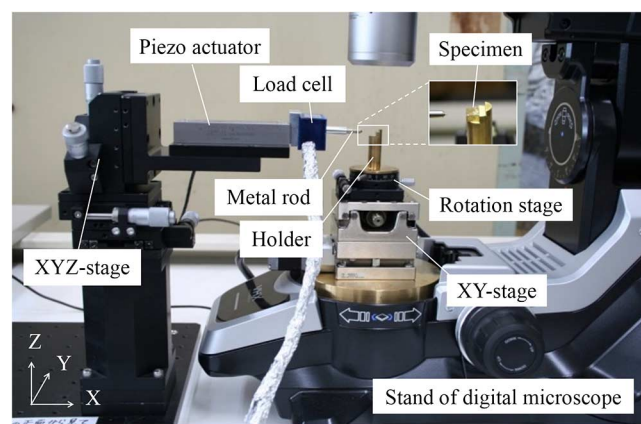
Preparation of micro-sized specimen: (a) rectangular parallelepiped of Iksan granite; (b)–(d) preparation process by FIB (after Kataoka et al. 2014; Jeong, Obara, and Kataoka 2016).



**FIG. 4** Block diagram of testing system for the micro-sized specimen. To provide a position alignment of the micro-sized specimen for loading, six accurate stages are equipped with a high-powered digital microscope (after Jeong, Obara, and Kataoka 2016).



**FIG. 5** View of the specimen placed at the mechanical testing system (after Jeong et al. 2016,2017).



rotation stage with a rotation resolution of  $0.2^\circ$  and an XY-stage with a translation resolution of  $0.1\text{ }\mu\text{m}$ .

A metal rod is attached to an actuator, which is installed on manual type XYZ-stages with a translation resolution of 0.1  $\mu\text{m}$ . A diamond chip with a curvature of 5  $\mu\text{m}$  is installed at the tip of the metal rod. The load is applied by the diamond chip at the loading point of the micro-sized specimen. The lateral displacement of the metal rod with the diamond chip is applied by a

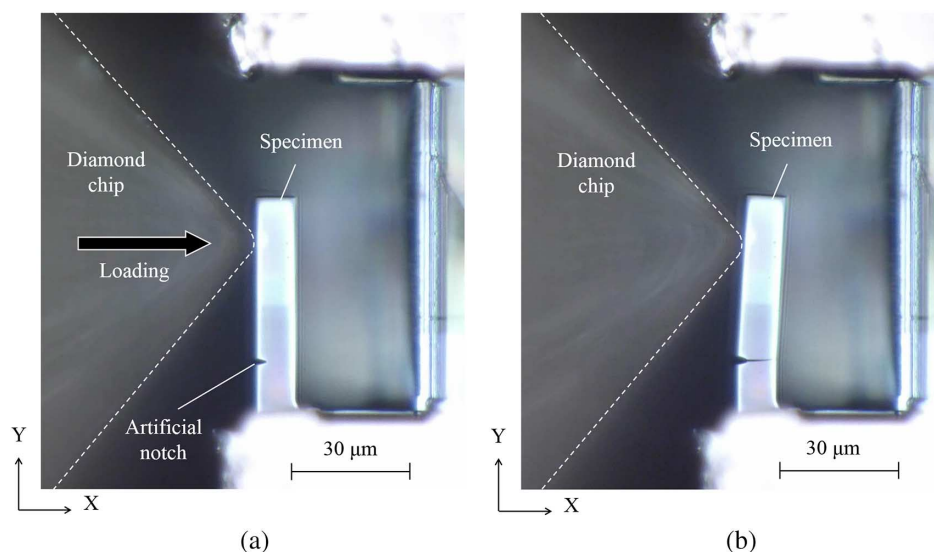
piezoactuator with a resolution of 0.2 nm and a maximum stroke of 38  $\mu\text{m}$ . With the six stages installed in the testing system, the positions of the micro-sized specimen and the diamond chip, and its loading direction can be adjusted with accuracy.

The rotation stage and XY-stage are fixed on a stand of a VHX-5000 digital microscope (Keyence, Osaka, Japan). The loading state shown in **Fig. 6**, as well as the adjustment of the positions of the specimen, can be observed in real time by the digital microscope with a magnification of 250 to 2,500. Load is measured by a load cell with a resolution of 20  $\mu\text{N}$  and a maximum of 200 mN equipped to the actuator. The loading rate was 0.1  $\mu\text{m/s}$ , and the sampling interval was 10  $\mu\text{s}$ .



**FIG. 6**

Loading state observed by the digital microscope with a magnification of 2,500: (a) start of the loading, (b) end of the loading. The crack propagation from the artificial notch tip can be observed (after Jeong, Obara, and Kataoka 2016).



## Experimental Results

The fracture toughness test was conducted at room temperature using the developed testing machine. The mineral type and size of micro-sized specimens and the test results are summarized in **Table 2**. The micro-sized specimens were prepared within the grains of plagioclase, alkali feldspar, and quartz of Iksan granite.

Load-displacement curves in the fracture toughness test are shown in **Fig. 7**. The load increases linearly with increasing displacement and the fracture suddenly occurs just after reaching maximum load,  $P_{\max}$ , for all the specimens. Both the  $P_{\max}$  value and the slope of the curve (deformability) vary widely from one specimen to the other, although in the same mineral type. The value of MFT  $K_{IC}$  was determined from the value of  $P_{\max}$  using Eq. 1. The MFT is also highly variable in value.

The fracture surfaces of specimens observed by the SIM after the test are shown in **Fig. 8**. The fractures of the feldspar group (plagioclase and alkali feldspar) shown in **Fig. 8a** and **b** do not initiate and propagate in the direction of the artificial notch straightly. On the other hand, as shown in **Fig. 8c**, the fracture of the quartz propagates straightly in almost the same direction as the artificial notch.

## Discussion

### VARIATION OF MFT

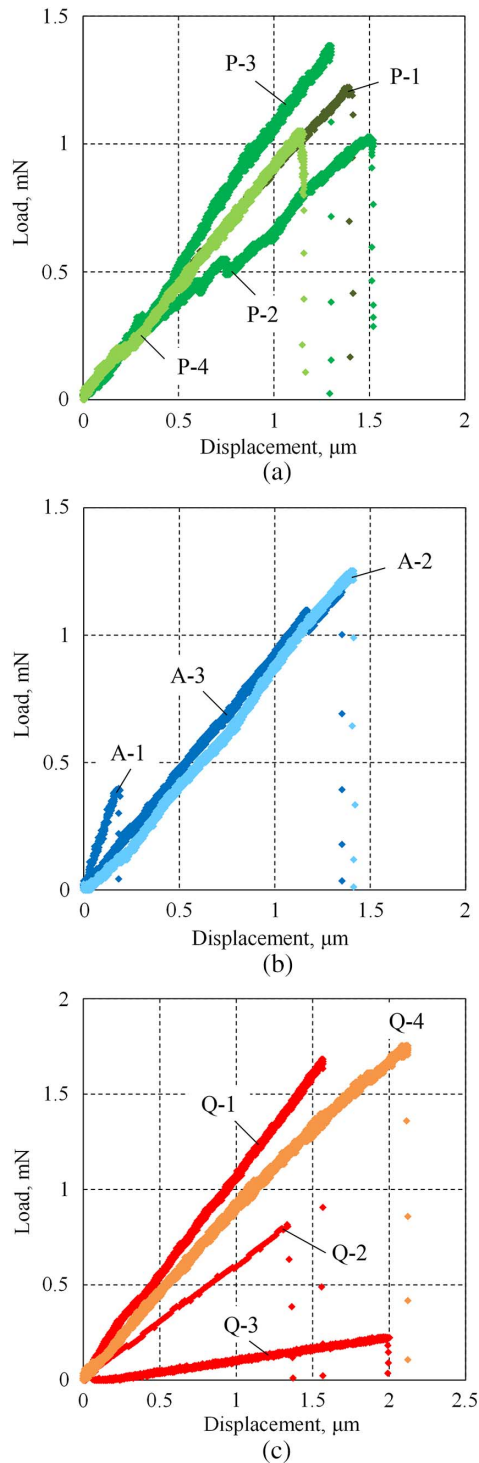
The variation of the MFT shown in **Table 2** is dependent on an existence of mechanical weak planes within the micro-sized specimens. The propagated direction of the fracture changes suddenly

**TABLE 2** Specimen dimensions and experimental results.

No.	Mineral	W (μm)	B (μm)	S (μm)	a (μm)	$P_{\max}$ (mN)	$K_{IC}$ (MN/m <sup>3/2</sup> )
P-1*	Pl	10.7	10.4	30.7	3.0	1.22	0.64
P-2	Pl	10.4	10.2	31.4	2.8	1.03	0.57
P-3	Pl	10.2	10.0	30.2	2.2	1.38	0.67
P-4	Pl	10.4	10.2	29.6	2.5	1.05	0.51
A-1†	Afs	9.6	11.0	29.4	3.2	0.40	0.25
A-2†	Afs	10.6	10.5	29.6	2.5	1.25	0.57
A-3	Afs	10.4	10.4	28.5	2.5	1.18	0.54
Q-1††	Qz	10.2	10.9	28.6	2.8	1.68	0.83
Q-2††	Qz	10.1	10.0	28.7	3.5	0.82	0.54
Q-3††	Qz	9.7	10.2	29.2	2.7	0.23	0.13
Q-4	Qz	10.2	11.2	30.5	2.5	1.75	0.83

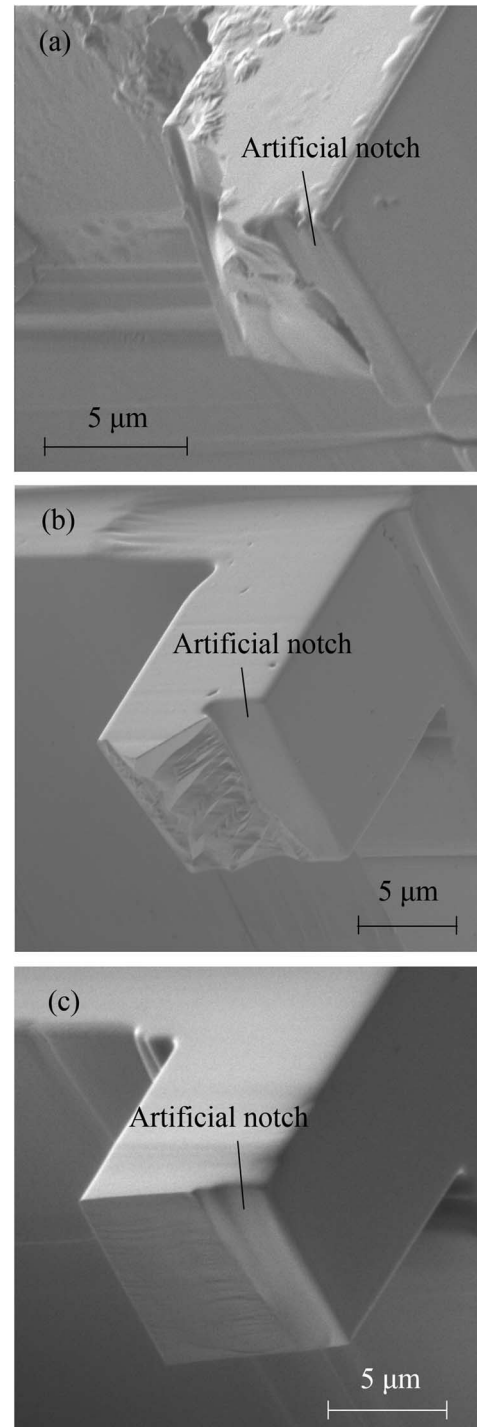
Note: Pl = Plagioclase; Afs = Alkali feldspar; Qz = Quartz; W, B, S and a = specimen dimensions shown in **Fig. 1**;  $P_{\max}$  = maximum load;  $K_{IC}$  = Mode I fracture toughness; \*, †, and †† at specimen No. heading indicate the data from Kataoka et al. (2014) and Jeong et al. (2016, 2017), respectively.

**FIG. 7** Load-displacement curves in the fracture toughness tests: specimens of (a) plagioclase, (b) alkali feldspar, and (c) quartz (some of the data are from Kataoka et al. (2014) and Jeong et al. (2016,2017)).



during the fracture process for the feldspar group (Fig. 8a and b). The feldspar group has two planes of cleavage meeting at or near  $90^\circ$ , forming mechanical weak planes (Lutgens and Tarbuck 1997;

**FIG. 8** SIM images of fracture surfaces of specimens after the test; (a) plagioclase P-1, (b) alkali feldspar A-1, and (c) quartz Q-2 (after Kataoka et al. 2014; Jeong et al. 2016,2017).



Nave 2017). The fracture state shown in Fig. 8a and b indicates the existence of cleavage within the specimens of the feldspar group. Moreover, shear fractures appear locally because of the mechanical weak planes in the mineral structure. The fracture may have

been due to the combination of both effects, resulting in the variation of the MFT.

Although the fracture of the quartz group propagates straightly in almost the same direction as the notch (Fig. 8c), there is also scattering in the MFT results (Table 2). Quartz frequently twins (Association for Geological Collaboration in Japan 1996; Amethyst Galleries, Inc., 1995). Twinning may follow the Dauphine law and the Brazil law and produces prism plane and rhombohedral plane. It is known that breakage occurs easily along these planes (Association for Geological Collaboration in Japan 1996). If the direction of the artificial notch is parallel to these planes, the fracture resistance in this case can be considered lower than that in the other directions. Thus, MFT of quartz is dependent on the direction of fracture. The mechanical weak planes can influence the MFT of rock mineral grains.

### SIZE EFFECT ON FRACTURE TOUGHNESS

Jeong et al. (2017) estimated the fracture toughness of Iksan granite using the SCB tests, which is suggested by ISRM as a standard testing method for the Mode I fracture toughness of rock (Kuruppu et al. 2014). In the tests, the semicircular disk specimens with various diameters ranging from 12.5 to 50 mm were used. Fig. 9 shows the relation between the fracture toughness and the specimen size (the radius  $r$  of the SCB specimens). In this figure, the MFT determined in this study is also plotted; the specimen size indicates the thickness  $W$  of the cantilever beam. It was observed that the fracture toughness of rocks increased with increasing specimen size. This trend was also observed in previous

studies (Ayatollahi and Akbardoost 2014; Kataoka and Obara 2015). The MFT is lower than the fracture toughness determined by the conventionally sized specimens.

As mentioned earlier, the effect of the mechanical weak planes on the MFT is significant in rock. Kataoka and Obara (2015) reported that the crack resistance decreases with the decrease in specimen size because the mechanical weak planes near the notch tip of the specimen can be assumed to be relatively large. The size effect on the fracture toughness of rock from micro-sized to conventionally sized specimens may be interpreted by this explanation.

Bazant (1984) and Bazant, Gettu, and Kazemi (1991) proposed the size effect law according to the nonlinear fracture mechanics caused by the existence of a microcracking zone, which is called the fracture process zone near the crack tip. The broken line in Fig. 9 shows the fracture toughness estimated by the SCB specimen calculated based on Bazant (1984), Bazant, Gettu, and Kazemi (1991), and Ayatollahi and Akbardoost (2014). The test results agree with the calculation.  $K_{IC}$  for an infinitely large specimen can be calculated as  $1.44 \text{ MN/m}^{3/2}$  when the specimen radius  $r \rightarrow \infty$ . However, the MFT tends to be larger than the calculated result for its size. Moreover, the fracture surfaces shown in Fig. 8 are similar to those of brittle material, such as glass and chalk (Bahat, Rabinovich, and Frid 2001; Gopalakrishnan and Mecholsky 2012). The load-displacement curves (Fig. 7) show that the compliance is not changed during increasing load and that the load falls just after reaching its maximum value in a brittle manner. These indicate that the estimation of the MFT is less affected by the fracture process zone. To make the mechanism clearer, a modification considering the nonlinearity (Barker 1979; Matsuki, Hasibuan, and Takahashi 1991) will also be necessary in future work.

MFT can correspond to the microscopic strength considered by Weibull's distribution (Weibull 1951). Fig. 10 shows the Weibull plot for the fracture toughness  $K_{IC}$  of Iksan granite determined by micro-sized specimens used in this study and the SCB specimens (Jeong et al. 2017). They follow the distribution given in Eq 3:

$$1 - F(K_{IC}) = \exp \left\{ - \left( \frac{K_{IC}}{\eta} \right)^m \right\} \quad (3)$$

where:

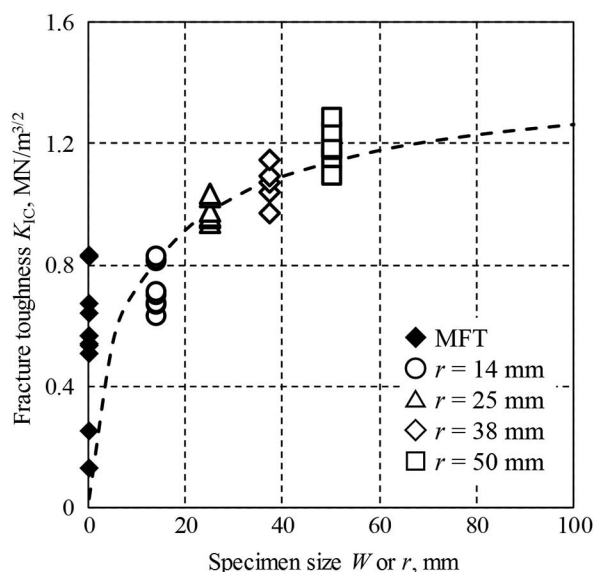
$F(K_{IC})$  = cumulative distribution function of  $K_{IC}$ ,

$m$  = shape parameter of the distribution, and

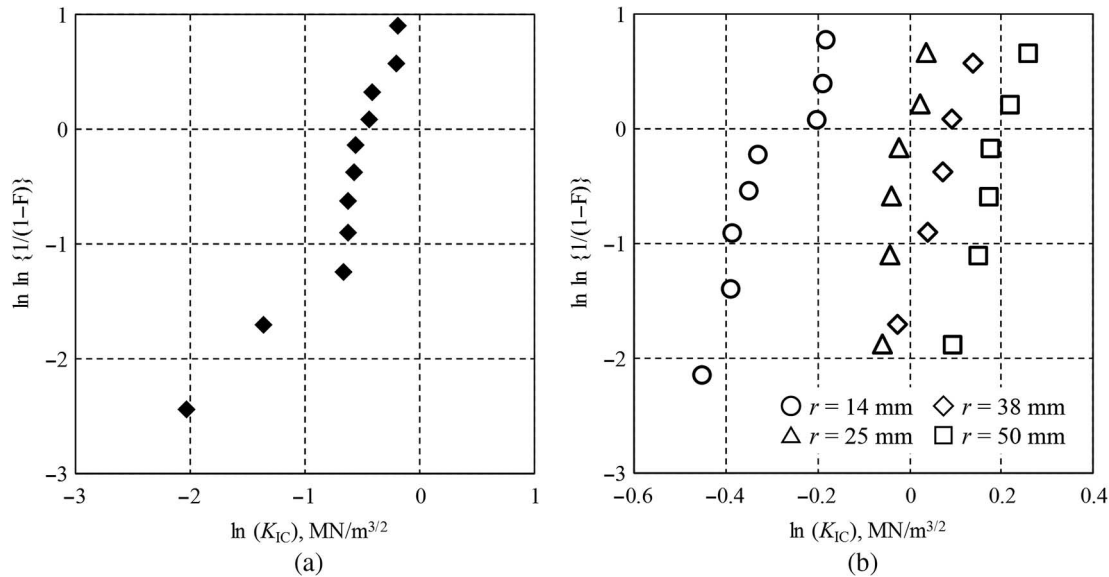
$\eta$  = scale parameter of the distribution.

$m$  is also known as the coefficient of uniformity, and the value is 1.66 for the MFT. The  $m$  value for  $K_{IC}$  determined by the SCB specimens with various radii ranged from 8.72 to 21.9 and were higher than that for the MFT. The  $m$  values for the uniaxial compressive strength and tensile strength of several rock types tend to be in the range of 10 to 35 (Shin et al. 2005) and are also higher

**FIG. 9** Relation between fracture toughness and specimen size for Iksan granite. The closed and open symbols indicate the values determined by the micro-sized and SCB specimens, respectively. The broken line indicates the calculated result based on the Bazant size effect law (Bazant 1984).



**FIG. 10** Weibull plot for the fracture toughness of Iksan granite determined by (a) micro-sized specimens and (b) SCB specimens. The symbols correspond to the ones in Fig. 9.



than that for the MFT. The inhomogeneity of rock materials plays a significant role in the fracture behavior of rocks so much so that it has been introduced into the models of some numerical simulations for rock fracturing (Cho, Ogata, and Kaneko 2003). The large variation of the microscopic strength used in previous studies (Tang 1997; Liu et al. 2002) is almost the same as that in the MFT observed in this study. It indicates that the variation of the MFT can be accommodated in the use of numerical simulations of rock fracturing.

## Conclusions

A testing method for the determination of the Mode I MFT for rock material was introduced in this article. Micro-sized specimens were prepared using Iksan granite by FIB machining. A special testing machine for the micro-sized specimen was developed. The MFT of plagioclase, alkali feldspar, and quartz within the granite was determined using this testing method. Results showed that the MFT varied widely in each micro-sized specimen, although in the same mineral type. Based on the mineralogical knowledge, it is concluded that the mechanical weak planes can influence the MFT of the rock. The size effect on the fracture toughness and the reasons for the variation of the MFT were also discussed.

The MFT determined by this testing method will be helpful to interpret the fracture behavior of rocks more accurately. By considering the MFT, the effect of the microstructures of rocks on the fracture behavior can be explained quantitatively. However, more experiments will be necessary to verify its repeatability, and, as

future work, we will perform additional MFT tests for artificial crystals of quartz in consideration of the existence of crystallographic axes, other types of mineral grains, and grain boundaries within rocks. The validation of the MFT estimated in this study might also require the use of other approaches, such as the J integral method and theoretical estimates of ideal  $K_{IC}$  of minerals (Tromans and Meech 2002,2004). Furthermore, if the MFT is used as a parameter of the numerical simulation for rock fracturing, this will lead to further understanding of the fracture mechanisms of rock.

## ACKNOWLEDGMENTS

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